

**You are free to work together with other students, but you should turn in your own copy of your work. You can use a computer, but try to figure it out first.**

1. To convert a number to binary (base 2), divide by 2 repeatedly, keeping track of the remainder each time.

Example: what is 25 base 2?

$$25 \div 2 = 12 \text{ remainder } 1$$

$$12 \div 2 = 6 \text{ remainder } 0$$

$$6 \div 2 = 3 \text{ remainder } 0$$

$$3 \div 2 = 1 \text{ remainder } 1$$

$$1 \div 2 = 0 \text{ remainder } 1$$

Reading the digits from bottom to top, we get  $25_{10} = 11001_2$

That's what this python function does:

```
def int_to_bits(num):  
    bits = []  
    while num > 0:  
        bit = num % 2  
        num = num // 2  
    bits.reverse()  
    return bits
```

Convert these two numbers to binary:

a)  $12_{10} =$

b)  $30_{10} =$

2. To get the value of a binary number, multiply each bit by a power of 2, and add up.

Example: what is  $1101_2$ ?

$$1101_2 = 1 * 2^3 + 1 * 2^2 + 0 * 2^1 + 1 * 2^0 = 8 + 4 + 0 + 1 = 13_{10}$$

What is the decimal value of these two binary numbers?

a)  $1011_2 =$

b)  $11111_2 =$

3. Consider a cellular automaton that uses this rule to get the next generation:

3 bits above	000	001	010	011	100	101	110	111
decimal number	0	1	2	3	4	5	6	7
new value	1	0	0	1	0	0	0	1

Start with the generation of the automaton shown below.

a) For the first row, treat the three bits above as a binary number, and get its decimal value

b) Write the second generation. I filled in the leftmost and rightmost entries with 1.

c) Repeat for generations 3, 4, 5, and 6.

Gen. 1	0	1	1	0	1	0	0	0	1
decimal value	x								x
Gen. 2	1								1
Gen. 3	1								1
Gen. 4	1								1
Gen. 5	1								1
Gen. 6	1								1

4. What is printed by the following python code?

```
import copy
a = [10, 20, 30, 40, 50, 60]
b = a
c = copy.copy(a)
b[2] = 99
c[2] = 99
```

print a

---

print b

---

print c

---