Temporal Planning while the Clock Ticks

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Abstract

One of the original motivations for domain-independent planning was to generate plans that would then be executed in the environment. However, most existing planners ignore the passage of time during planning. While this can work well when absolute time does not play a role, this approach can lead to plans failing when there are external timing constraints, such as deadlines. In this paper, we describe a new approach for time-sensitive temporal planning. Our planner is aware of the fact that plan execution will start only once planning finishes, and incorporates this information into its decision making, in order to focus the search on branches that are more likely to lead to plans that will be feasible when the planner finishes.

Introduction

One of the original motivations for domain-independent planning was for controlling robots performing complex tasks (Fikes and Nilsson 1971). The typical approach to controlling robots using a planner is to call the planner to generate a plan which solves the problem, and then execute that plan in the environment. This approach works well if the plan remains applicable regardless of when it is executed. However, if there are external timing constraints, such as deadlines which must be met, things become more complex. This is because we must take into account the planning time.

For example, in the Robocup Logistics League (RCLL) challenge (Niemueller, Lakemeyer, and Ferrein 2015), a team of robots must move workpieces between different machines that perform some operations on them, and fulfill some order with a deadline. This calls for using temporal planning, because we would like all robots to work in parallel, and actions have different durations. The typical approach would have the planner come up with a plan which would work had it been executed at time 0, and then execute this plan when the planner completes. Obviously, this might lead to missing the deadline, and thus, plan failure.

One simple approach to handling this problem is to use some estimate on how long planning will take, and adapt all the deadlines assuming plan execution would start when the planner finishes. While using an upper bound on planning time will eliminate the problem of plans failing, it might lead to the planner not finding a feasible plan to begin with. On the other hand, using too low an estimate could still lead to plans failing, as discussed above.

In this paper, we describe a new approach for situated temporal planning. Our planner is aware of the fact that plan execution will start once planning finishes, and incorporates this information into the internal data structure for temporal reasoning used by the planner, together with estimates of remaining planning time. This helps our planner prune partial plans which are likely to lead to the planner finishing planning too late for the plans to be of use, and focus on more promising branches of the search.

Our empirical evaluation demonstrates that this planner can handle temporal planning problems with absolute deadlines much better than a naive baseline approach, in realistic settings where planning time counts, and the plan can only start executing once it is completed. To the best of our knowledge, this is the first temporal planner to explicitly consider planning time, within the context of planning and execution. Thus, our planner is especially applicable to online planning for robotics, where a robot must find a plan to execute, but the world does not stop while the robot is planning.

Preliminaries

We consider propositional temporal planning problems with Timed Initial Literals (TIL) (Cresswell and Coddington 2003; Edelkamp and Hoffmann 2004). Such a planning problem $\Pi$ is specified by a tuple $\Pi = (F, A, I, T, G)$, where:

- $F$ is a set of Boolean propositions, which describe the state of the world.
- $A$ is a set of durative actions. Each action $a \in A$ is described by:
  - Minimum duration $\text{dur}_{\text{min}}(a)$ and maximum duration $\text{dur}_{\text{max}}(a)$, both in $\mathbb{R}^{0+}$ with $\text{dur}_{\text{min}}(a) \leq \text{dur}_{\text{max}}(a)$.
  - Start condition $\text{cond}_{\text{start}}(a)$, invariant condition $\text{cond}_{\text{invariant}}(a)$, and end condition $\text{cond}_{\text{end}}(a)$, all of which are subsets of $F$, and
  - Start effect $\text{eff}_{\text{start}}(a)$ and end effect $\text{eff}_{\text{end}}(a)$, both of which specify which propositions in $F$ become true (add effects), and which become false (delete effects).
• \( I \subseteq F \) is the initial state, specifying exactly which propositions are true at time 0.

• \( T \) is a set of timed initial literals (TIL). Each TIL \( l \in T \) consists of a time \( \text{time}(l) \) and a literal \( \text{lit}(l) \), which specifies which proposition in \( F \) becomes true (or false) at time \( \text{time}(l) \).

