

CS 925

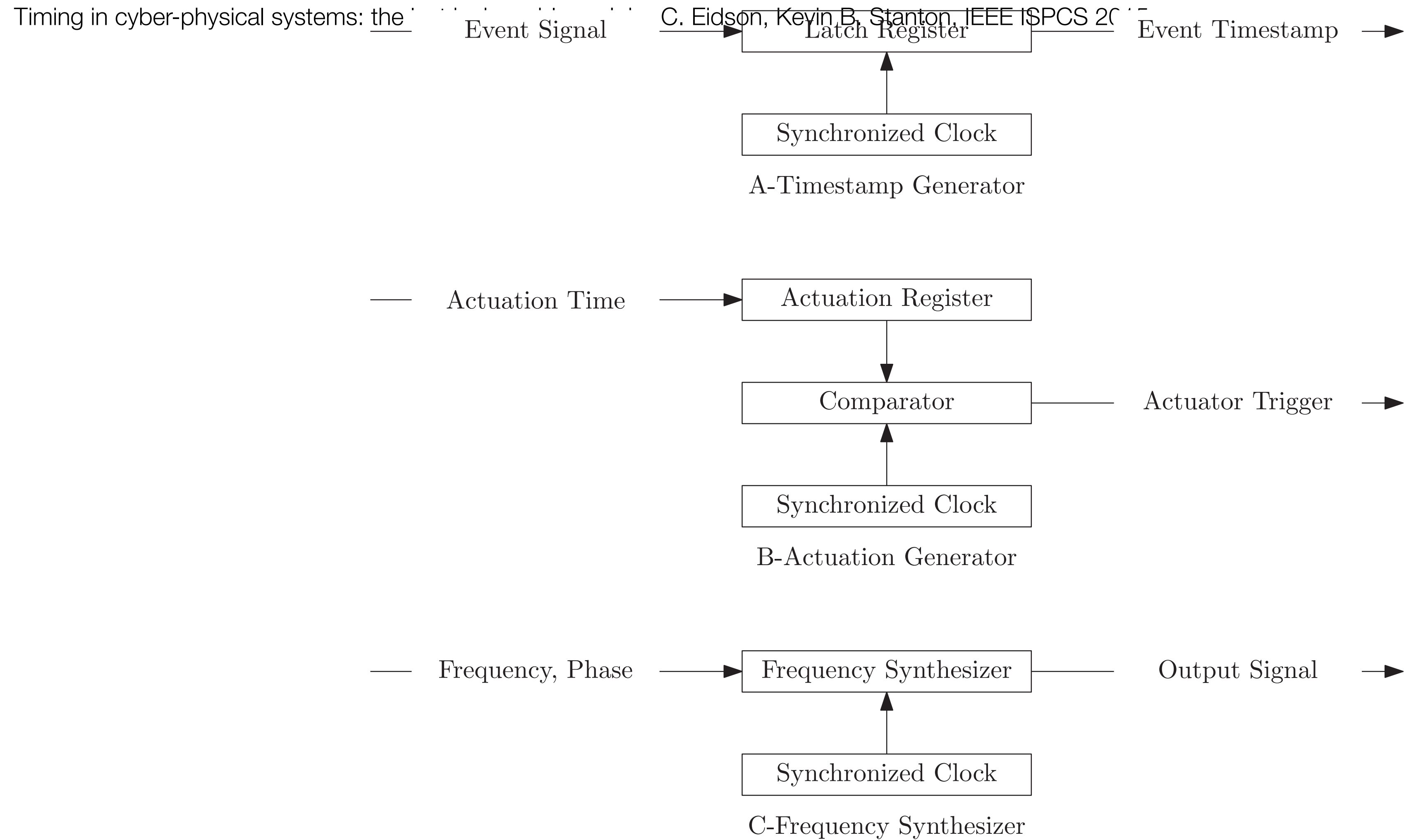
Lecture 21

Network-based

Time Synchronization

Tuesday, April 16, 2024

Motivation



Current Applications

▶ Navigation

- Satellite positioning
- Indoor navigation



▶ Telecom networks

▶ IoT networking

- e.g., LoRa

▶ Power grid

- Synchrophasor networks



Applications

- ▶ **Industrial automation**
 - Industry 4.0
- ▶ High-speed algorithmic **securities trading**
 - trade scheduling
 - globally-timestamped logs of trades (for audit)
- ▶ Professional **audio-video**
- ▶ High-energy particle **physics**



Applications

- ▶ Distributed **consensus** in blockchain algorithms (Algorand)
- ▶ **Consistency** in geographically-distributed data centers (Google)
- ▶ **Power conservation** in IoT (LoRa)
- ▶ Stereo **audio** (Apple HomePod)
- ▶ Delayed **message authentication** (IEEE 1588)

