

# Recursive Best-First Search with Bounded Overhead

Matthew Hatem and Scott Kiesel and Wheeler Ruml



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# Problem Summary

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Background

■ Problem

■ IDDFS

■ IDA\*

■ RBFS

■ RBFS<sub>CR</sub>

Evaluation

Conclusion

- A\* remembers every state it visits, often exceeds memory

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    - Suffers from thrashing overhead

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  - ◆ Recursive Best-First Search (Korf 1993)
    - Always best-first!
    - Suffers from thrashing overhead
      - ◆ This is what we fix!

# Iterative Deepening Depth-First Search (IDDFS)

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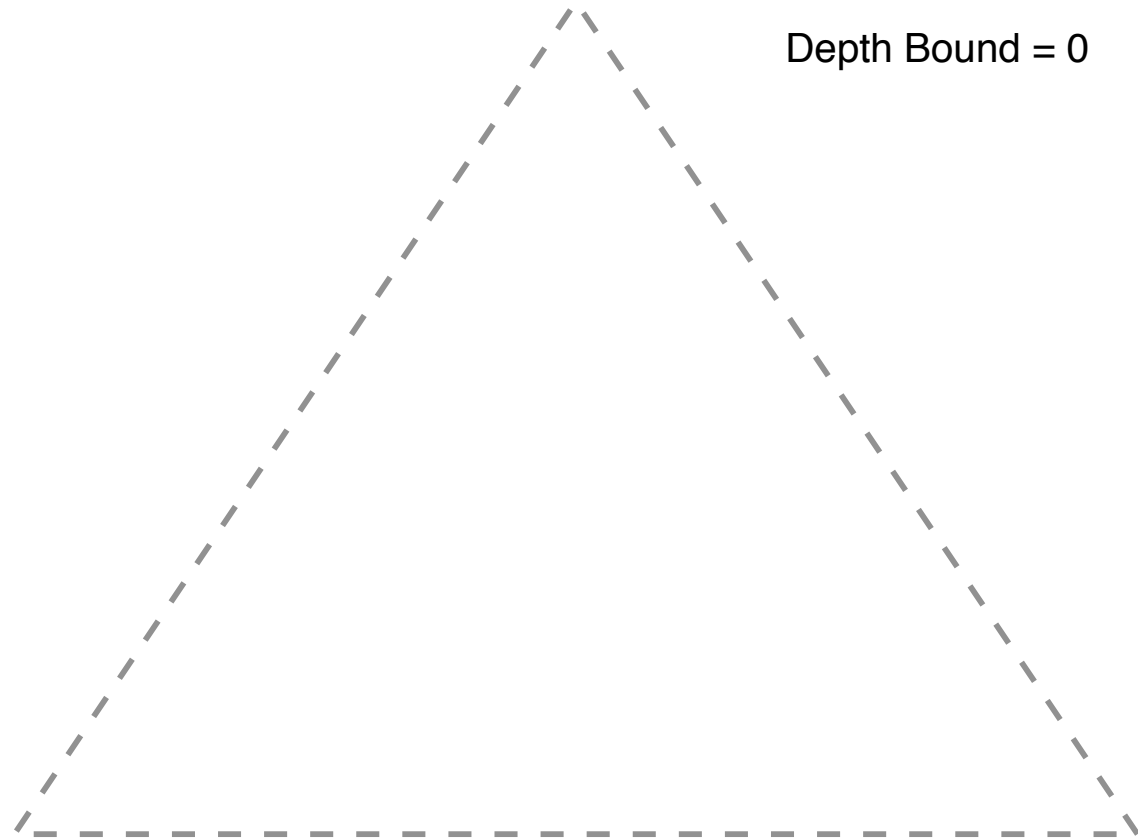
■ IDA\*

