

Real-time Motion Planning with Dynamic Obstacles

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Motivation

Introduction

■ Motivation

■ The Problem

■ Execution

■ Heuristic Search

■ The Search Space

■ Two Approaches

■ The Literature

Real-time R*

RTA* for Robotics

Evaluation

Conclusion



- planning for robots!
- responsiveness, safety: real-time with dynamic ‘obstacles’
- kino-dynamic motion planning, not shortest path
- heuristic search is general and powerful
- human environments are generally forgiving

The Problem

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Given at start:

- map of static world
- goal pose for agent
- time bound per action

Given at each step:

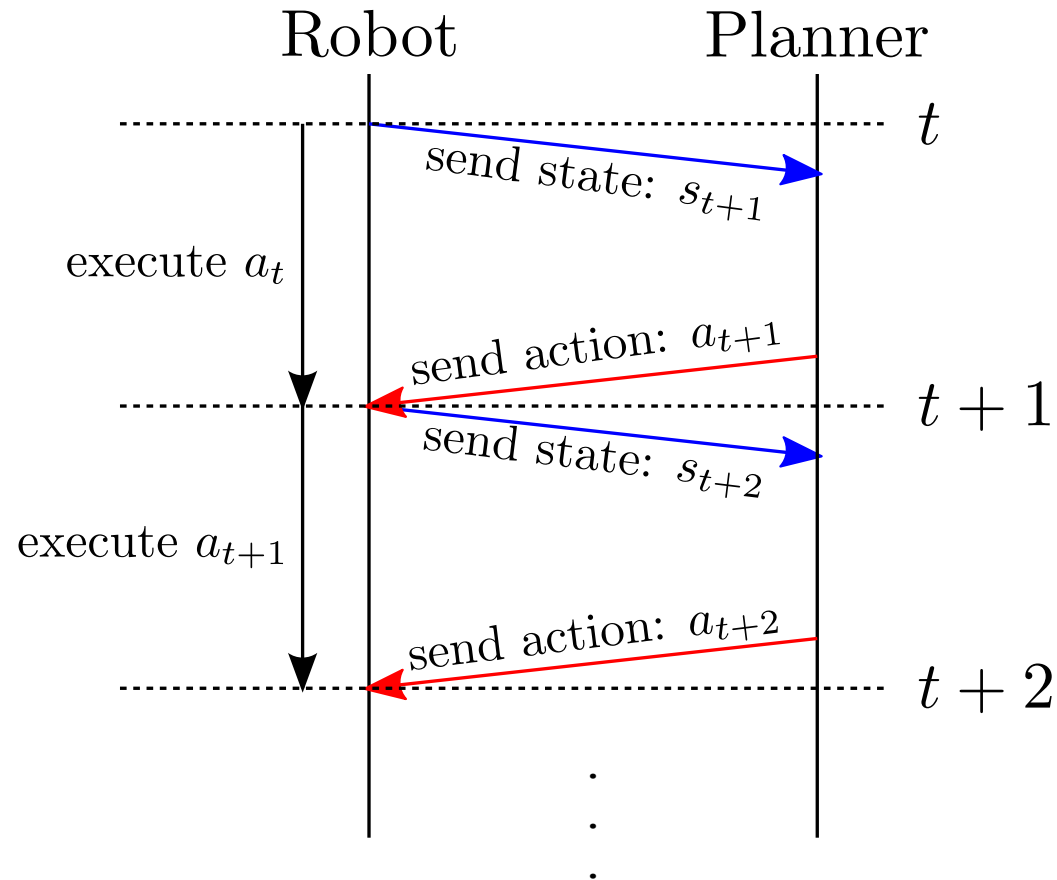
- agent's estimated pose
- probabilistic estimates for each dynamic obstacle's future

Find:

- within time bound
- feasible action
- that minimizes agent's total cost to horizon

Execution Setting

while executing, plan for next action



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agent's state: x, y, θ, s

obstacles move, so world state adds t

discretize space and time to yield motion primitives

$$\text{cost} = P(\text{col}) \cdot \text{cost}_{\text{col}} + \text{cost}_{\text{time}}$$