Three challenges

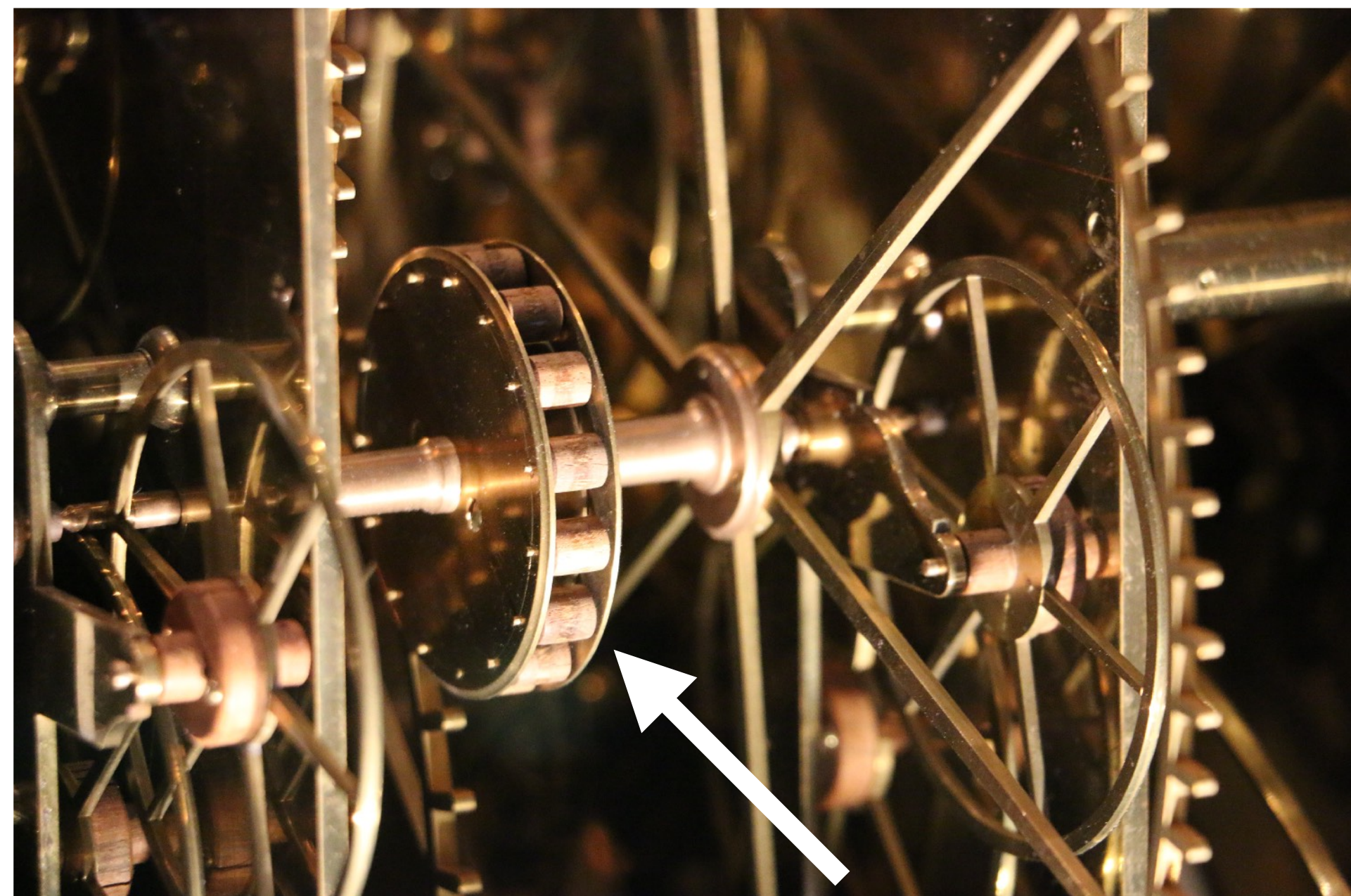
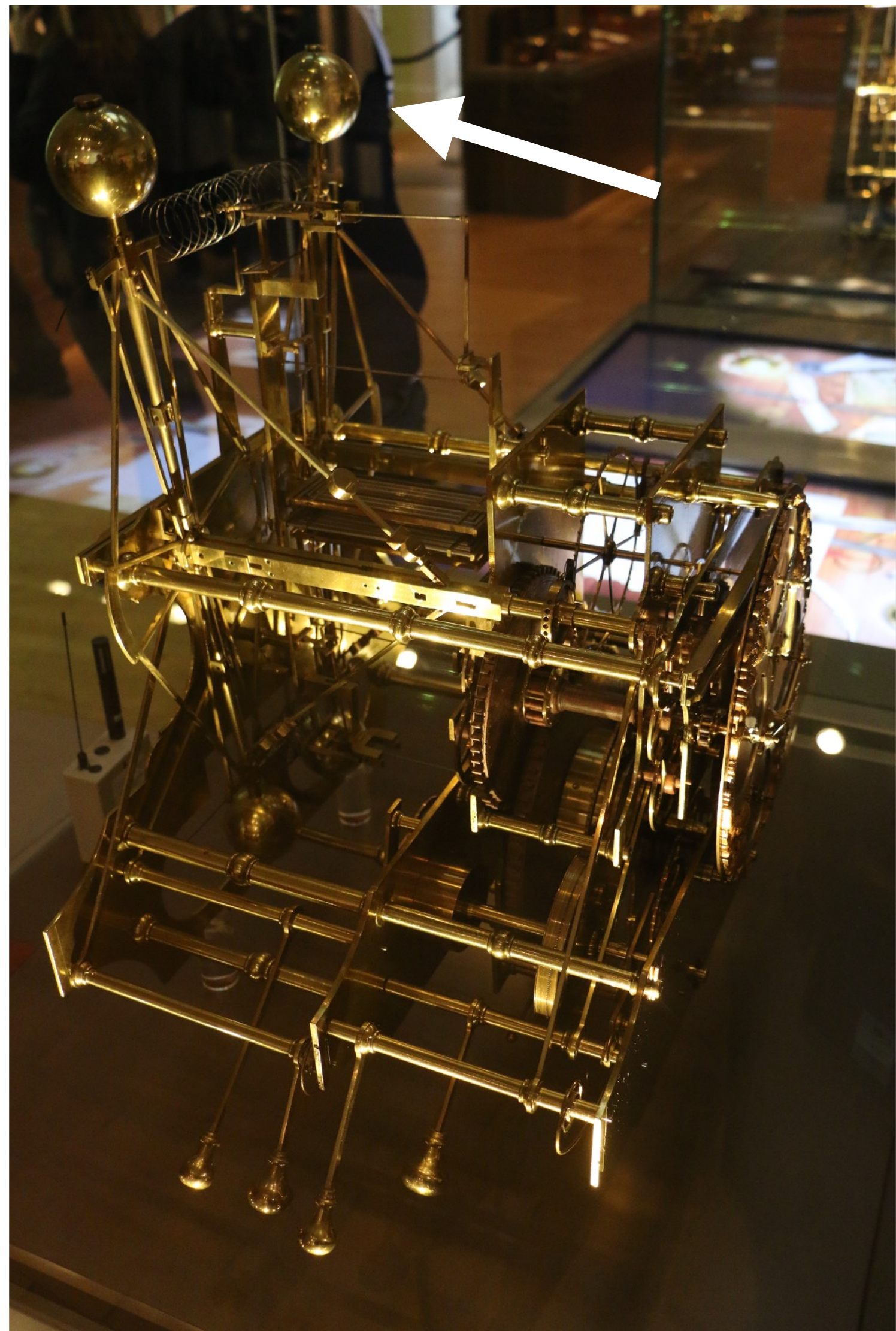
- ▶ What is the “correct” time?
 - “Clock in the sky” - time derived from astronomical observations
 - Atomic time (which one? TAI, UTC)
 - Says who? Consortium of national bureaus of standards
 - Mostly futile question when you bring in the theory of relativity
- ▶ Design a clock that **keeps the correct time** (syntonized with the reference)
- ▶ Design a mechanism for **time transfer**



5.

HOROLOGIA FERREA.
Rota æqua ferrea ætherisq; voluitur, Recludit æquè et hæc et illa tempora.

Precise clocks



John Harrison marine clocks
to be used to determine
ship's longitude



National time reference

- ▶ NIST 7 Cesium Frequency Standard (1993)



Time transfer

► Dropping balls...



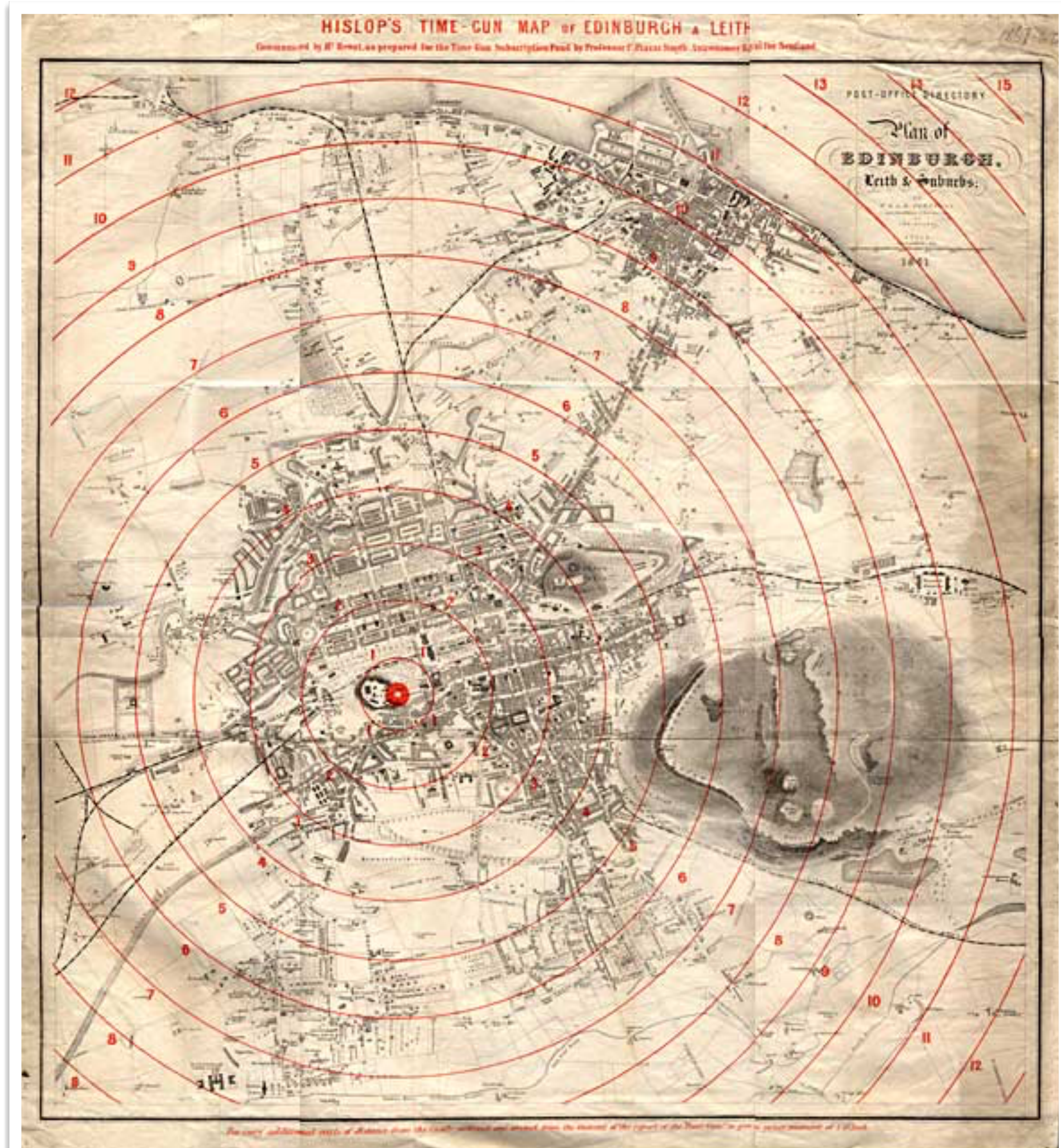
Telegraph Time Ball at the Strand, London, 1852.