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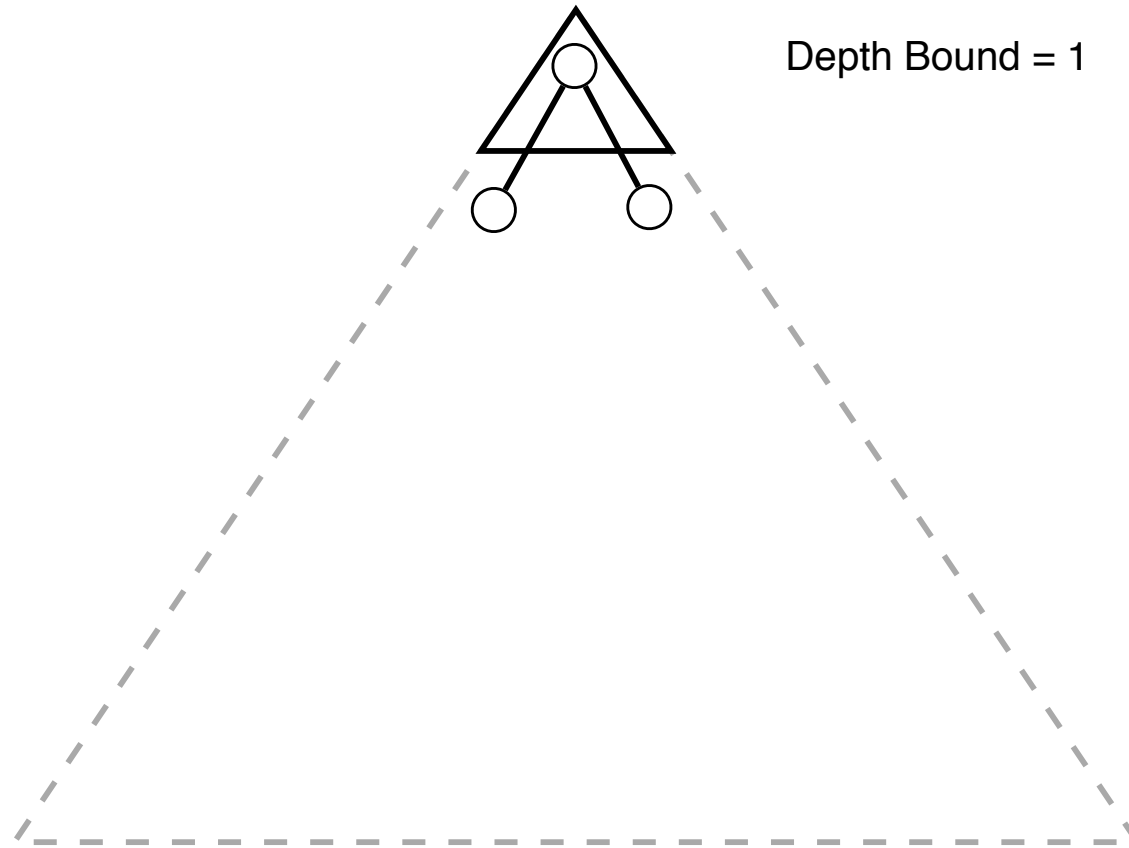
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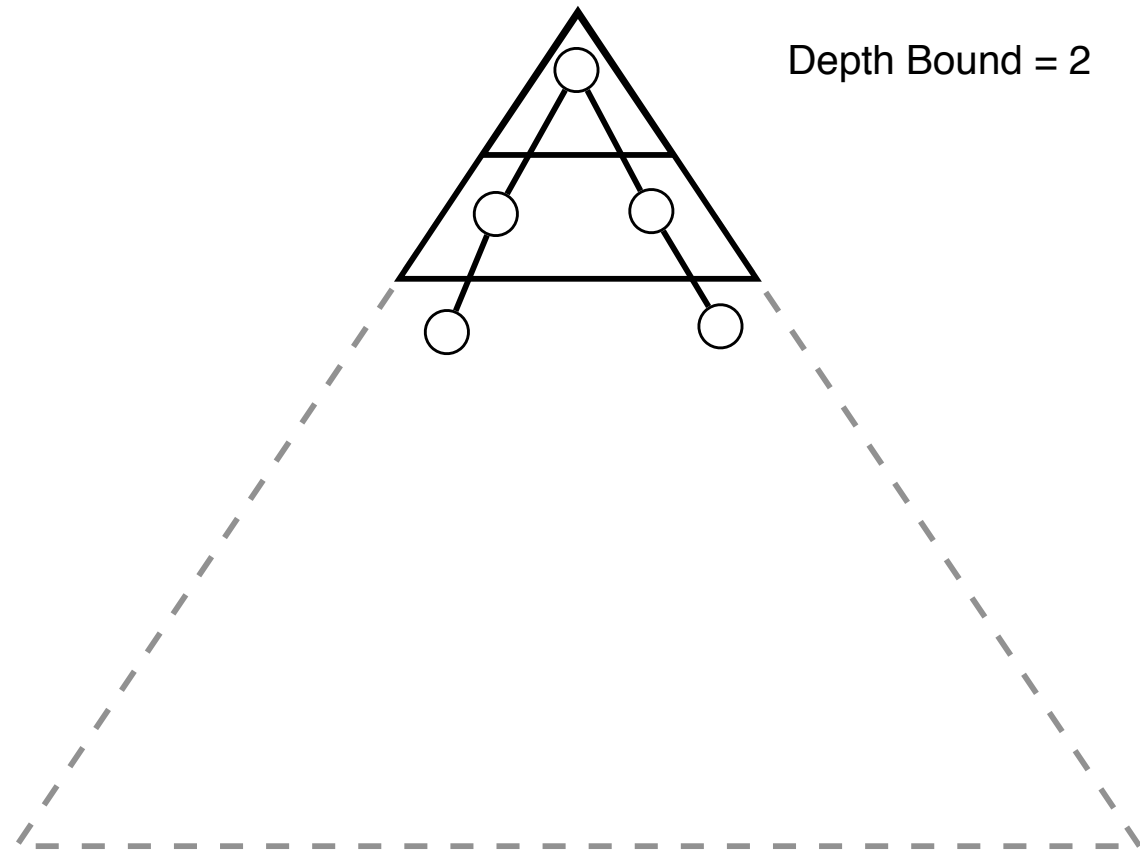
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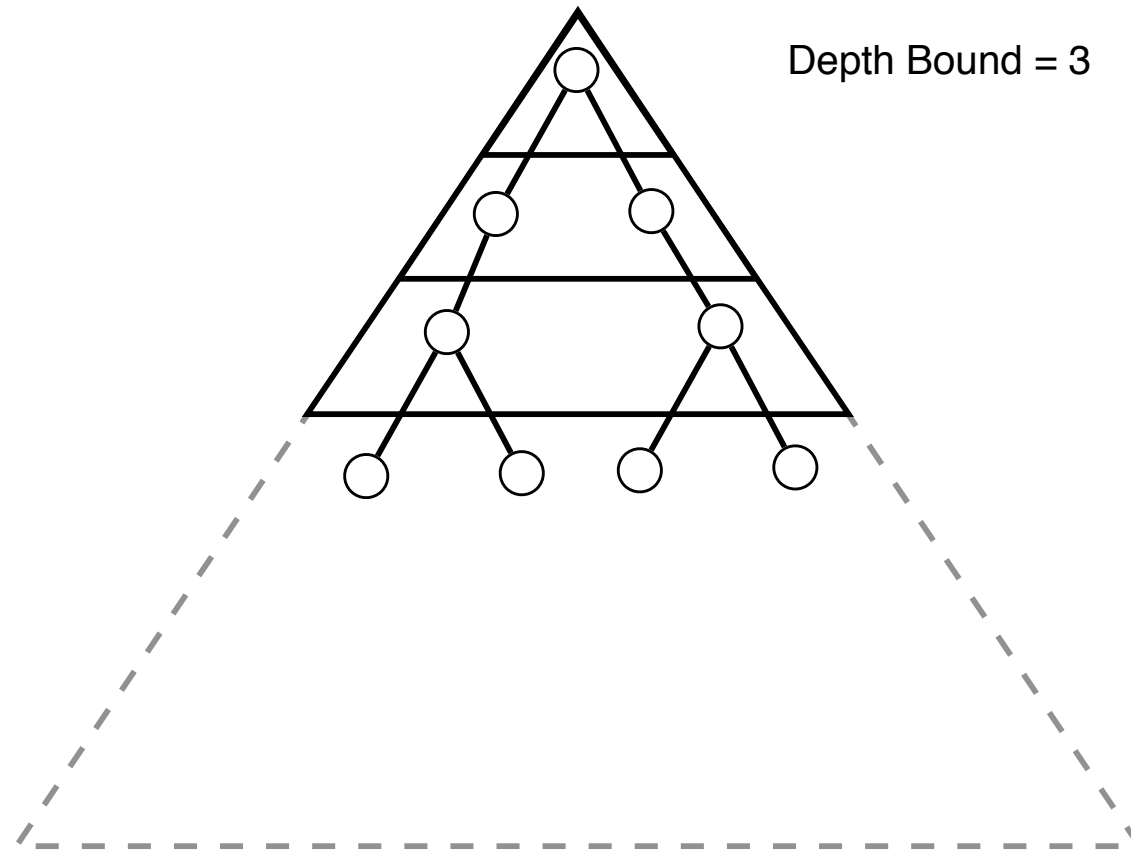
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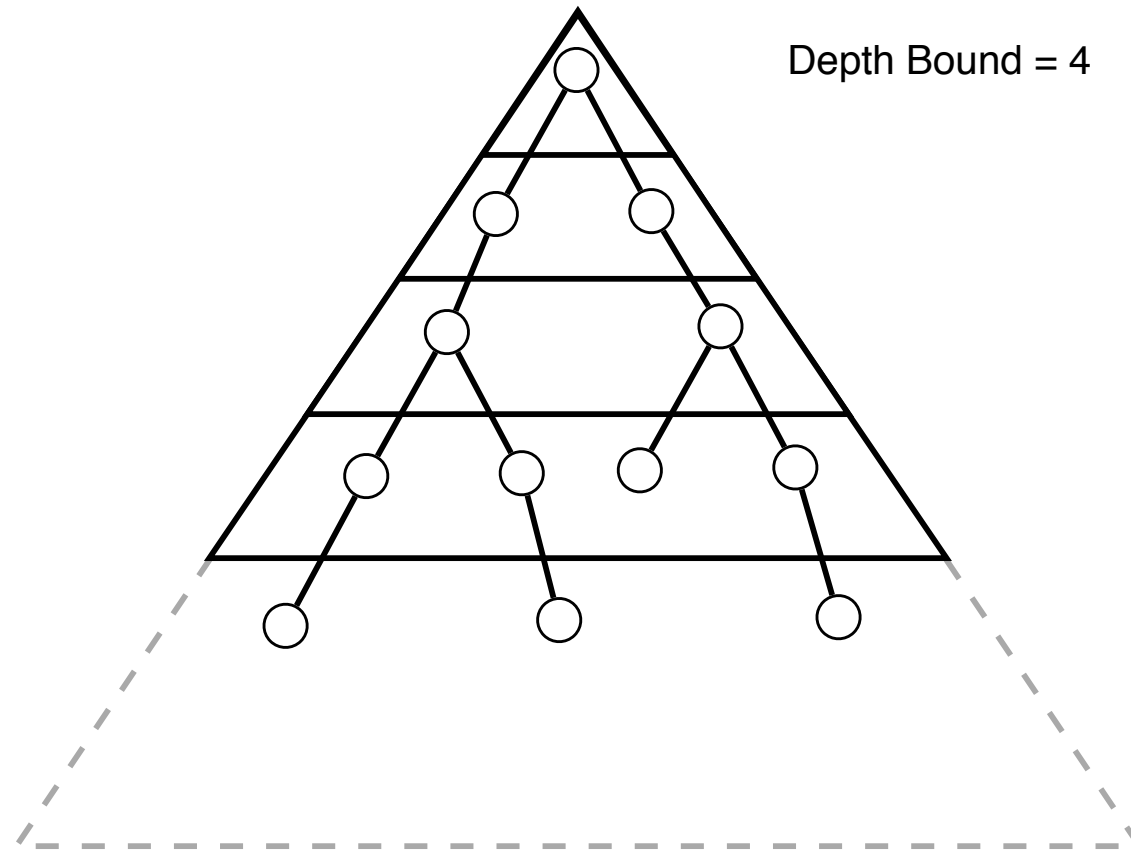
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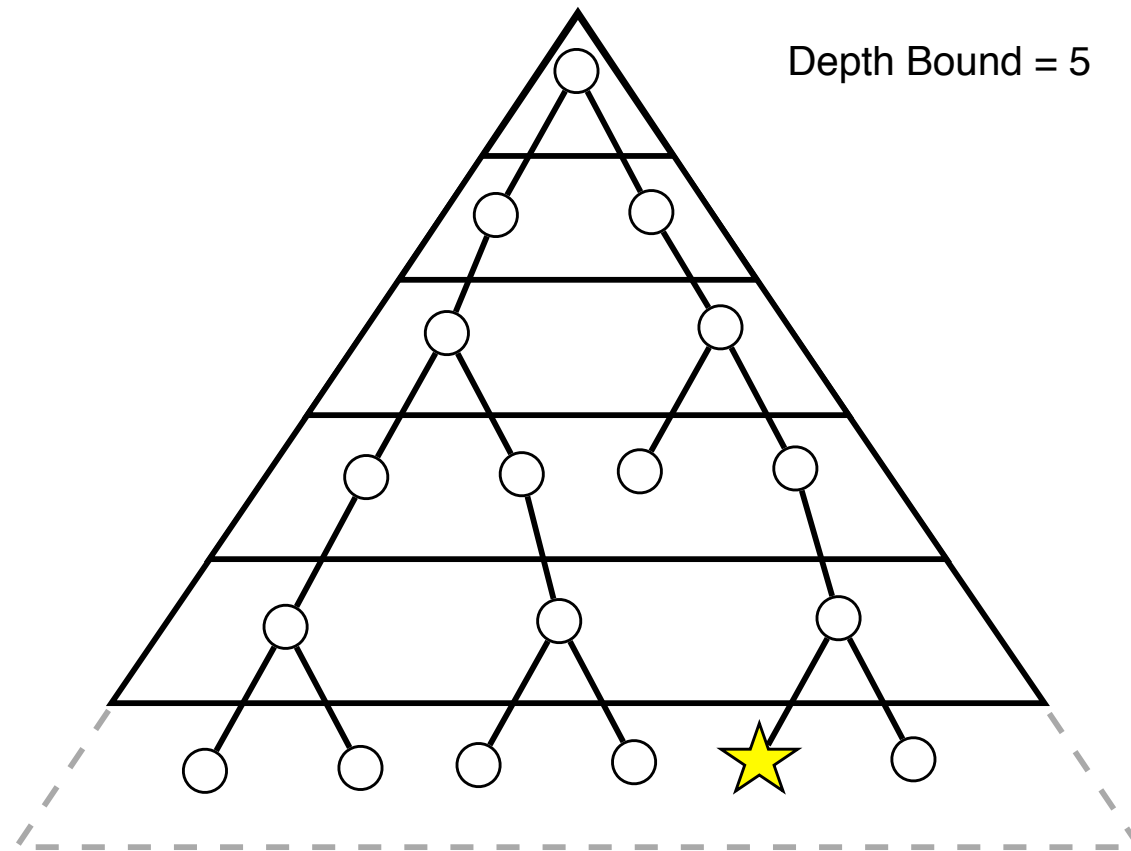
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# Iterative Deepening Depth-First Search (IDDFS)