The Search Space

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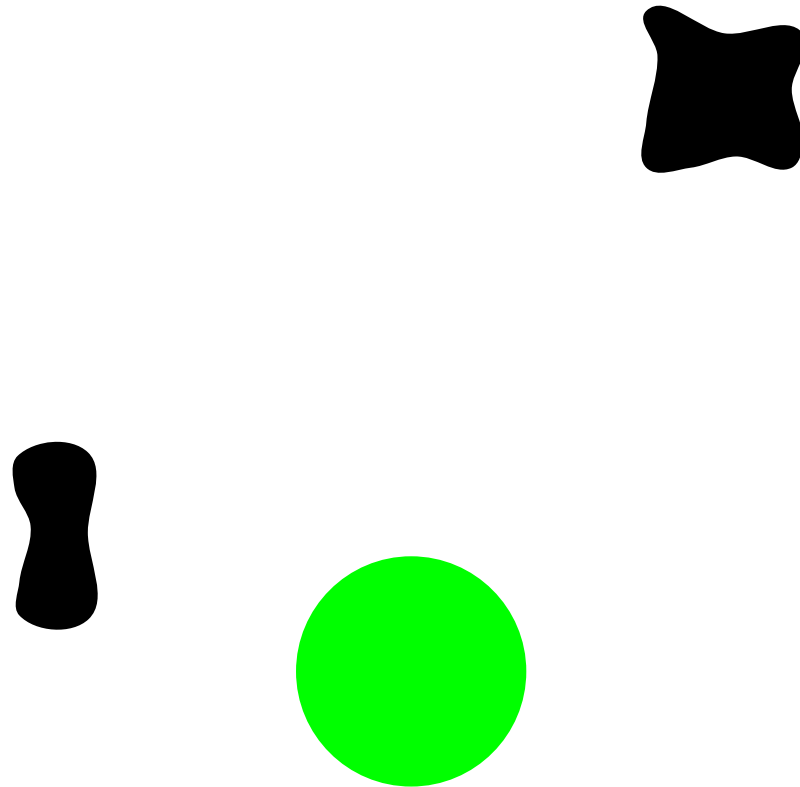
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robot with two static obstacles

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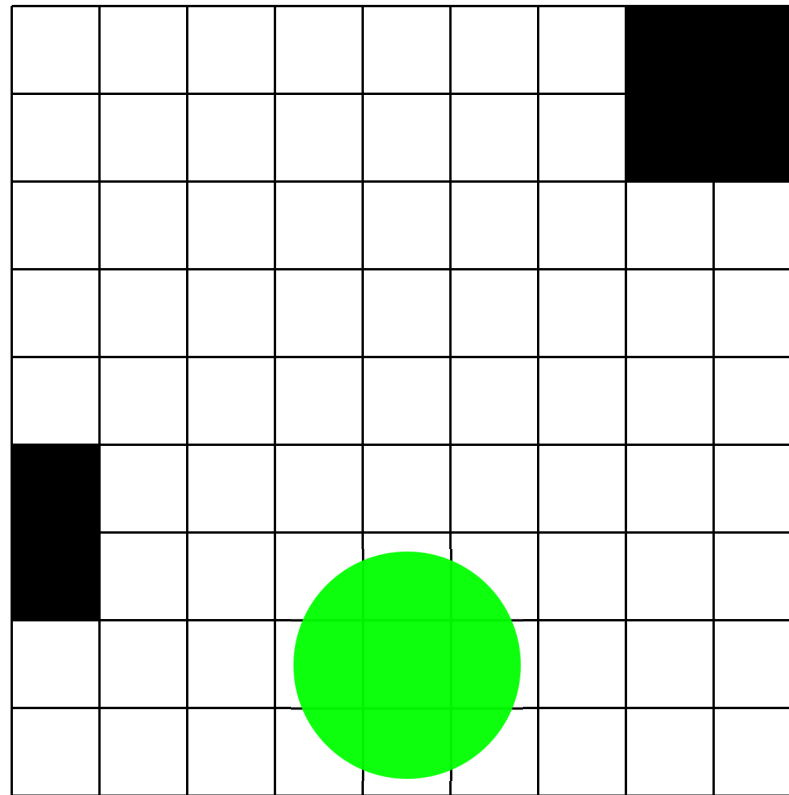
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overlay grid