Science Museum / Science & Society Picture Library

Time transfer



- ▶ One O'clock Gun
Edinburgh Castle



Centralized time reference

- ▶ Radio broadcast
 - **WWV** broadcasting from Fort Collins, CO



- ▶ Phone: Talking Clock

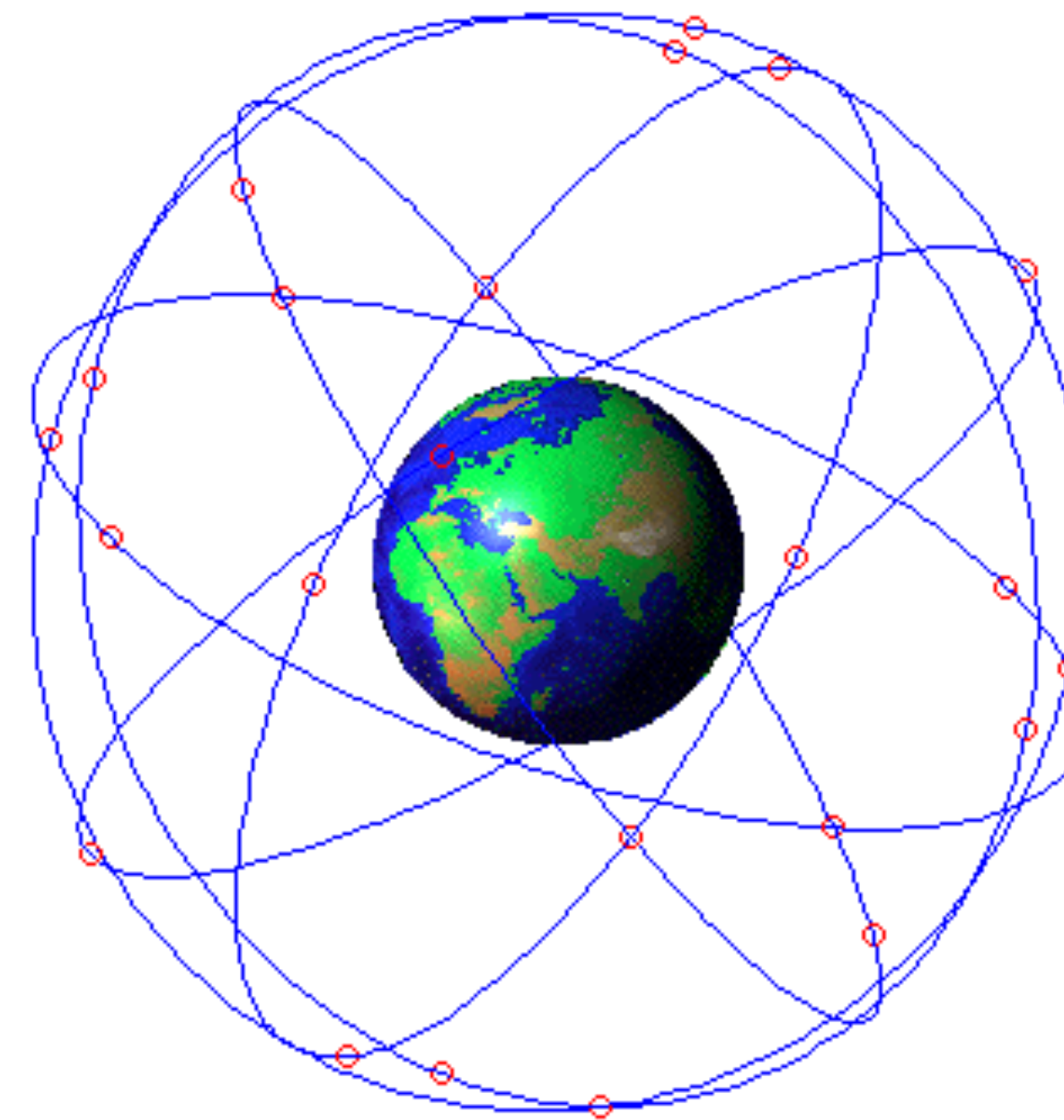


- ▶ Minute or second time signal from a reference time source

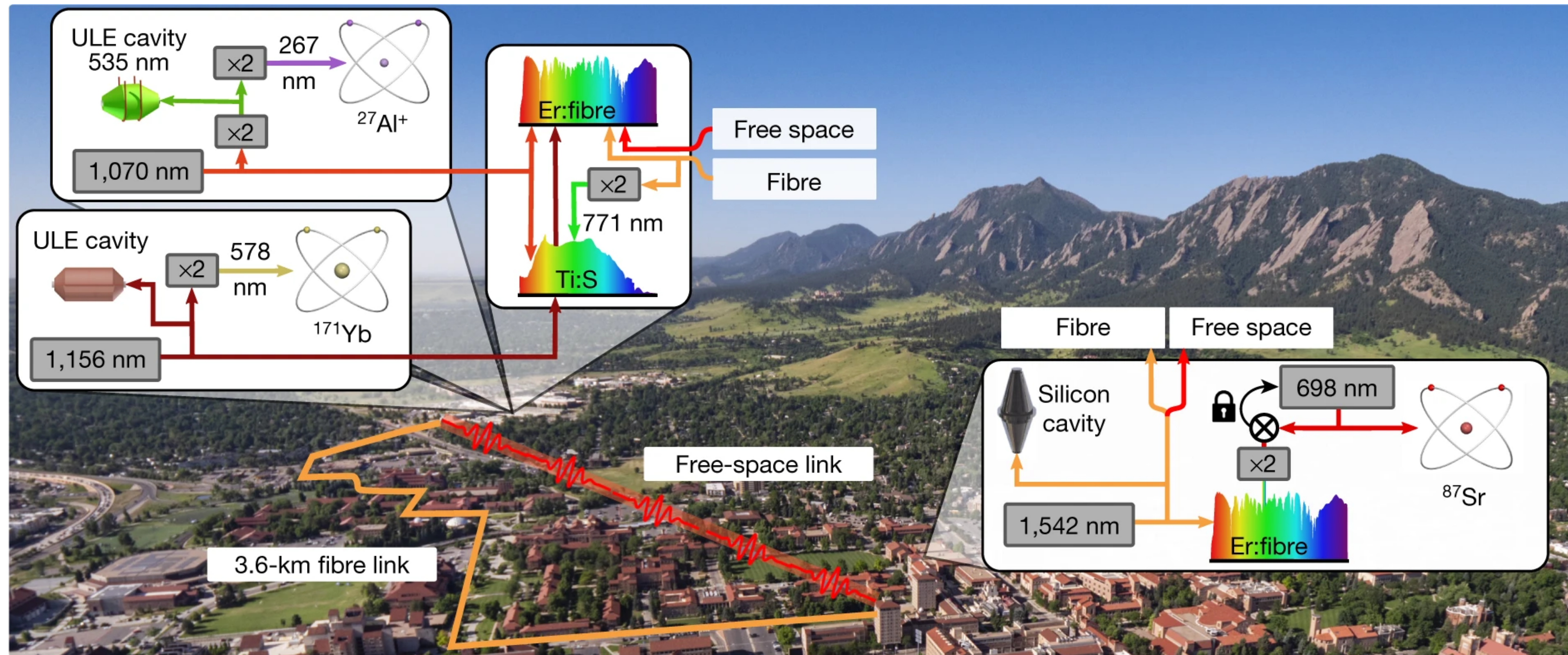


GNSS-based systems

- ▶ Multiple **satellites** with high-precision clocks on board at known precise locations send the timing information to terrestrial clients:
 - location
 - **precise time (!)**
- ▶ **Operational systems:**
 - GPS (USA)
 - Glonass (Russia)
 - BeiDou (China)
 - Galileo (European Union)
 - QZSS (Japan)



10^{-18} uncertainty...