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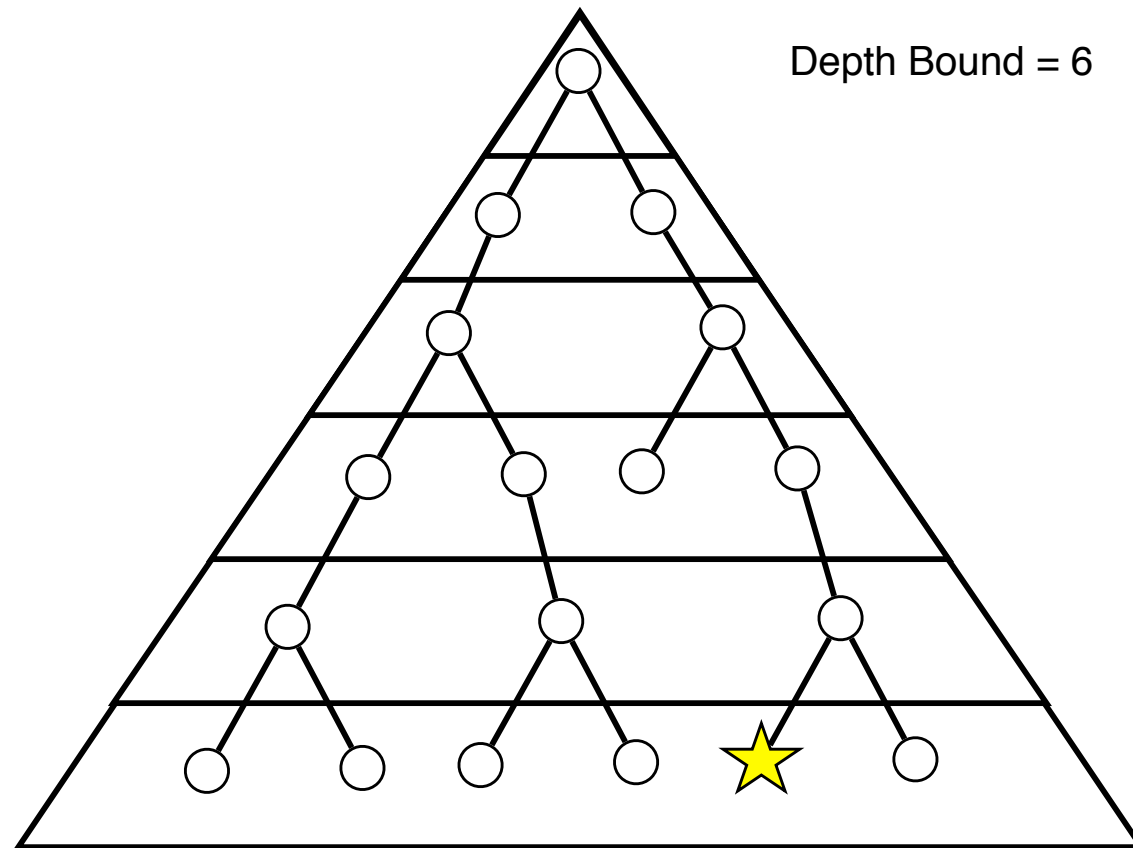
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# Iterative Deepening A\* (IDA\*)