• \( G \subseteq F \) specifies the goal, that is, which propositions we want to be true at the end of plan execution.

A solution to a temporal planning problem is a schedule \( \sigma \), which is a sequence of triples \((a, t, d)\), where \( a \in A \) is an action, \( t \in \mathbb{R}^{\mathbb{N}} \) is the time when action \( a \) is started, and \( d \in [\text{dur}_{\min}(a), \text{dur}_{\max}(a)] \) is the duration chosen for \( a \). A schedule can be seen as a set of instantaneous happenings (Fox and Long 2003), which occur when an action starts, when an action ends, and when a timed initial literal is triggered. Specifically, for each triple \((a, t, d)\) in the schedule, we have action \( a \) starting at time \( t \) (requiring \( \text{cond}_a(a) \) to hold a small amount of time \( \epsilon \) before time \( t \), and applying the effects \( \text{eff}_a(a) \) right at \( t \), and ending at time \( t + d \) (requiring \( \text{cond}_{\neg a}(a) \) to hold \( \epsilon \) before \( t + d \), and applying the effects \( \text{eff}_{\neg a}(a) \) at time \( t + d \)). For a TIL \( l \) we have the effect specified by \( \text{lit}(l) \) triggered at time \( \text{time}(l) \). Finally, in order for a schedule to be valid, we also require the invariant condition \( \text{cond}_{\neg a}(a) \) to hold over the open interval between \( t \) and \( t + d \), and that the goal \( G \) holds at the state which holds after all happenings have occurred.

### Related Work
Temporal planners have of course been used in on-line applications before. For example, researchers at PARC built a special-purpose temporal planner for on-line manufacturing (Ruml et al. 2011). As in many temporal planners, each search node contains a Simple Temporal Network (STN) (Dechter, Meiri, and Pearl 1991) to represent the time points of events in the plan and constraints on when they can occur. To reflect the fact that actions cannot occur until planning has completed, the PARC planner includes a hard-coded estimate of the required planning time, and every time point in the STN is constrained to occur at least that far after the time that planning started (Ruml et al. 2011, Figure 11). While this is a reasonable solution in a domain where the expected planning problems are all of similar difficulty, this approach can perform poorly in domains that include a wide variety of problems, as we will see below.

There has also been work on time-aware planning in the search community. Dionne, Thayer and Ruml (2011) present a so-called ‘contract algorithm’ called Deadline-Aware Search (DAS) that, given a deadline, attempts to return the cheapest complete plan that it can find within that deadline. The main part of the algorithm works by estimating the time that will be required to find a solution beneath each node in the open list, and pruning those for which this estimate exceeds the remaining search time. The estimate is the product of three quantities that are determined on-line: the time required to expand a node, expressed in seconds, an estimate on the number of search nodes remaining on the path to a goal beneath the given node, notated \( d(n) \), and the average number of expansions required before a generated node is selected for expansion, called the expansion delay. Although DAS was shown to surpass anytime algorithms on combinatorial benchmarks, its ideas have never been implemented in a domain-independent planner.

Bugsy (Burns, Ruml, and Do 2013) is a search algorithm that attempts to minimize the user’s utility, which is represented as a linear combination of planning time and plan cost. If plan cost is makespan, then the utility measures the ‘goal achievement time’, or the time from when the goal is presented to the planner, and planning starts, to when the plan finishes executing, and the goal is achieved by the agent. Bugsy is a best-first search algorithm, and relies on an estimate of remaining planning time similar to that of DAS in order to estimate the utility of each node it expands. While Bugsy is sensitive to its own planning time, it is not cognizant of external timed events such as deadlines, and does not prune nodes based on temporal information.

Related concepts in the search community include real-time search and anytime search. In the real-time search setting, the planner must return within a prespecified time bound the next action for the agent to take. This differs from our setting, in which the planner must return a complete plan and the temporal constraints are fine-grained and can relate individual domain propositions to absolute times. In anytime search, a planner quickly finds a complete plan, and then uses additional computation time to improve it until either it is terminated by an external signal or an optimal solution is found. In our setting, the planner may not run indefinitely, but rather is expected to minimize the agent’s goal achievement time. And while doing so, we demand that the planner recognize that time is passing and that it be responsive to timed events in the external world.