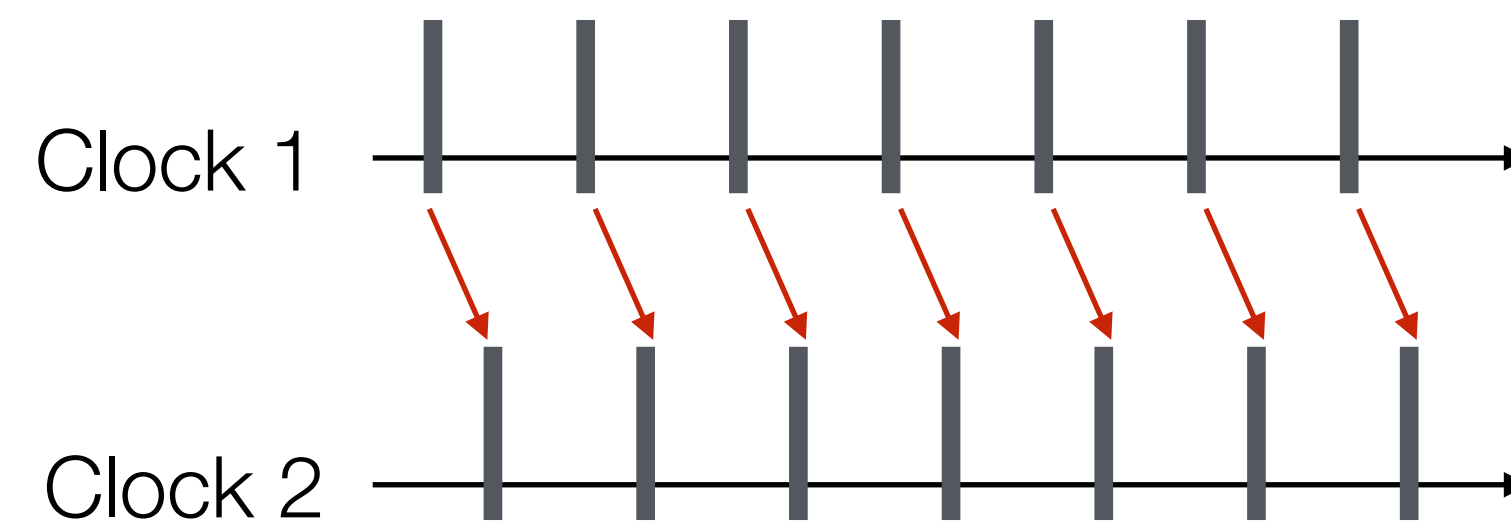
Source: Frequency ratio measurements at 18-digit accuracy using an optical clock network, Nature, March 2021, <https://doi.org/10.1038/s41586-021-03253-4>

Synchrony vs syntony

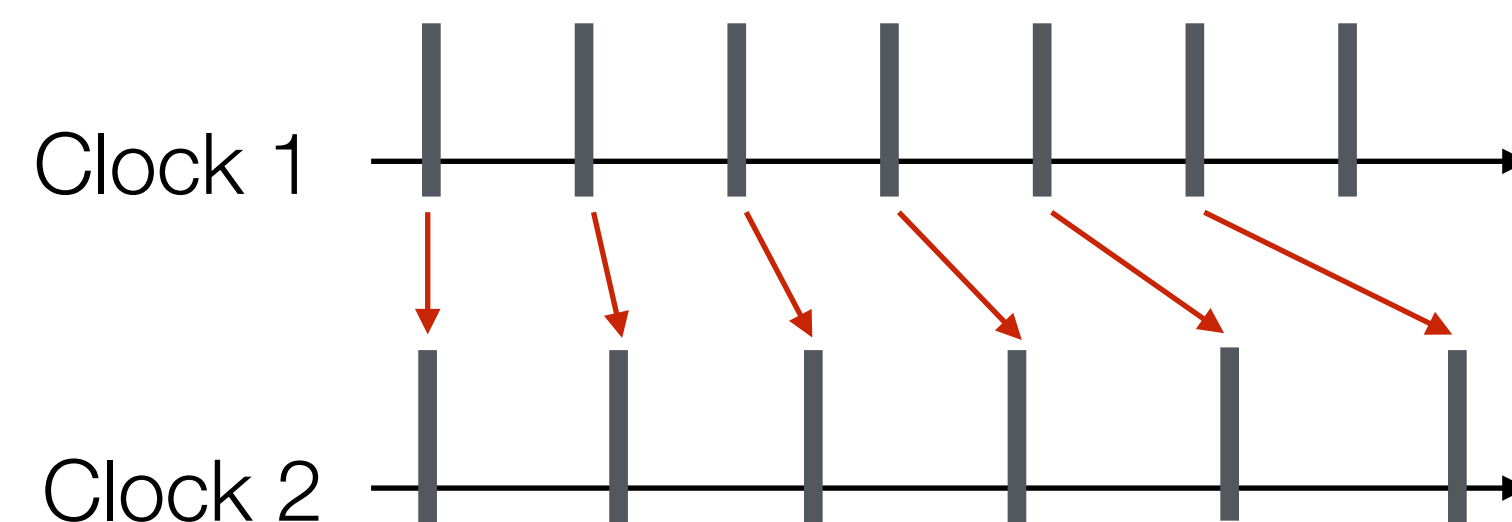
- ▶ Clocks are said to be **synchronized** (at a specific point in time) when they “show the same time”
 - synchrony = same time
- ▶ Clocks are said to be **syntonized** (over a period of time) when they “tick” at the same rate
 - syntony = same tone (frequency)
- ▶ We need solutions for synchronization and syntonization

Offset and Skew

- ▶ **Offset** - difference between the clock time and global (reference) time (a.k.a. **phase difference**)

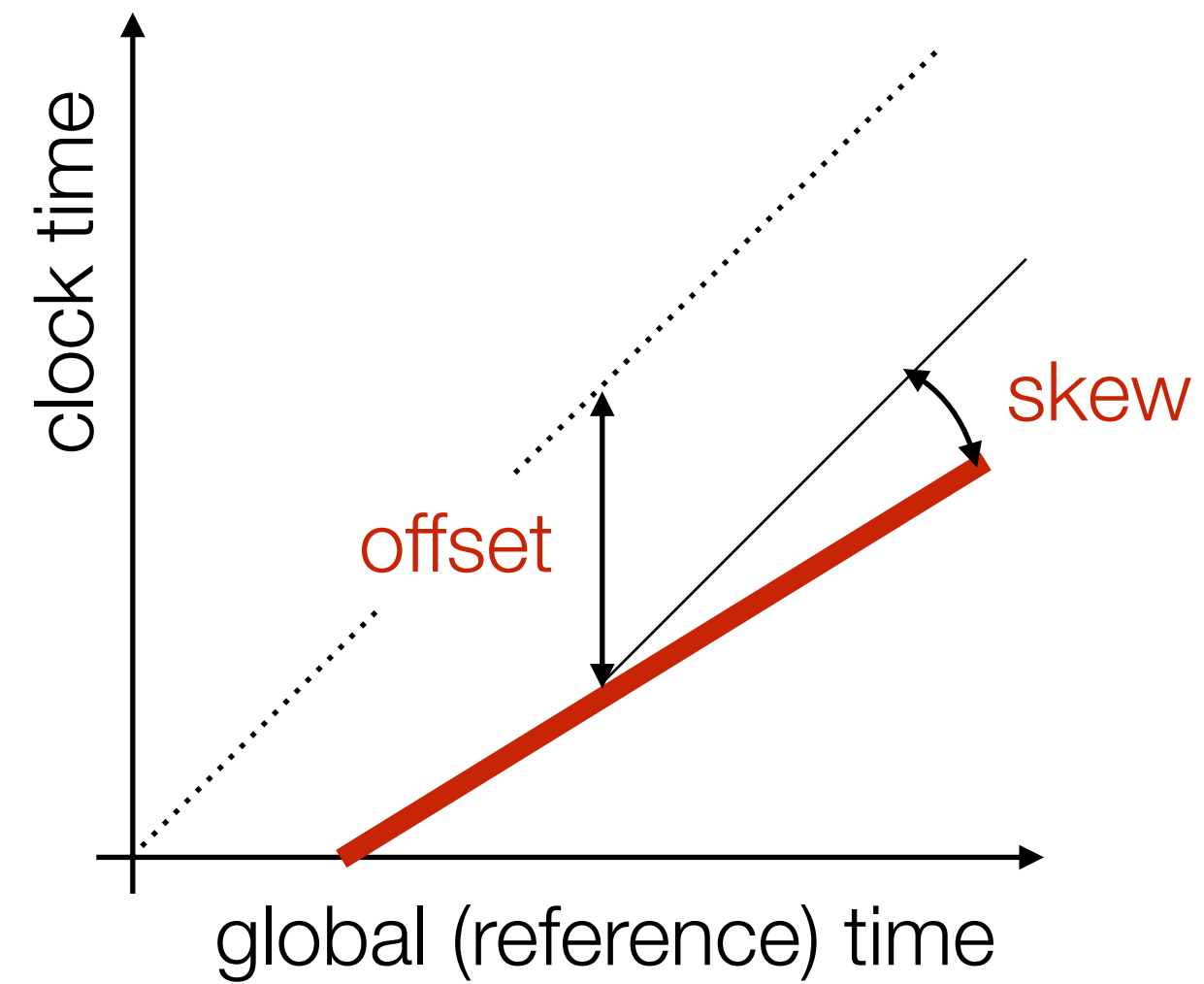


- ▶ **Skew** - the rate with which the clock drifts with respect to the global (reference) time (a.k.a. **frequency difference**)