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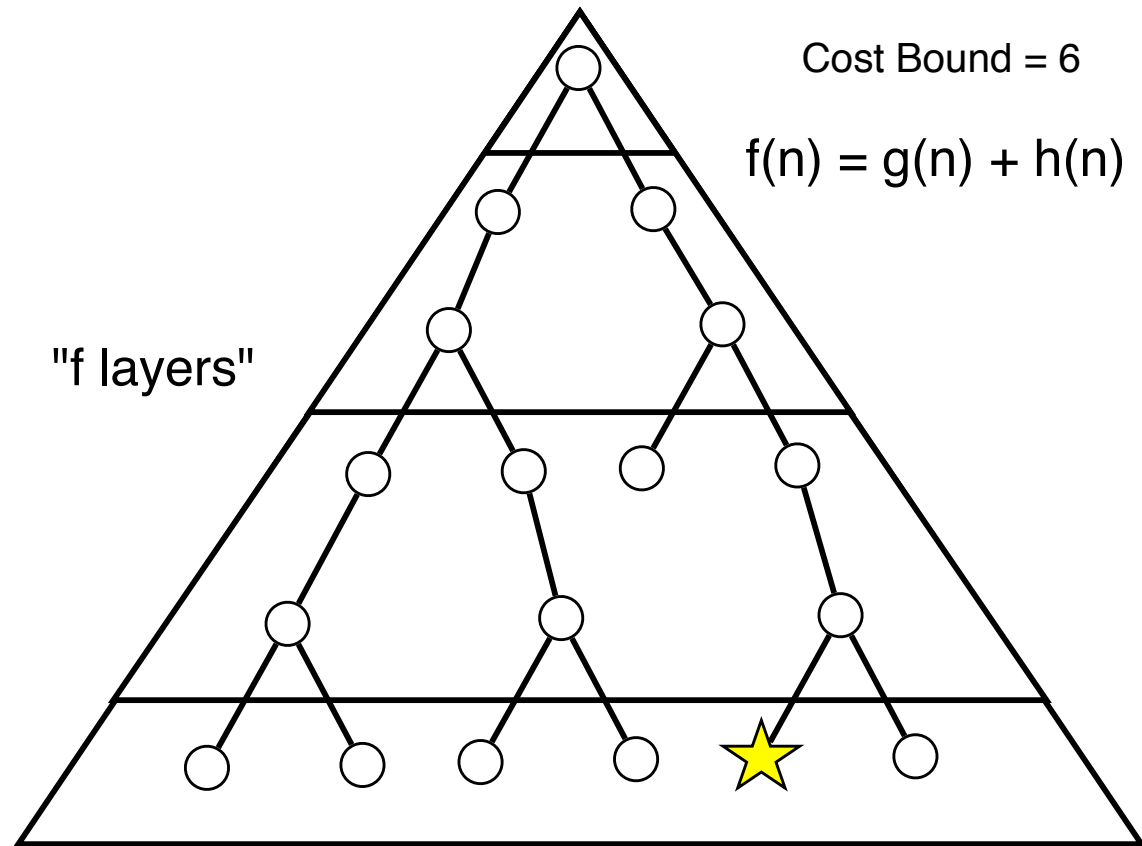
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# Iterative Deepening A\* (IDA\*)

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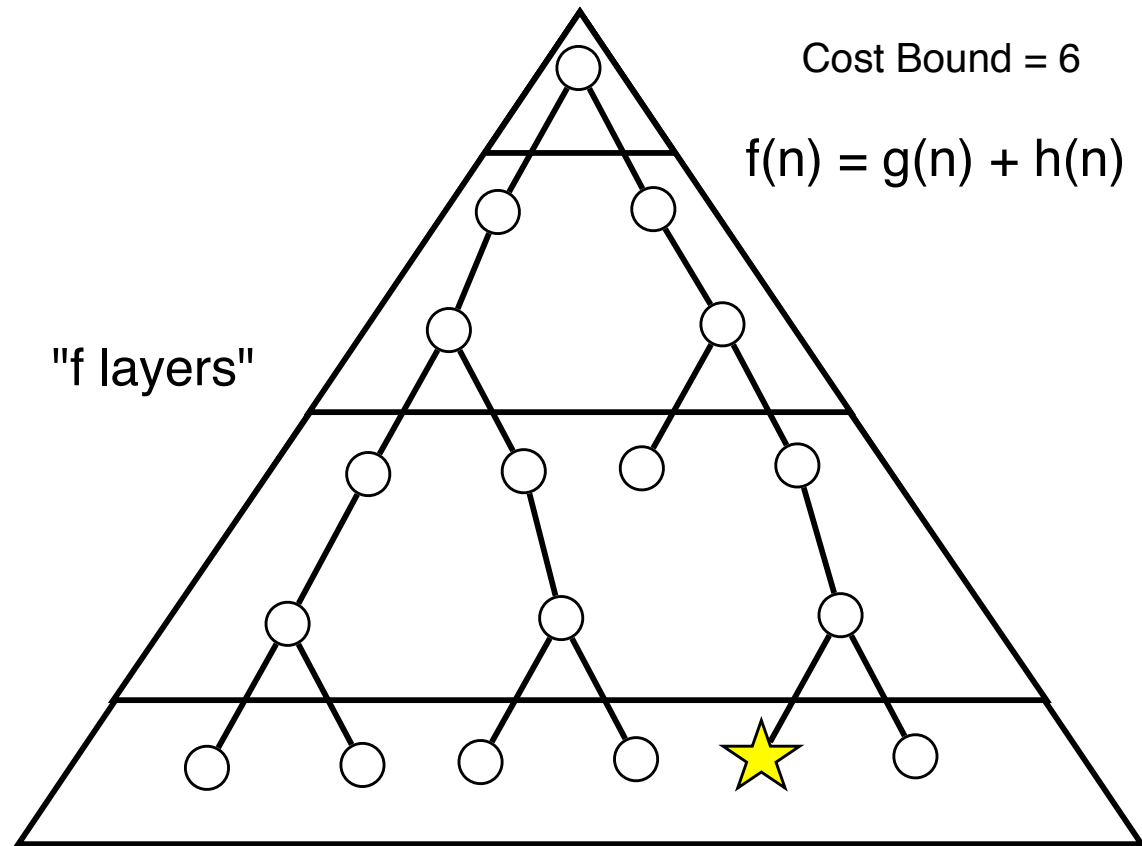
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Only best-first if f layers are monotonically increasing!  
(not the case in, eg, suboptimal variants)