### Encoding Planning and Execution Time
Many temporal planners (e.g., (Coles et al. 2009; 2012; 2010; Benton, Coles, and Coles 2012; Fernández-González, Karpas, and Williams 2015; 2017)) rely on an internal Simple Temporal Network (STN) (Dechter, Meiri, and Pearl 1991) (or possibly a linear program or a convex optimization problem — but we will abuse terminology and call all of these the STN) to represent the temporal constraints between the set of the time points where actions start or end. Specifically, planners that support required concurrency (Cushing et al. 2007) tend to use this representation to support concurrent execution of actions.

When planning is done offline, the STN contains some time point \( t_{ES} \), which is the start of plan execution, and is assigned the value of 0. For convenience, we split each occurrence of action \( a \) in the plan into two snap-actions: \( a_{\text{start}} \) and \( a_{\text{end}} \), corresponding to the start and end of the action, respectively. For each of these we have a corresponding time point in the STN: \( t(a_{\text{start}}) \) when \( a \) starts, and \( t(a_{\text{end}}) \) when \( a \) ends. Actions which have started but not yet finished will only have the start time point, since this is a partial plan (as noted earlier, all starts eventually need to be paired with an end, but this is not a requirement of plans that are still under construction). Temporal constraints between the time points are either action \( \text{duration} \) constraints (between the time points of the same action occurrence), or \( \text{sequencing} \) constraints.
due to causal relations between actions. For example, if the end of action \( a \) achieves the start conditions of action \( b \), then we would have \( t(a) - t(b) \geq \epsilon \), where \( \epsilon \) is the minimum separation between two events that depend on each other (Fox and Long 2003). Or, if the start of \( c \) threatens the preconditions of \( d \), then \( t(c) - t(d) \geq \epsilon \). Additionally, timed initial literals (TIL) (Edelkamp and Hoffmann 2004) are encoded into the STN by adding a time point \( t(f) \) for the occurrence of TIL \( f \), with the temporal constraint \( t(f) - t_{ES} = \text{time}(f) \), where \( \text{time}(f) \) is the time at which \( f \) occurs, as specified in the problem definition. These are then ordered with respect to the other steps in the plan by, again, adding sequencing constraints due to the causal relations between \( \text{lit}(f) \) and the other steps in the plan.

In this paper, we focus on online planning. We want to account for the fact that time passes during the planning process, and that, in fact, planning time and execution time are both the same. In order to do so, we modify the STN described above by adding two additional time points: \( t_{PS} \) which is the time when planning started, and \( t_{now} \) which is the current time. We add the temporal constraint that \( t_{now} - t_{PS} \) equals the currently elapsed time in planning. The expression \( t_{ES} - t_{now} \) corresponds to the remaining planning time, which is, of course, unknown. We will discuss this expression, and how to treat it, in the next section. Now, \( t_{PS} = 0 \), while \( t_{ES} \) is unknown. Finally, because TILs describe absolute time, we must modify the temporal constraints corresponding to TILs to use \( t_{PS} \) instead of \( t_{ES} \), i.e., the temporal constraint for TIL \( l \) would be \( t(l) - t_{PS} = \text{time}(l) \), where \( \text{time}(l) \) is the time at which \( l \) must occur.

### Time-Aware Planning

We have described a technique for encoding an STN which captures the fact that execution only starts after planning ends, and planning takes time. We now describe the impact this has on search within a temporal planner.

#### Forward Planning Search Space

We take as our basis the forward-search approach of the planner OPTIC (Benton, Coles, and Coles 2012). Here, each search state comprises the plan \( \pi \) (of snap actions) that reaches that state; the propositions \( p \subseteq F \) that hold after \( \pi \) was executed from the initial state; and the Simple Temporal Network \( STN(\pi) \) encoding the temporal constraints over \( \pi \).