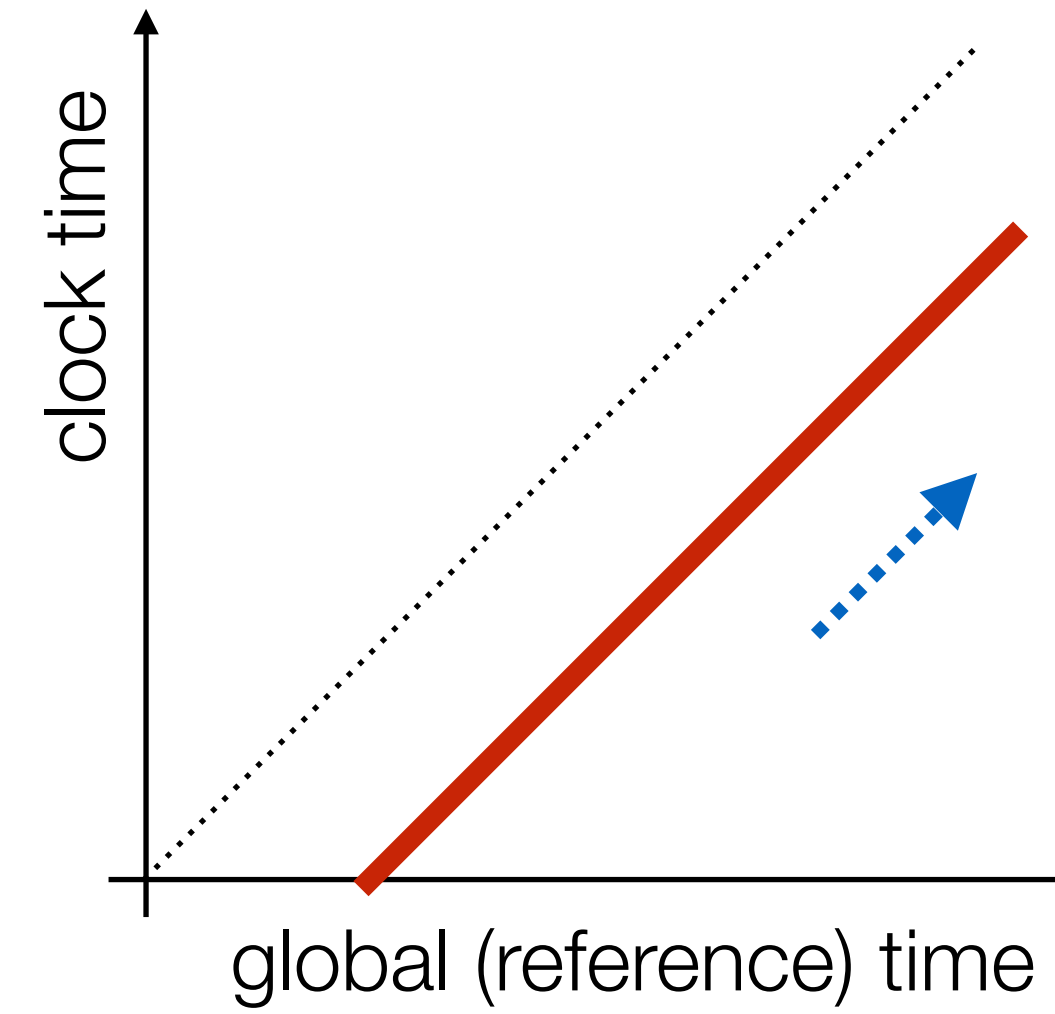


Offset and Skew

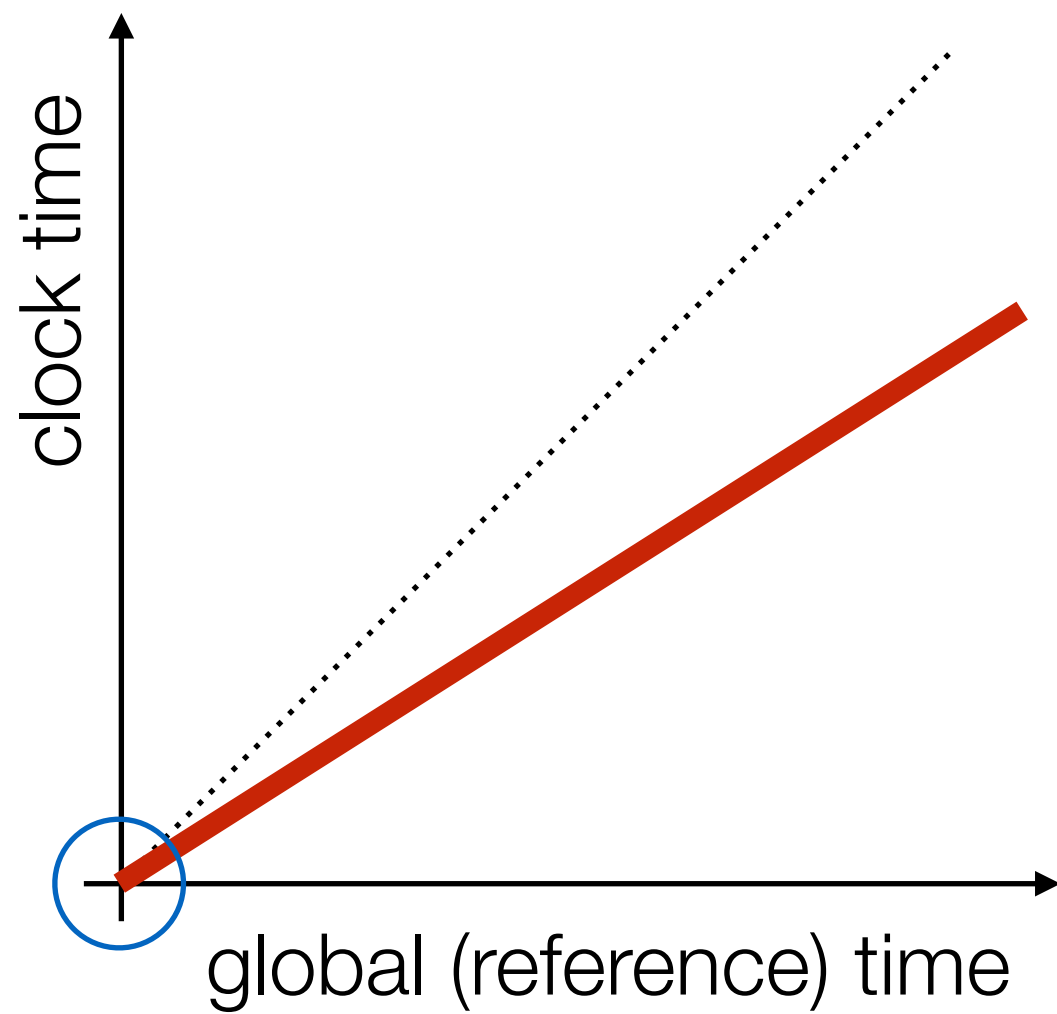
Clock with offset and skew



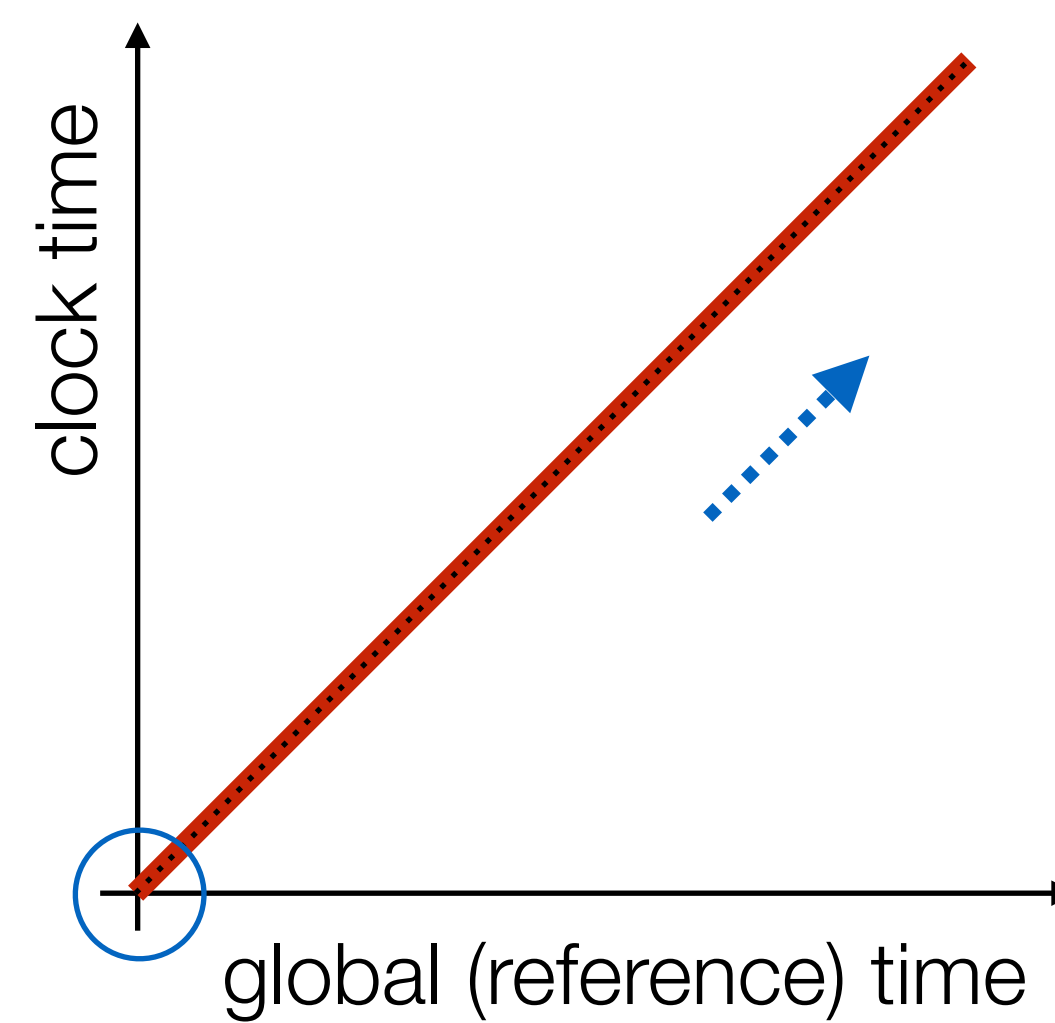
Clock with offset



Clock with skew



Perfect clock



Synchronized ○

Offset and Skew

- ▶ Ideally, knowing the the values for skew s and offset o (*and assuming the they