# Recursive Best-First Search (RBFS)

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■ **RBFS**

■ RBFS<sub>CR</sub>

Evaluation

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# Recursive Best-First Search (RBFS)

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■ Problem

■ IDDFS

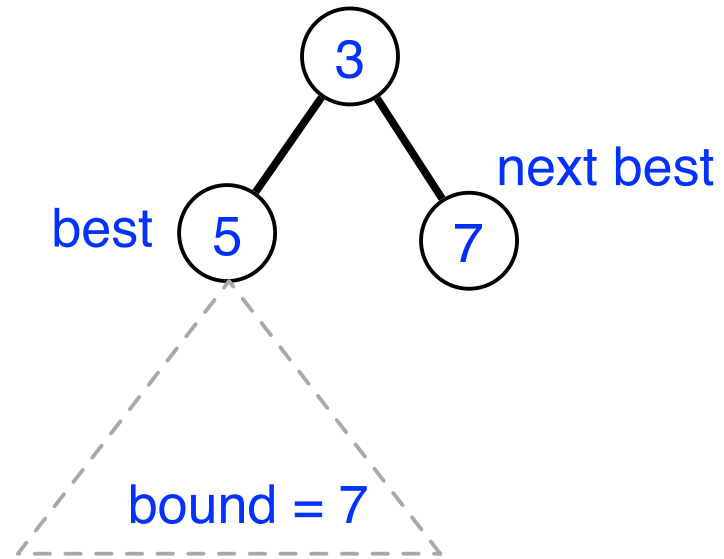
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# Recursive Best-First Search (RBFS)

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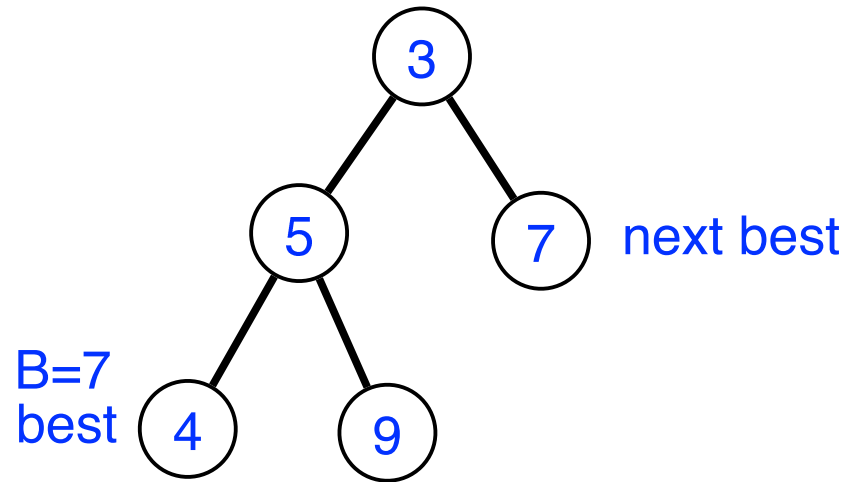
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# Recursive Best-First Search (RBFS)