When expanding a state in OPTIC, successors were generated in one of three ways:

- **By applying a start snap-action that is logically applicable:** any \( a_{ \pi } \) where \( p \not\models \text{cond}_{ \pi } (a_{ \pi }) \); \( \text{eff}_{ \pi } (a_{ \pi }) \) would not break the invariant condition of an action that has started in \( \pi \) but not yet ended; and \( \text{cond}_{ \pi } \) would be satisfied once \( a_{ \pi } \) has been applied. In this case, in the successor state, \( \pi' = \pi + [a_{ \pi }] \), \( p \) is updated according to \( \text{eff}_{ \pi } (a_{ \pi }) \) to yield \( p' \), and a variable \( t(a_{ \pi }) \) added to \( STN(\pi') \). Sequence constraints are imposed on this such that it follows any step in \( \pi \) that met one of \( \text{cond}_{ \pi } (a_{ \pi }) \); or whose effects refer to the same propositions as \( \text{eff}_{ \pi } (a_{ \pi }) \); or whose preconditions (including invariant conditions) would be threatened by \( \text{eff}_{ \pi } (a_{ \pi }) \).

- **By applying an end snap-action that is logically applicable:** any \( a_{ \pi } \) where \( a_{ \pi } \) has started in \( \pi \) but not yet ended; \( p \models \text{cond}_{ \pi } (a_{ \pi }) \); and whose effects \( \text{eff}_{ \pi } (a_{ \pi }) \) would not break the invariant of any other action that has started in \( \pi \) but not yet ended. In this case, the successor state is updated in a way analogous to starting an action, with the additional STN constraint \( \text{dur}_{ \min } (a_{ \pi }) \leq t(a_{ \pi }) - t(a_{ \pi }) \leq \text{dur}_{ \max } (a_{ \pi }) \).

- **By applying a Timed Initial Literal \( l \) that has not already occurred in \( \pi \).** In this case, \( \pi' = \pi + [l] \), \( p \) is updated according to \( \text{lit}(l) \) to yield \( p' \), and a variable \( t(l) \) is added to \( STN(\pi') \). For the purposes of sequence constraints, this can be thought of as being a snap-action with no preconditions – it suffices to order it after steps in \( \pi \) whose preconditions or effects refer to \( \text{lit}(l) \). To fix the time at which \( l \) occurs, an additional STN constraint is added: \( t(l) - t_{PS} = \text{time}(l) \); while snap-actions are ordered only relative to other points in the plan, TILs must also occur a specific amount of time after time zero.

State expansion in this way generates candidate successors that are logically feasible; to ensure they are also temporally feasible, only those whose STNs are consistent are kept. Using an all-pairs shortest path algorithm in the STN will both check consistency (with negative cycles corresponding to an inconsistent STN), and give us the earliest and latest possible time at which each snap-action could be applied. We denote these \( t_{\min } (x) \) and \( t_{\max } (x) \) for each STN variable \( t(x) \). Typically, only the former of these is used – to map \( \pi \) to a schedule \( \sigma \), each start–end snap-action pair \( a_{ \pi } \), \( a_{ \pi } \) gives a triple \( (a_{ \pi }, t_{\min } (a_{ \pi }), t_{\min } (a_{ \pi }) - t_{\min } (a_{ \pi })) \).

In other words, apply each action as soon as possible, with the shortest possible duration, thereby minimizing execution time.

Extending this approach to planning while aware of planning and execution time requires a number of modifications, which we now step through.

### No action can start before plan execution starts

Because execution cannot start until a plan has been produced. That is, for each \( a_{ \pi } \) in the plan \( \pi \), we add a constraint \( t_{ES} \leq t(a_{ \pi }) \) to the STN, where \( t_{ES} \) is the time at which execution will start. We do not know this \textit{a priori}, but can at least say \( t_{now} \leq t_{ES} \) is the time since the planner started executing. An STN for a plan produced during successor generation will then be consistent \textit{iff} it is not already too late to start executing the plan.