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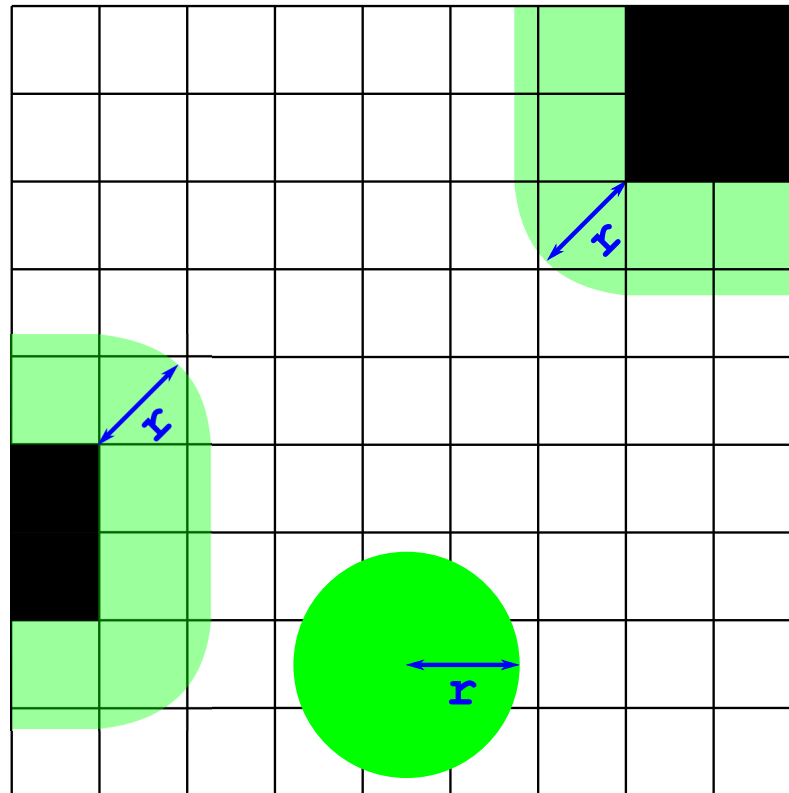
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expand static obstacles by robot's radius

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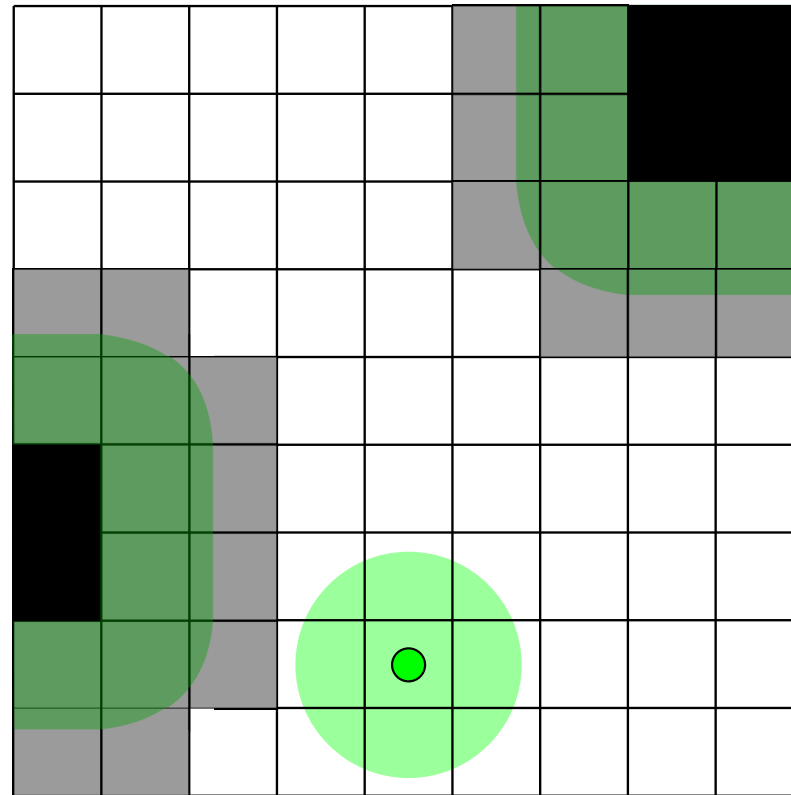
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robot now a single point