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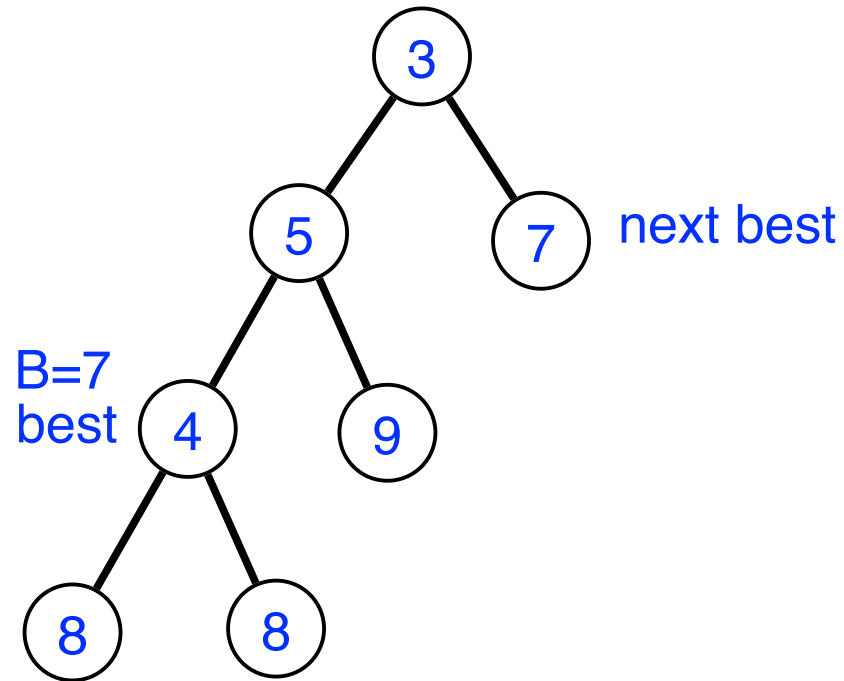
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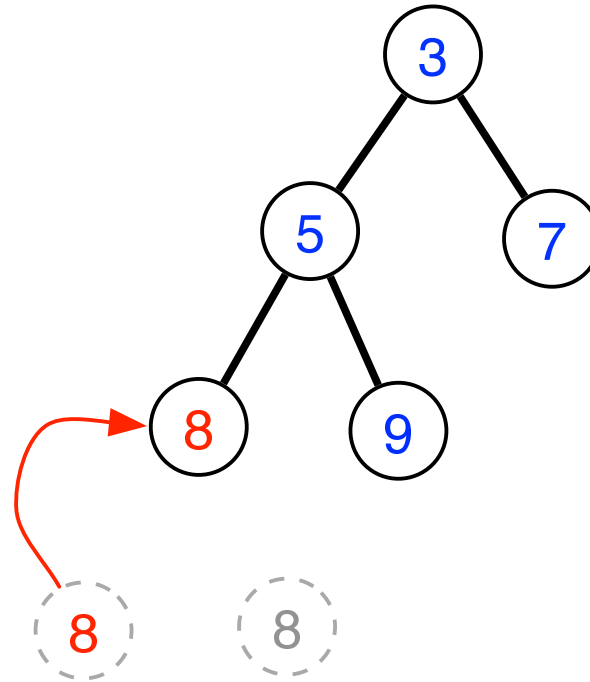
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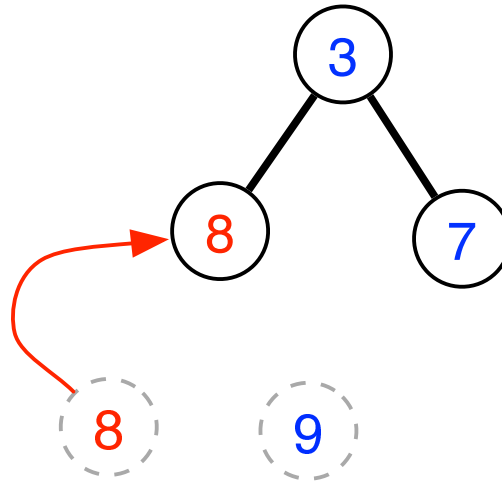
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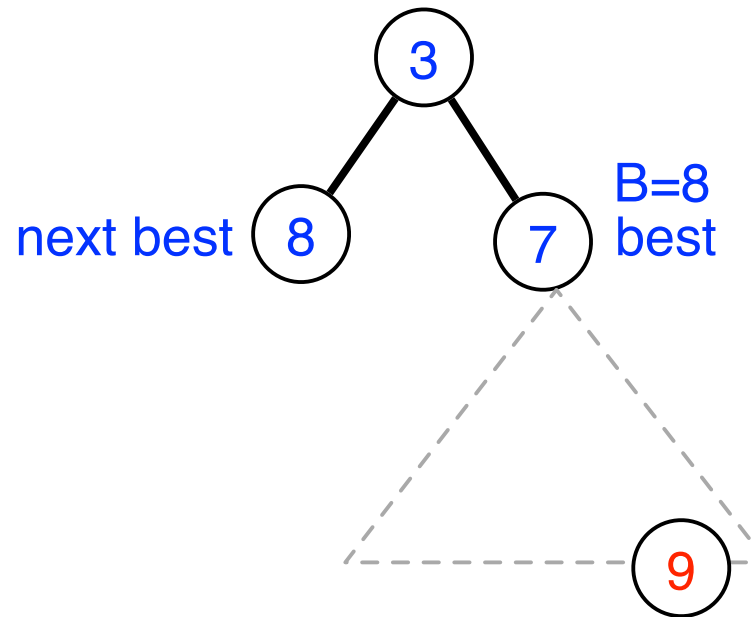
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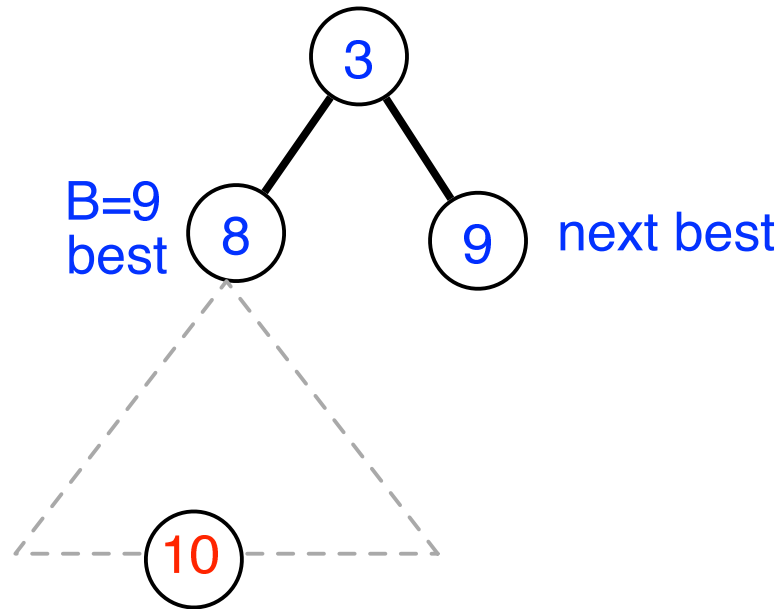
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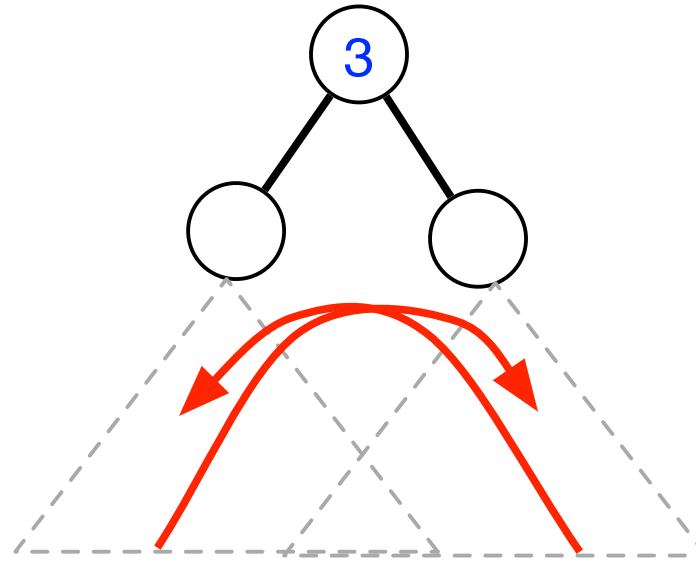
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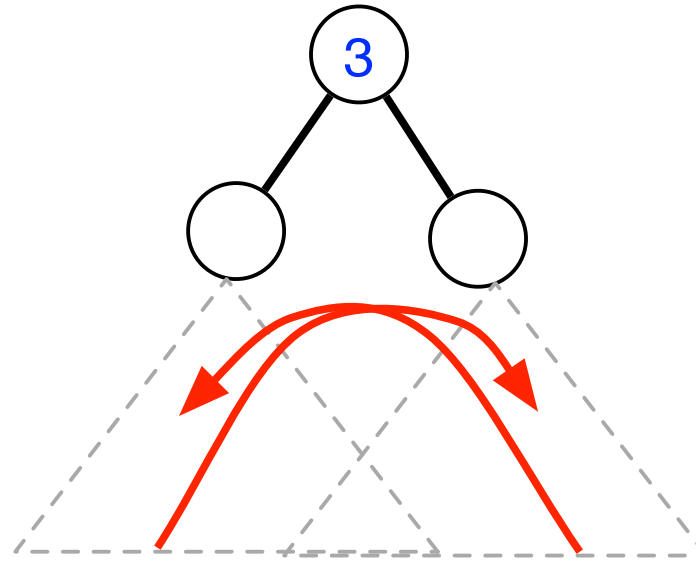
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Strict best-first search order causes thrashing!

# RBFS with Bounded Overhead

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■ Problem

■ IDDFS

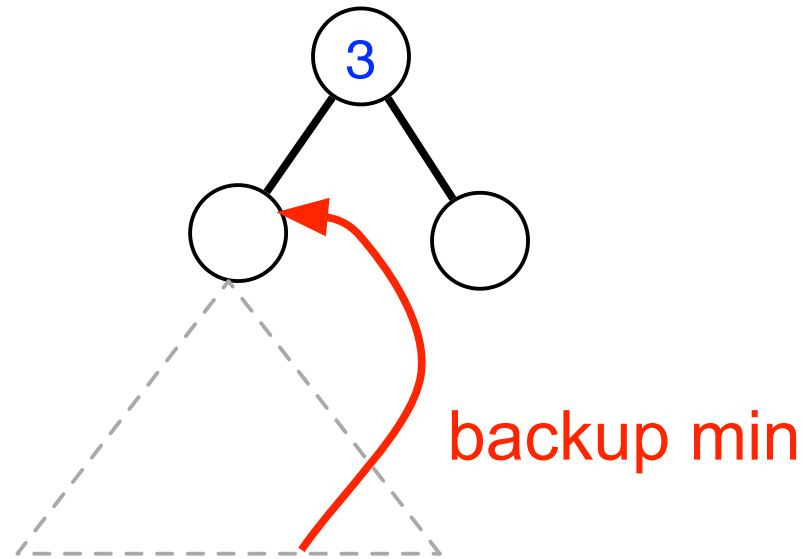
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# RBFS with Bounded Overhead