are constant*), the clock time t_c can be converted to global (reference) time t_g :

$$t_g = t_c + (\Delta t \cdot s + o)$$

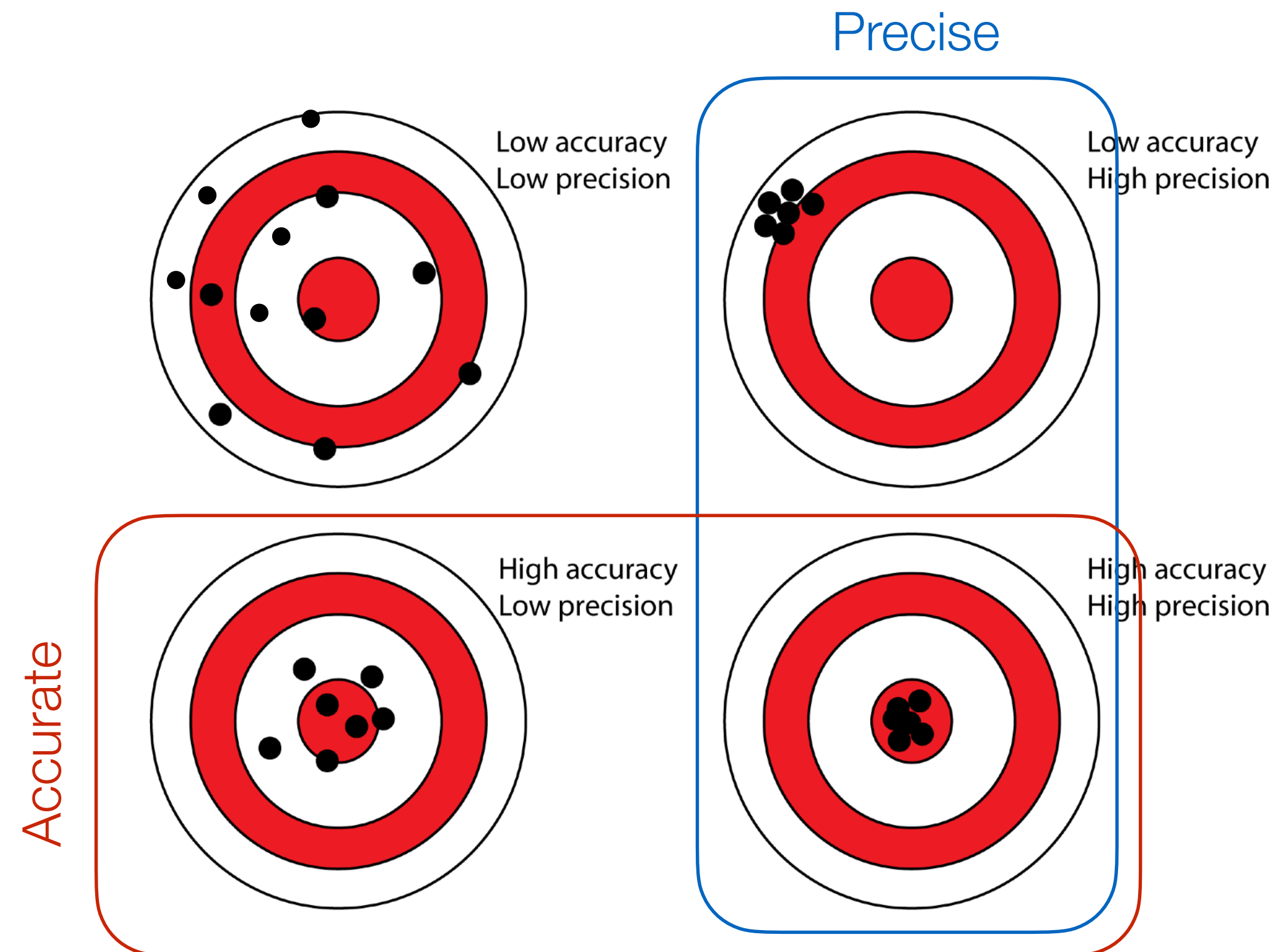
Precision and Accuracy

► Precision

- how well the clock tracks passing of time (over a period of time)

► Accuracy

- how well the clock reflect the global time (at an instant)