These additional constraints can be thought of as pushing the earliest actions in the plan to start after now; the effects of which are then propagated through the STN to appropriately delay the later actions, according to the sequence and duration constraints. If an otherwise-consistent STN is made inconsistent by these, then necessarily there must be a snap-
action \( x \) where \( t_{\text{max}}(x) < t_{\text{now}} \) – i.e. we are past the latest point at which \( x \) could have been applied.

Planning time particularly matters in the presence of TILs – in the absence of these, we can start executing a plan whenever we like by simply delaying the start of the first action. If TILs are present, though, these anchor the plan to having to fit around absolute time: with reference to state expansion, when a TIL is added to the plan, this fixes it to come after any earlier steps with which it would interfere, thereby constraining their maximum time.

Automatically applying past TILs – if we are now past the time at which a TIL has occurred, it is added to \( \pi \) before expanding the state.

More formally, immediately before expanding a state \( S = (\pi, p, STN(\pi)) \), the following TILs are applied:

\[
\{ l \in T \mid t(\text{now}) \geq \text{time}(l) \land l \notin \pi \}
\]

If there are several such TILs, they are applied in ascending order of \( \text{time}(l) \). The mechanism for applying these TILs is identical to that in OPTIC: each is applied, to yield a successor state \( S' \); and then \( S' \) replaces \( S \). By doing this before expanding the state, we account for time having passed since \( S \) having been placed on the open list, and it being expanded – if in this time a TIL will have happened, \( S \) is updated accordingly, before expansion.

If this modification was not made, search would be free to branch over what step should next be added to \( \pi \). In the case where a TIL \( l \) represents a deadline – by deleting a precondition on actions that must occur by a given time – search would be free to apply these actions, even though in reality it is too late. By forcing the application of past TILs, we avoid this behavior: all such actions would then become inapplicable.

Pruning states where it is too late to start their plan

From the STN for a plan \( \pi \), we can note the latest point at which that plan can start executing; and prune any states for which this time has already passed.

As noted earlier, to check if the STN for a state is consistent, we use an all-pairs shortest path algorithm. This incidentally yields the minimum and maximum time-stamps for each snap-action. For snap-actions that are ordered before a TIL – which are fixed in time – these maximum time-stamps are finite. Moreover, because the plan is expanded in a strictly forward direction, the maximum time-stamps are monotonically decreasing: it is not possible to somehow order a new action before a plan step, in a way that reduces its maximum time-stamp. Thus, for each state \( S = (\pi, p, STN(\pi)) \) we identify the start snap-action in \( \pi \) that has the earliest possible maximum time-stamp – this is the latest time at which \( \pi \) could feasibly be executed:

\[
\text{latest}\_\text{start}(\pi) = \min\{ t_{\text{max}}(a) \mid a \in \pi \}
\]

Then, when \( S \) is about to be expanded – after it was generated, placed on the open list, and then removed – it is pruned if \( t_{\text{now}} > \text{latest}\_\text{start}(\pi) \).

Estimating Search Time

Having discussed our search space, we now turn our attention to how to efficiently search within it.

Estimating Search Time with Expansion Delay

The first approach we propose relies on estimating the remaining search time. This could be done by using solution length estimates (Thayer and Ruml 2011; Thayer et al. 2012). For example, the length of a relaxed plan could be used as such an estimate (Coles et al. 2010), while another heuristic could be used to estimate plan cost (Coles et al. 2011). Furthermore, our estimates of solution length could be adjusted on-line (Thayer, Dionne, and Ruml 2011).

Perhaps the most relevant to our needs here is the deadline-aware search methodology of Dionne, Thayer and Ruml (2011). This estimates the time taken to reach the goal state from a given search state \( s \) by using:

- The average expansion delay, \( \Delta e \). By indexing expansions as search proceeds, one can record \( e(s) \) as the expansion number that generated \( s \). When \( s \) is later expanded one can take the current expansion number \( e_{\text{curr}} \) and compute \( \Delta e = (e_{\text{curr}} - e(s)) \) – the number of expansions that occurred between the generation, and expansion, of \( s \). The global value of \( \Delta e \) is then a sliding-window average over recent values of \( \Delta e(s) \).
- The expansion rate \( r \): how many ‘expansions per second’ are being performed by search. This is computed using a sliding window over the recent expansions in search.
- The heuristic distance-to-go from \( d(s) \) to the goal state, for which we use the number of actions in a temporal relaxed plan (Coles et al. 2010).