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■ Problem

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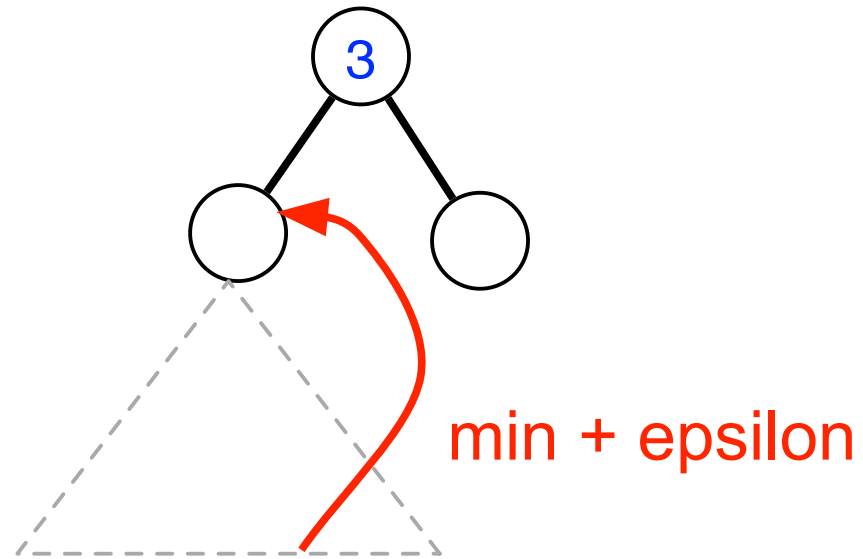
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# RBFS with Bounded Overhead

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■ Problem

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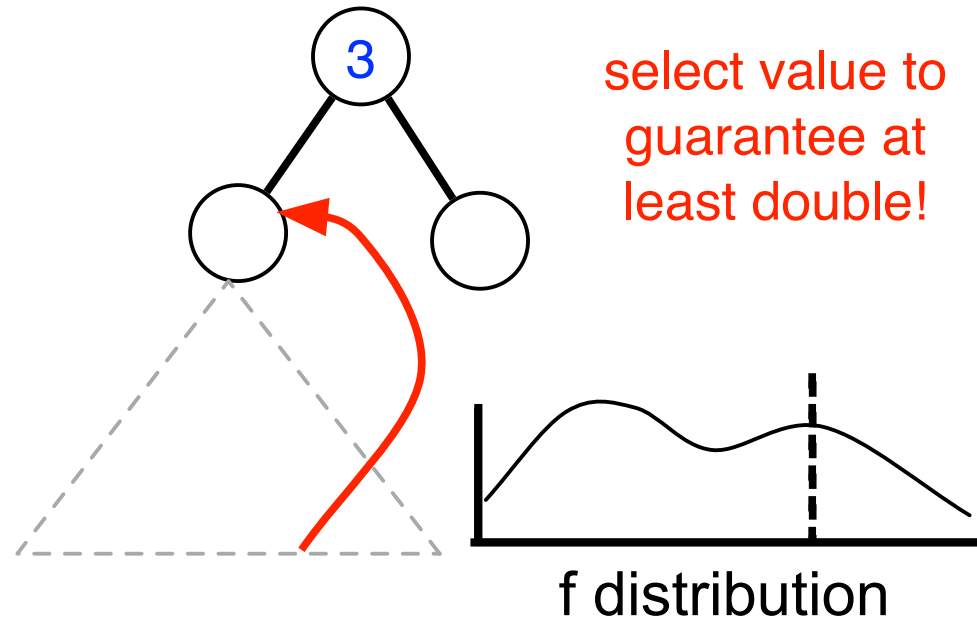
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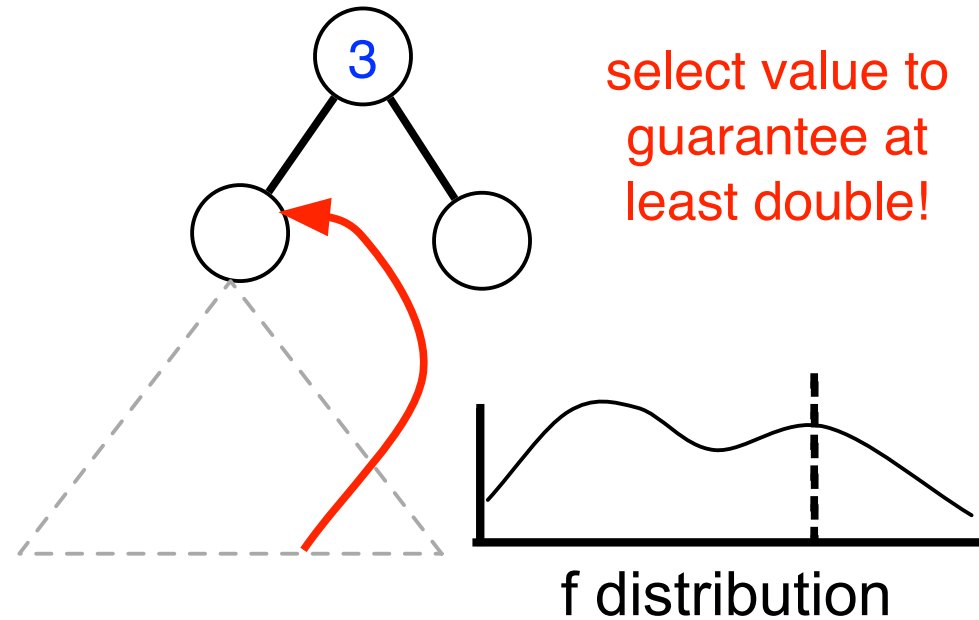
# RBFS with Bounded Overhead

## Background

- Problem
- IDDFS
- IDA\*
- RBFS
- RBFS<sub>CR</sub>

## Evaluation

## Conclusion



Relaxing best-first search order reduces overhead!  
See paper for proof

# Sliding Tile Puzzle

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Background

Evaluation

■ Tile Puzzle

■ Planning

Conclusion

- Korf 100 (Korf 1985)
- A\* with Manhattan Distance runs out of memory

6	2	5	14
3	15	4	
7	12	11	10
8	1	13	9

# Sliding Tile Puzzle

Background

Evaluation

■ Tile Puzzle

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Korfs 100 15 puzzles (unit cost)

(w=2)	Exp.	Avg. Cost	Time
RBFS	29,253,944	<b>62</b>	44
RBFS <sub>ε</sub>	13,078,227	71	30
RBFS <sub>CR</sub>	11,695,743	66	56
IDA*	<b>11,136,196</b>	68	<b>11</b>

Relaxing best-first search order gives faster solving times  
Better solutions but slower than IDA\*