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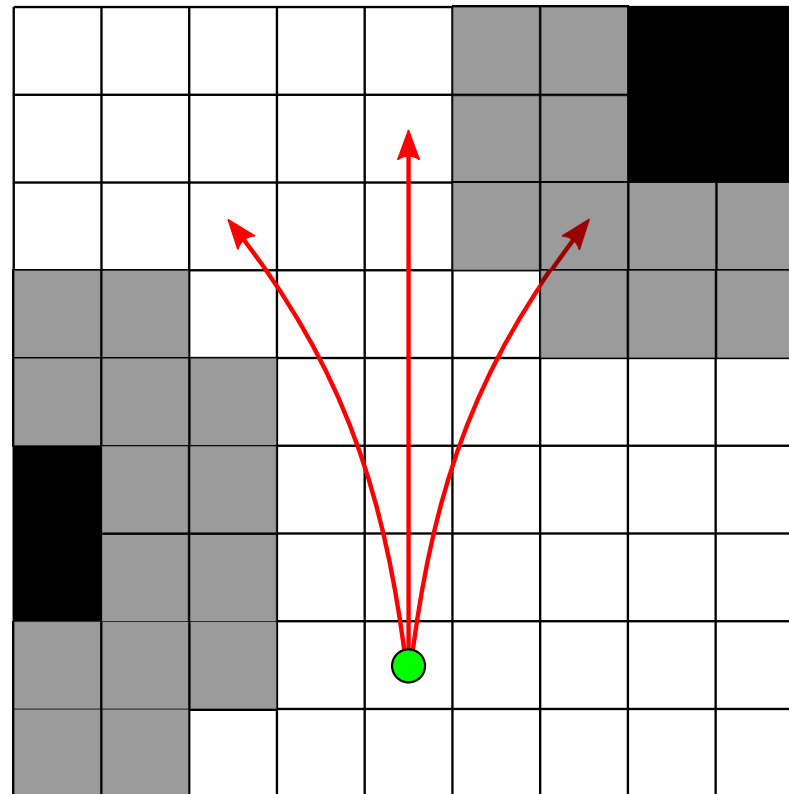
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applicable actions

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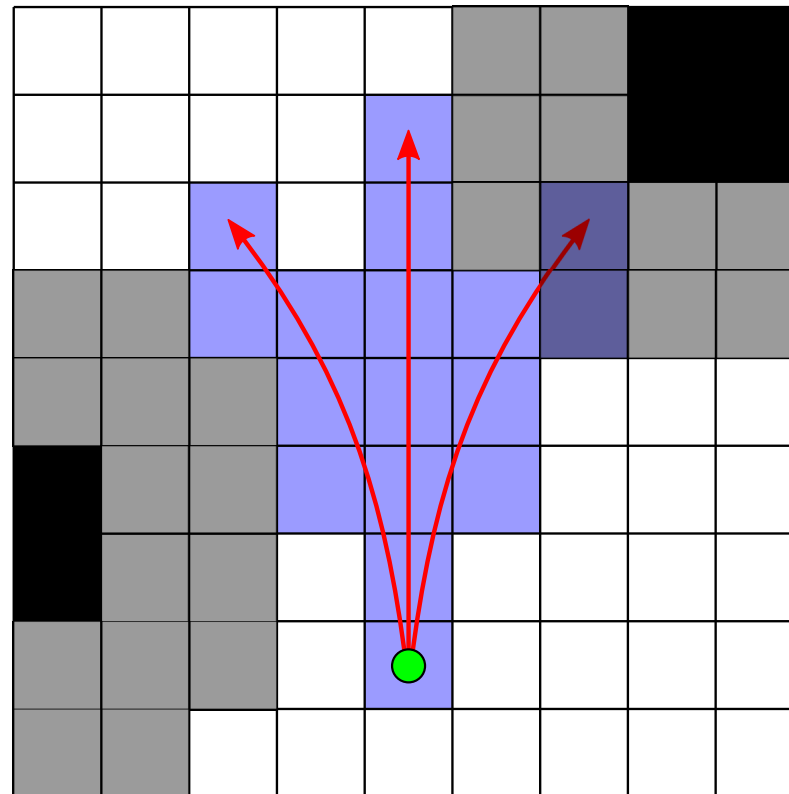
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(pre-)compute touched cells