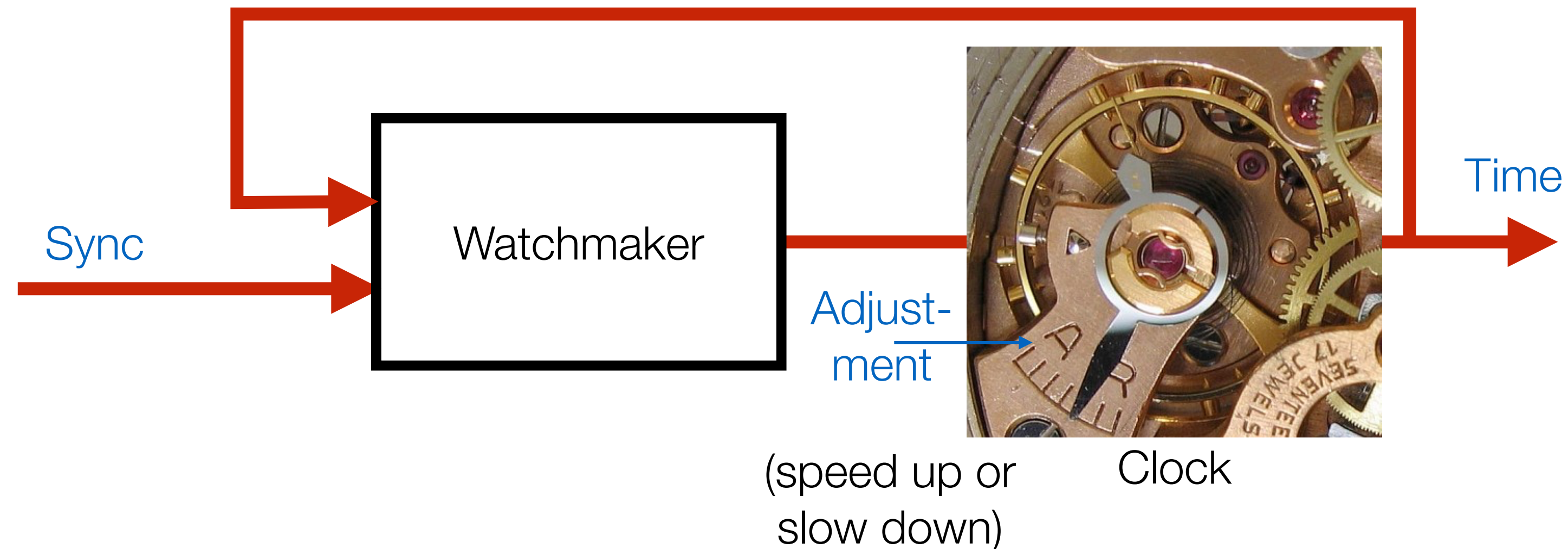
ALERT: Frequently used but highly misleading analogy

Maintaining local time

- ▶ Synchronize with a reference clock to find **offset**
 - adjust the clock time (how?)
- ▶ Do it periodically to find **skew**
 - adjust the clock

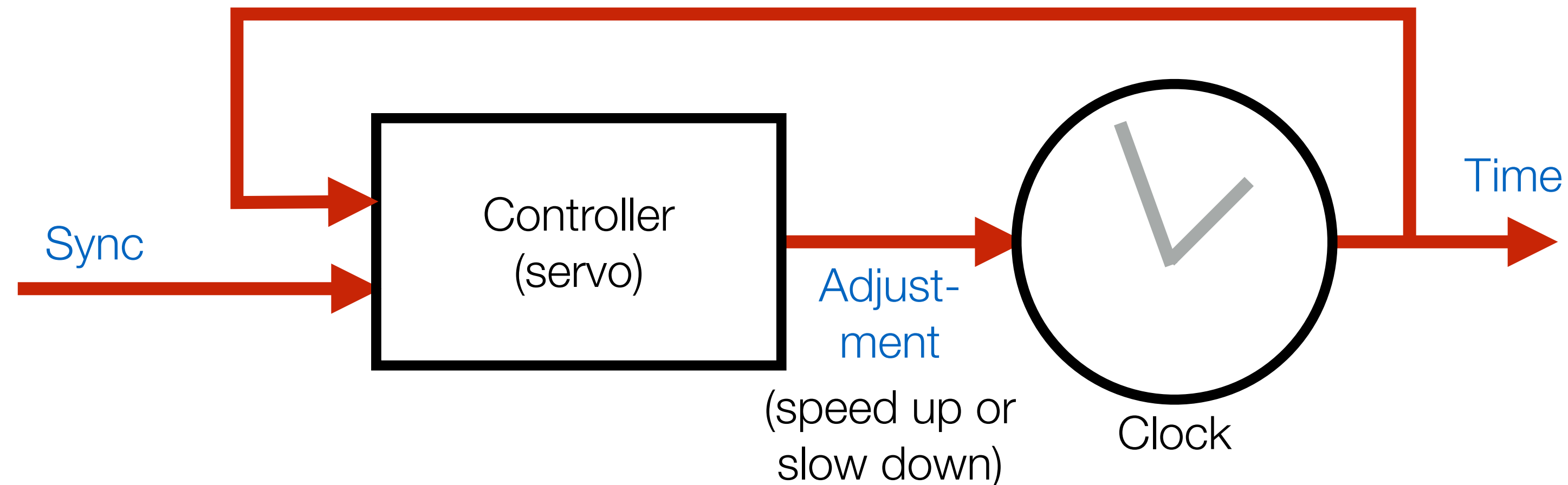
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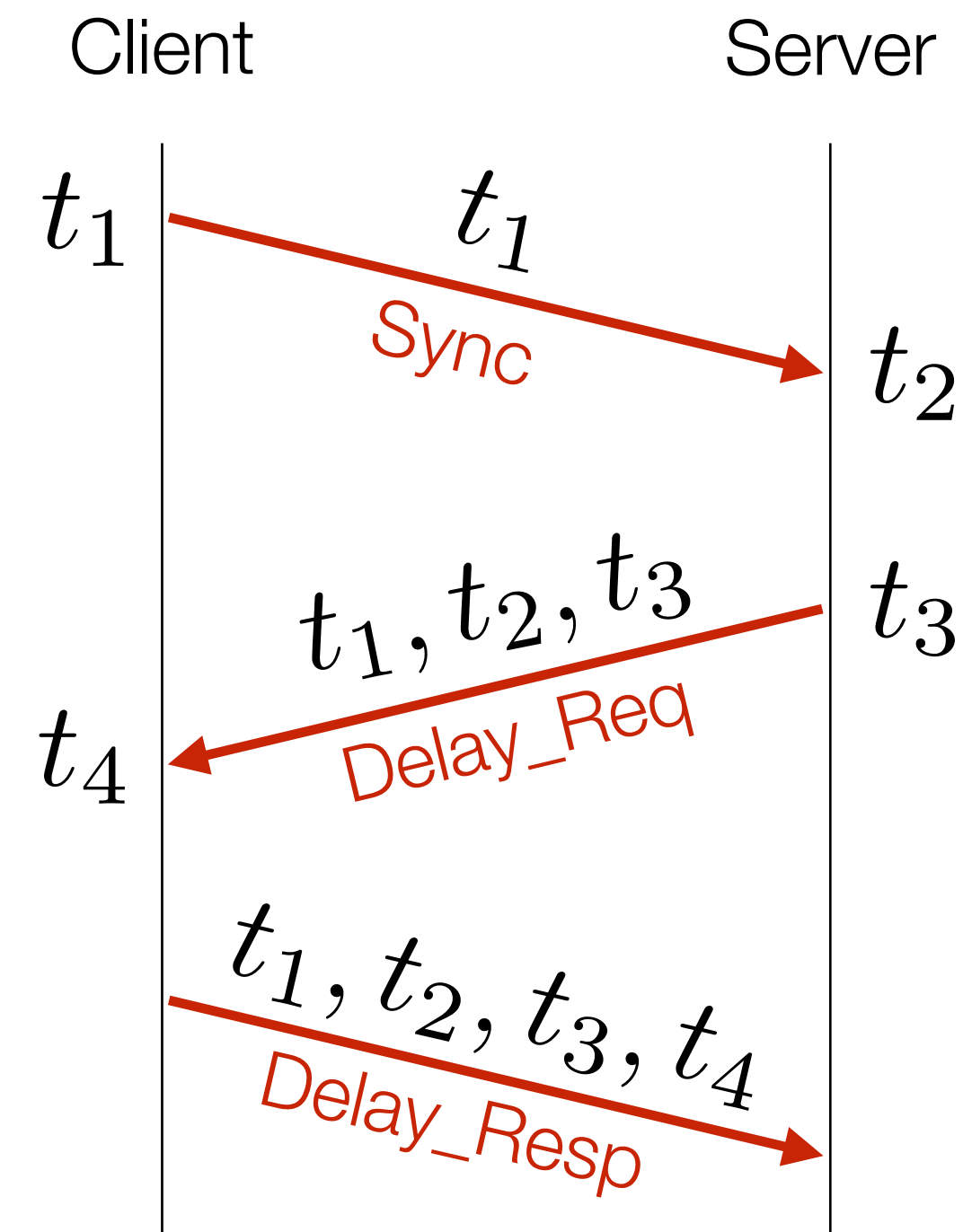


Time transfer

- ▶ Let's assume that I have the **most precise master clock** that money can buy and that the **clock is synchronized** to some form of universal time
- ▶ *You need precise time...
... so I write the current time on Post-it note and take it to you ...*
- ▶ The key issue is **time transfer** and the key challenge is the **latency of** the communication