These can be combined to give an estimate of the remaining search time from \( s \) to the goal:

\[
R_e(s) = (\Delta e \times d(s))/r
\]

To use these within search, we turn to the \( \text{latest}\_\text{start}(\pi) \) value recorded for each \( \pi \) in each node of the search space. Simply, for a state \( s = (\pi, p, STN(\pi)) \), if \( t_{\text{now}} + R_e(s) > \text{latest}\_\text{start}(\pi) \), then our estimated remaining search time indicates that by the time search has reached the goal from \( s \), it will be too late for \( \pi \) to be a feasible plan. Note that this amends the criterion originally put forwards by Dionne, Thayer and Ruml (2011) – we move away from a single global deadline on the time by which search must complete, to a state-dependent deadline depending on the actions in \( \pi \).

Exploiting Information from the Heuristic

The approach presented above takes into account the \( \text{length} \) of a relaxed plan, in terms of number of actions, but ignores the \( \text{contents} \) of the relaxed plan. However, the \( \text{contents} \) of the relaxed plan might provide valuable information about which actions or TILs are going to be used in the future, which would provide us with much more accurate information about how much planning time we actually have.

For example, suppose the partial plan \( \pi \) in the current search node does not itself have any steps on which there are deadlines (due to preconditions on TILs); and hence \( \text{latest}\_\text{start}(\pi) = \infty \). In this case, we would be optimistic and assume that regardless of \( t_{\text{now}} \), the current plan is good: there is no deadline on beginning plan execution. However, if our relaxed plan comprises actions that have TIL preconditions that correspond to tight deadlines, then it is very likely
that the current node will not lead to completing planning on time: while the actions in the relaxed plan are not landmarks (Karpass et al. 2015) they are indicative of what steps might be needed to reach the goals. Thus, we propose a second, estimated measure latest start time, taken from the temporal relaxed plan built for the heuristic.

A temporal relaxed plan that extends $\pi$ to one that reaches the goal (under the delete relaxation) can be defined as a sequence of time-stamped snap-actions $\text{rp}(\pi) = [(t_0, a_0), \ldots, (t_n, a_n)]$. In terms of the structure of the RPG, $t_i$ is the timestamp of the layer at which $a_i$ appeared. This is an admissible estimate of the earliest time at which $a_i$ could be applied, following the relaxed reachability forwards from $\pi$. As we are working with a temporal RPG, if we are evaluating a state $s = (\pi, p, \text{STN}(\pi))$, each the facts $p$ does not appear at layer 0. Rather, each fact $f \in p$ is delayed until RPG layer $t_{\min}(f+)$, where $f+$ is the step in $\pi$ that most recently added $f$. When the RPG is expanded, this then delays snap-actions to a timestamped layer by which their preconditions are at least relaxed-reachable.

For the earlier definition of $\text{latest}_\text{start}(\pi)$ we relied on having a simple temporal network $\text{STN}(\pi)$ to give us the upper-bound $t_{\max}$ on applying each plan step. We do not have an STN for the relaxed plan, but can — using static analysis — find the global latest possible time $t_{\max}(a_i)$ at which a snap action $a_i$ could be applied, due to deadlines imposed by TILs (Tierney et al. 2012). This allows us to compute the slack of the relaxed plan — the amount by which the actions in the relaxed plan can be delayed, such that no snap-action occurs after its global latest time:

$$\text{slack}(\text{rp}(\pi)) = \min[t_{\max}(a_i) - t_i \ | \ (t_i, a_i) \in \text{rp}]$$

The latest possible start time for a relaxed plan is then:

$$\text{latest}_\text{rp}_\text{start}(\text{rp}(\pi)) = t_{\text{now}} + \text{slack}(\text{rp}(\pi))$$