The Search Space

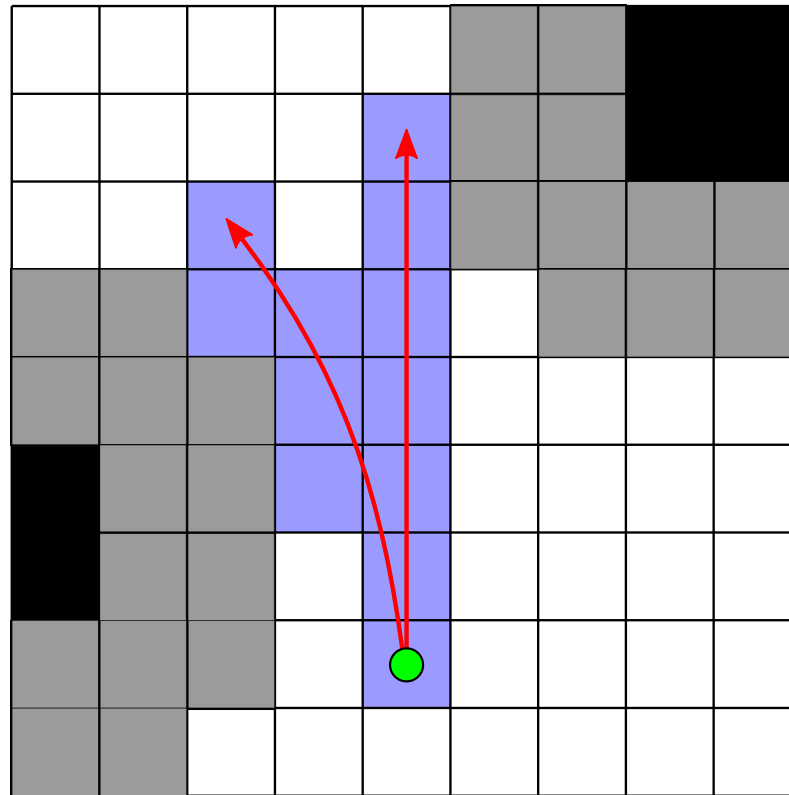
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remove actions with static collisions

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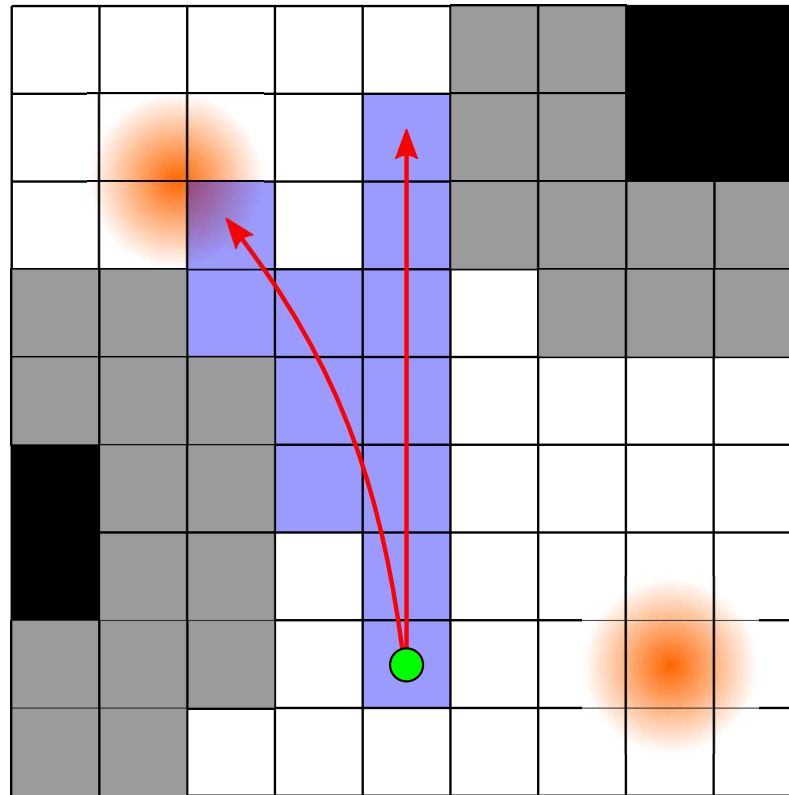
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time-dependent obstacle probability distributions

Two Approaches

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Motion Planning:

Take a search algorithm designed for motion planning, and make it real-time.

Real-time Search:

Take a real-time search algorithm, and adapt it to motion planning.