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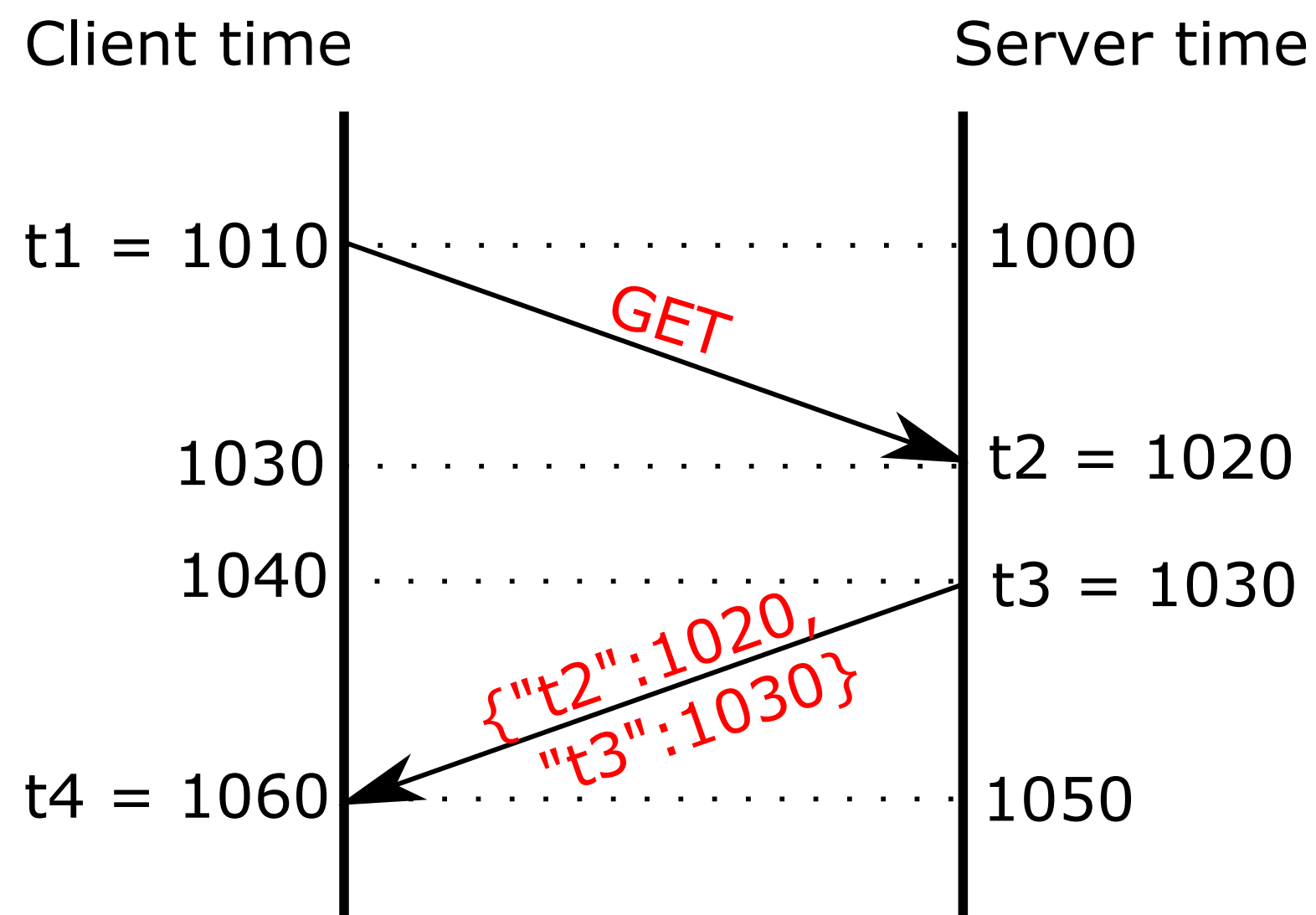
$$RTT = (t_4 - t_1) - (t_3 - t_2)$$

$$Offset = (t_2 - t_1) - \frac{RTT}{2}$$

Time transfer - example

$$RTT = (t_4 - t_1) - (t_3 - t_2)$$

$$Offset = (t_2 - t_1) - \frac{RTT}{2}$$



$$RTT = (1060 - 1010) - (1030 - 1020) = 40 \text{ units}$$

$$Offset = (1010 + 40/2) - 1020 = 10 \text{ units}$$

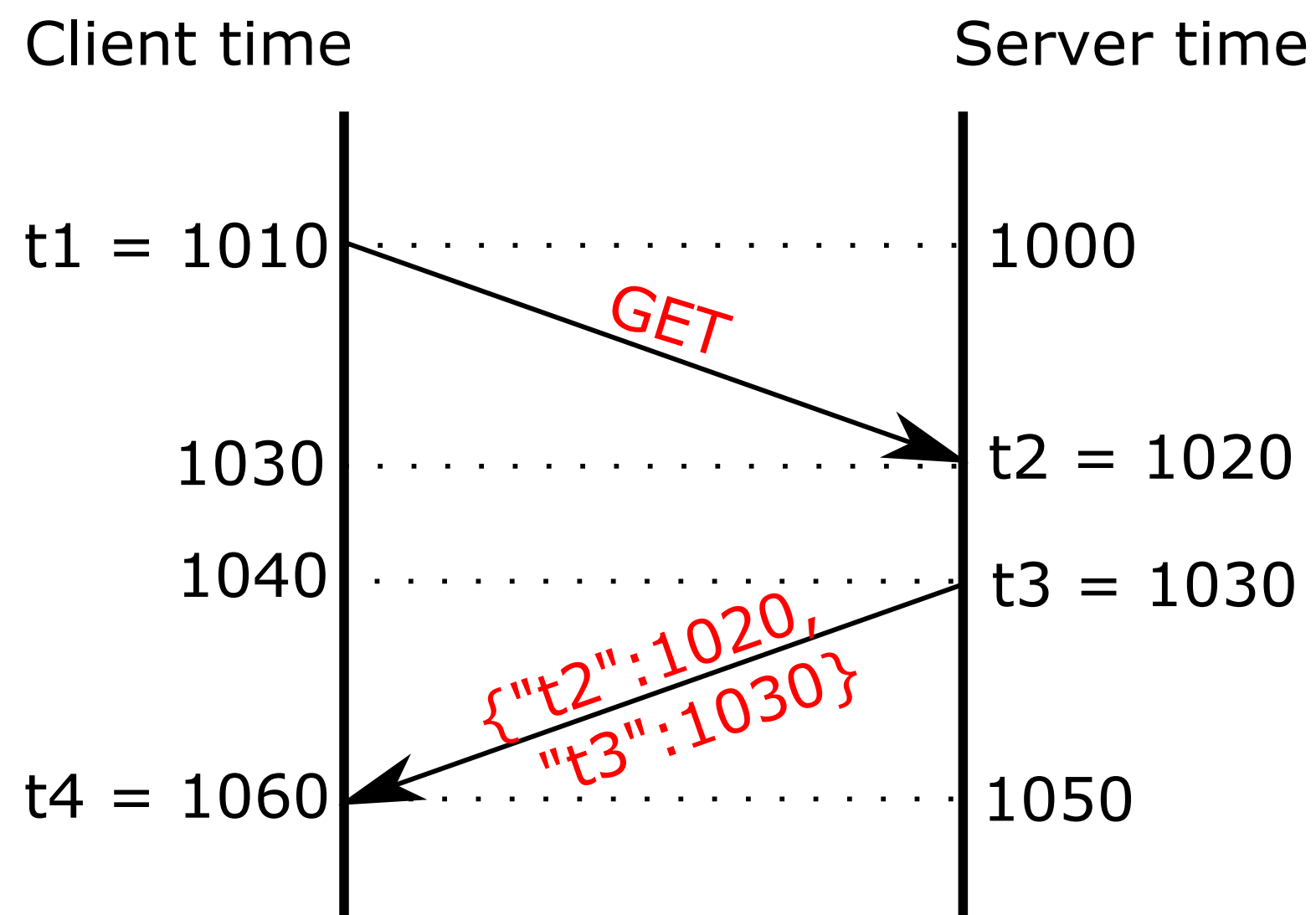
The client clock is 10 units ahead of the server clock

Time transfer - example

$$RTT = (t_4 - t_1) - (t_3 - t_2)$$

$$Offset = (t_2 - t_1) - \frac{RTT}{2}$$

Assumption!
Sometimes not true
in real systems



$$RTT = (1060 - 1010) - (1030 - 1020) = 40 \text{ units}$$

$$Offset = (1010 + 40/2) - 1020 = 10 \text{ units}$$

The client clock is 10 units ahead of the server clock