# Dockyard Robot Planning

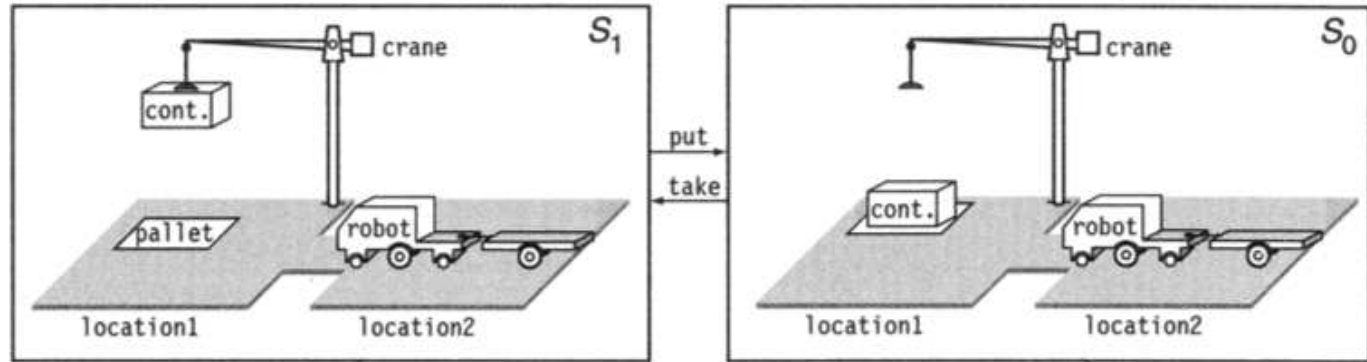
Background

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- From Ghallab, Nau, Traverso (2004)
- All actions have real costs
- Many duplicate states
- $IDA^*_{CR}$  and  $RBFS_{CR}$  with transposition tables

# Dockyard Robot Planning

Background

Evaluation

■ Tile Puzzle

■ Planning

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5 locations, cranes, piles and 8 containers

	Exp.	Exp./Sec.	Time	Reopened
IDA* <sub>CR</sub>	2,044m	112k	18,394	2,042m
RBFS <sub>CR</sub>	188m	103k	1,824	87m
RBFS <sub>ε=1</sub>	472m	<b>147k</b>	3,222	<b>4m</b>
RBFS <sub>ε=2</sub>	251m	140k	1,795	5m
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RBFS<sub>CR</sub> is faster because it expands 10x fewer nodes

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- IDA\* is depth-first, RBFS is always best-first!

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- Simple modifications reduce overhead (see paper)
- RBFS<sub>CR</sub> gives first provable bounds for overhead
- Is it time for IDA\* to retire?

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- IDA\* is depth-first, RBFS is always best-first!
- Simple modifications reduce overhead (see paper)
- RBFS<sub>CR</sub> gives first provable bounds for overhead
- Is it time for IDA\* to retire?
- RBFS deserves more attention!
  - ◆ IDA\* citations: 1523
  - ◆ RBFS citations: 310

Background

Evaluation

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**Backup**

# Backup

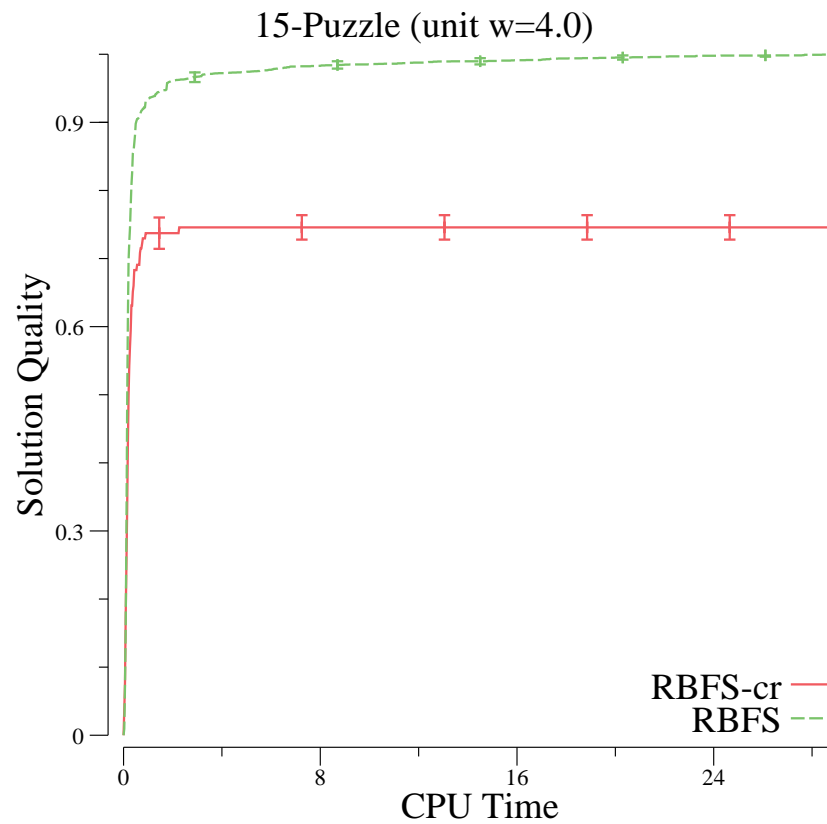
# Anytime Heuristic Search

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Evaluation

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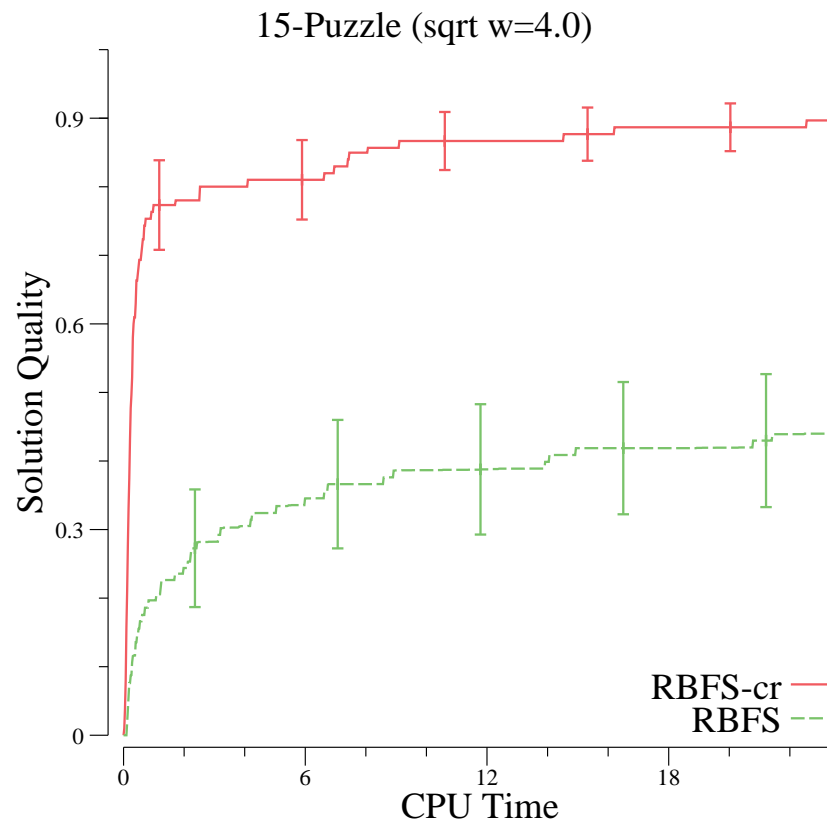
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