The Heuristic Search Literature

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Motion Planning:

“R* [provides] probabilistic guarantees on the suboptimality of the overall solution [and] can scale to large complex planning problems, can find solutions to such problems much more often than weighted A* search, and can minimize the cost of the found solutions much better than randomized motion planning algorithms, developed specifically for continuous domains.” — Likhachev and Stentz, *AAAI*, 2008

Real-time Search:

“We illustrate agent-centered search in nondeterministic domains using robot-navigation tasks” — Koenig, *AI Magazine*, 2001

“State-of-the-art real-time search algorithms, like LSS-LRTA*” — Hernandez and Baier, *JAIR*, 2012

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Real-time R*

■ R*

■ Advantages

■ Overview

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Real-time R*

R* Search

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■ R*

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- Combines ideas from heuristic search and random sampling
- Breaks search up into smaller, easier subproblem
- High-level nodes are sampled randomly
- Low-level search between high-level nodes

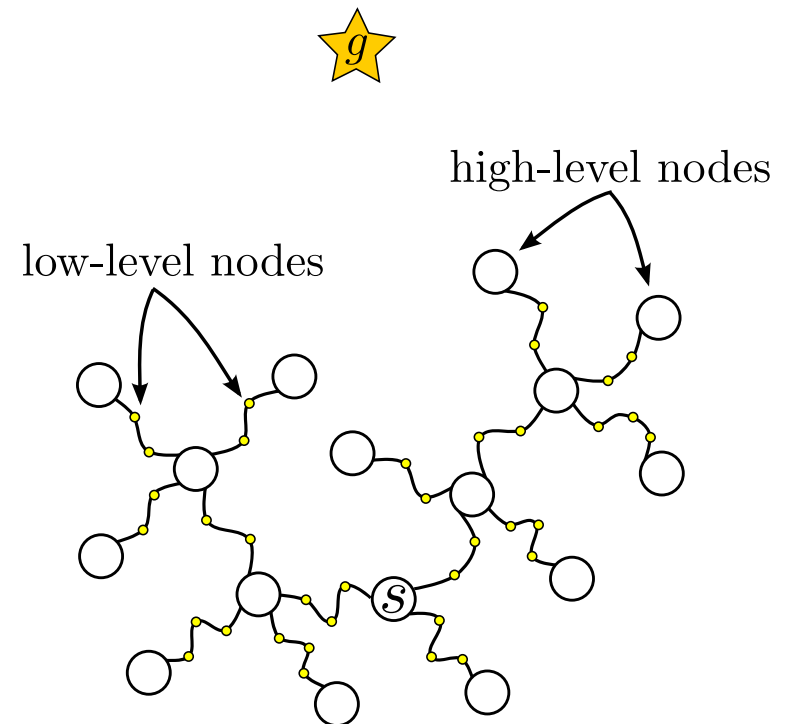


Figure 1: R* Search

(Likhachev and Stentz, 2008)

R* Advantages

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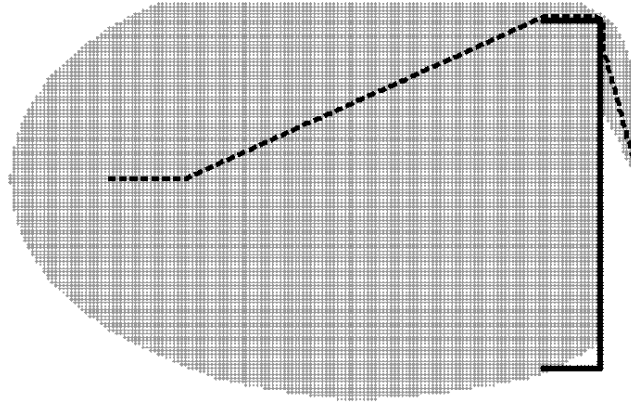


Figure 2: A* Search

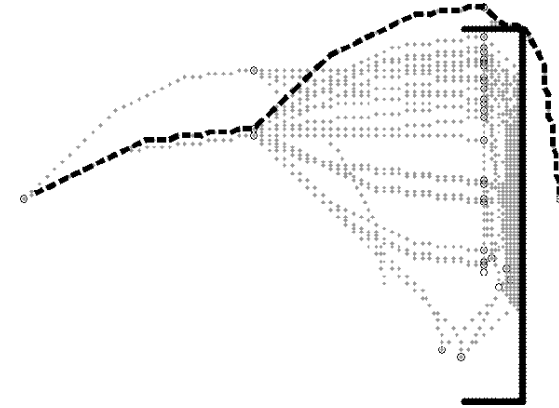


Figure 3: R* Search

- samples continuous space sparsely
- finds solutions faster than ARA*, lower cost than RRT
- works well in high dimensions and with local minima