For a plan $\pi$, we can then compute an estimate of its latest start time, considering its relaxed plan, as:

$$\text{estimated}_\text{latest}_\text{start}(\pi) = \max\{\text{latest}_\text{start}(\pi), \text{latest}_\text{rp}_\text{start}(\text{rp}(\pi))\}$$

### Accounting for Inadmissible Heuristics
As we are using a relaxed planning graph heuristic that is neither admissible nor consistent, then compared to the original scenarios of Dionne, Thayer and Ruml (2011), we can be comparatively less confident in the accuracy of $R_t(s)$. If it overestimates remaining search time, then using $t_{\text{now}} + R_t(s) > \text{latest}_\text{start}(\pi)$ as a strict criterion for pruning a state $s$ risks pruning states from which the goal was reachable in an acceptable amount of time. Further, the actions that appear in pruning states from which the goal was reachable in an acceptable amount of time. Thus, we turn to an established approach for overcoming the weaknesses of domain-independent heuristics in planning: dual open-list search (Richter and Helmert 2009). Our search alternates between two open lists:

**OnTime:** states reached by a plan $\pi$ where $t_{\text{now}} + R_t(s)$ is less than some latest start time: either $\text{latest}_\text{start}(\pi)$, or $\text{estimated}_\text{latest}_\text{start}(\pi)$. (These can be thought of as states reached by a preferred operator.)

**All:** all states (both on time and “late”) are considered.

When a state $s$ is generated, it is placed onto the appropriate open lists, given these criteria. Each of these open lists is sorted by heuristic distance-to-go, $d(s)$. Search then alternates between these two open-lists.

Compared to a single open-list without pruning, this ensures that at least half of the search effort is spent expanding nodes from which we estimate the goal would be reached in time. Compared to a single open-list with strict pruning, we mitigate against the tendency for the heuristic to incorrectly over-estimate $R_t(s)$ in a way that excludes states that should have been kept; and for the case when $\text{estimated}_\text{latest}_\text{start}$ is used, where latest start time due to the relaxed plan is pessimistic.

### Experiments

To gain a concrete sense of the practical import of our technique, we experimentally compared it to the baseline method of prespecified planning times. We performed experiments in two types of domains: the Robocup Logistics League (RCLL) domain, and a set of IPC domains containing TILs. As a baseline against which to compare our planner, we used OPTIC with a fixed planning time of $T$ seconds. Time windows were considered to be $T$ seconds earlier, to adjust the initial state to the start of execution time. Therefore, a TIL $l$ occurring at time $\text{time}(l)$ seconds, using a planning time of $T$ seconds, will occur at time $(\text{time}(l) - T)$ (at least 0) in the plan. We compared our approach to this baseline with multiple values for $T$.

As planning time and execution time are one and the same here, we use goal-achievement-time (GAT) — the sum of planning time and plan makespan — to measure the performance of our planners. We also used the standard measures of IPC quality score, number of solved instances, and mean planning time. Tables 1, 2, 3 present these results, where the GAT and planning time are averaged over all instances in the group that were solved by all planners, and thus the numbers might appear low. If no such instances exist in a particular group then these rows are omitted.

All our planners used the same limits of 200s of CPU time and 4GB of memory, and are abbreviated as follows:

- **Time Aware (TA):** using a single open list, only pruning nodes which are definitely too late to start without estimating remaining planning time
- **Time Predictive (TP):** using estimated search time with a dual-open list based on $\text{latest}_\text{start}(\pi)$
- **Time Predictive+ (TP+):** as TP, but instead using $\text{estimated}_\text{latest}_\text{start}(\pi)$
- **OPTIC x ($O_x$):** subscripted with the fixed planning time $x$. 

We remark that all of these planners returned the first solution they found, which was used to compute IPC quality. Note that once the first plan is found, it is possible to compute how much longer the planner can spend on trying to improve this plan, until it must be started, and spend this time safely searching for a better plan. We will explore this possibility in future work.

**Robocup Logistics League**

We evaluated our planner on 300 instances of the robocup logistics league PDDL description (Niemueller et al. 2016), generated by a random problem generator (Schaepers et al. 2018). 100 random configurations of the playing field (machine locations) and orders were generated. For each of those, we have 3 problems instances: with 1, 2, and 3 robots available. Each instance has a single order which must be fulfilled.

We modified the domain to add a soft fulfillment deadline for each order. More specifically, we have two versions of the fulfill order action: one which must fulfill the order within the specified deadline and takes 0.01 time units, and one which does not have to respect the deadline, but has a duration of 1000 as a penalty.

Furthermore, the planner must commit to ontime delivery much more quickly — within the commitment deadline. Otherwise, it can only use the late fulfillment action (and incur the penalty) even if the order is fulfilled on time. The commitment deadline forces the planner to make an early choice about whether it should try to plan for ontime delivery or not.

In order to set reasonable times for the deadlines, we ran the OPTIC planner on our problem instances, and recorded both planning time and makespan. For each problem, we set the fulfillment deadline to planning time + makespan + 10 seconds, and the commitment deadline to planning time + 5 seconds. For problems that were not solved within 200 second (about half of them), we used the average values for planning time and makespan to set the deadlines.

Our modifications to the problem ensure that all instances solvable by choosing the late fulfillment option. However, although as the results in Table 1 show, our time-aware planners do a much better job exploiting this than the baseline planners. We remark that as there was no instance that was solved by all 6 planners, we omit the mean planning time and GAT.

**IPC Domains**

In our IPC experiments, we tested all IPC-4 and IPC-5 domains that contain TILs: airport, pipesworld, satellite, truck, and UMTS. The UMTS domains and half of the airport instances were omitted as none of the planners completed these under our limits of 200s of CPU time and 4GB of memory.

Table 2 presents results on the IPC domains. The fixed planning time planners were outperformed by the time-aware methods in every domain. Several instances were unsolvable by the former due to the fixed planning time constraints. Table 3 shows the detailed performance in each relevant domain tested.

In addition to the fixed planning times that are showed in Table 2 and Table 3 we have tested 50s, 100s, and 200s. The performance of the baseline approach with these planning

![Table 1: Robocup Logistic League Results](image)

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Table 2: Aggregate results for IPC Benchmarks

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times was worse than the time-aware method and the best presented baseline, thus these results were omitted.

Conclusions and Future Work

We have presented a domain-independent temporal planner that takes the interaction between the time spent on planning and execution time into consideration. We have demonstrated empirically that this planner achieves much better results in domains with absolute deadlines than our baseline approach. However, our work is merely the first step in addressing this important topic. There remain many exciting avenues for future work.

For example, using the actual contents of the relaxed plan to predict remaining planning time is not always helpful, as the empirical evaluation shows. This is likely because the heuristic is not admissible, and might cause promising states not to be put on the OnTime open list. In order to get an admissible estimate which takes future actions and TILs into account, we intend to explore using temporal landmarks (Karpas et al. 2015). These landmarks could be encoded into the same STN of the partial plan, and thus we believe we will be able to achieve even better hard pruning of branches of the search tree which will not lead to a solution in time.

More broadly, the problem we are addressing here could benefit from more explicit metarereasoning (Russell and Wefald 1991). For example, suppose we had a planning problem with two possible solutions, each of which must be explored on a separate branch of the search tree. Further suppose that each of these solutions has a deadline which leaves just enough time to explore one of the branches, but not both of them. Clearly, a planner with perfect knowledge would choose one of these branches and explore it. On the other hand, the approach we present here will explore both branches until it realizes there is not enough time left, and will then prune both branches — without solving the problem. In future work, we will explore ways of addressing this type of problem by incorporating explicit metarereasoning on planning time allocation into the search strategy, based on similar ideas to those of Rational Lazy $A^*$ (Karpas et al. 2018).

One possible approach for this would be to treat the expression $t_{ES} - t_{now}$ as a variable, which we will denote by slack. We can then treat the STN as a mathematical optimization problem, and maximize the slack. The slack for node $n$ can serve as a proxy for the probability of finding a solution in time in the subtree rooted at $n$. Our metarereasoning algorithm could then choose the next node to expand based on both heuristic estimates and the slack.

Acknowledgements

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References