Real-time R* Overview

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■ R*

■ Advantages

■ **Overview**

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Modifications:

1. Bounded lookahead: count high-level expansions more
2. Action selection: prefer nodes with low-level paths
3. Path caching: save high-level nodes only
4. Making easier subproblems: loose goal test
5. Limit work on “avoid” nodes: exponentially increasing bound

see paper for details

Introduction

Real-time R*

RTA* for Robotics

■ LSS-LRTA*

■ Challenges

■ Partitioned Costs

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Local Search Space Learning Real-Time A* (LSS-LRTA*)

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■ LSS-LRTA*

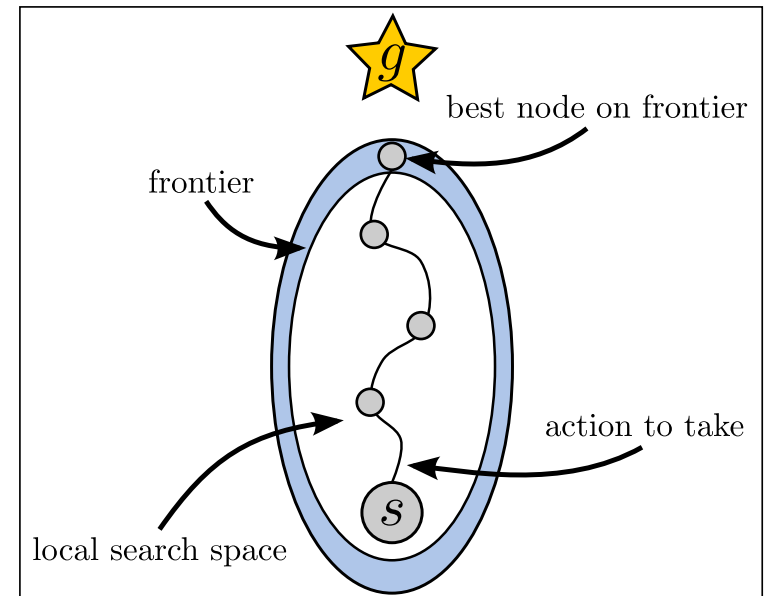
■ Challenges

■ Partitioned Costs

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- A* until node expansion limit.
- Move toward best node on *open*



- Learn improved heuristic for all expanded nodes
 - ◆ Compute shortest paths back from the frontier

(Koenig and Sun, 2009)

The Challenge of Dynamic Motion Planning

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■ LSS-LRTA*

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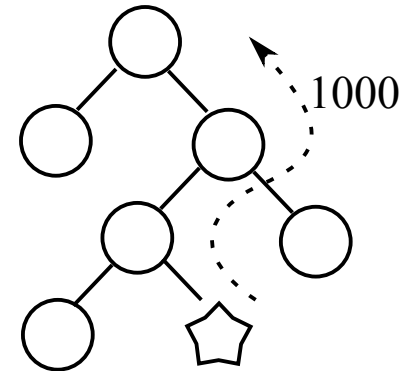
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theoretical: inadmissible g values

- no good h for dynamic obstacles
- estimated collisions noticed via g values
- edge costs in graph are changing!
- backed-up values inadmissible

practical: many possible paths

- hard to back-up a higher value



Partitioned Costs

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Modifications:

- partition cost into static versus dynamic

$$f(n) = g_s(n) + g_d(n) + h_s(n) + h_d(n)$$

- learn separate static and dynamic h values
- all states at pose share h_s value
- decay h_d values for completeness

see paper for details

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- Evaluation
- Random Bms.
- Cost Incurred
- Scaling

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unusually wide variety of algorithms:

1. RTA*
2. LSS-LRTA*
3. PLRTA* - partitioned learning
4. R*
5. RTR* - real-time
6. RRT
7. TBL

two types of problems:

1. 36 random 'frogger' benchmarks
2. 6 handcrafted challenge problems

Random Benchmarks

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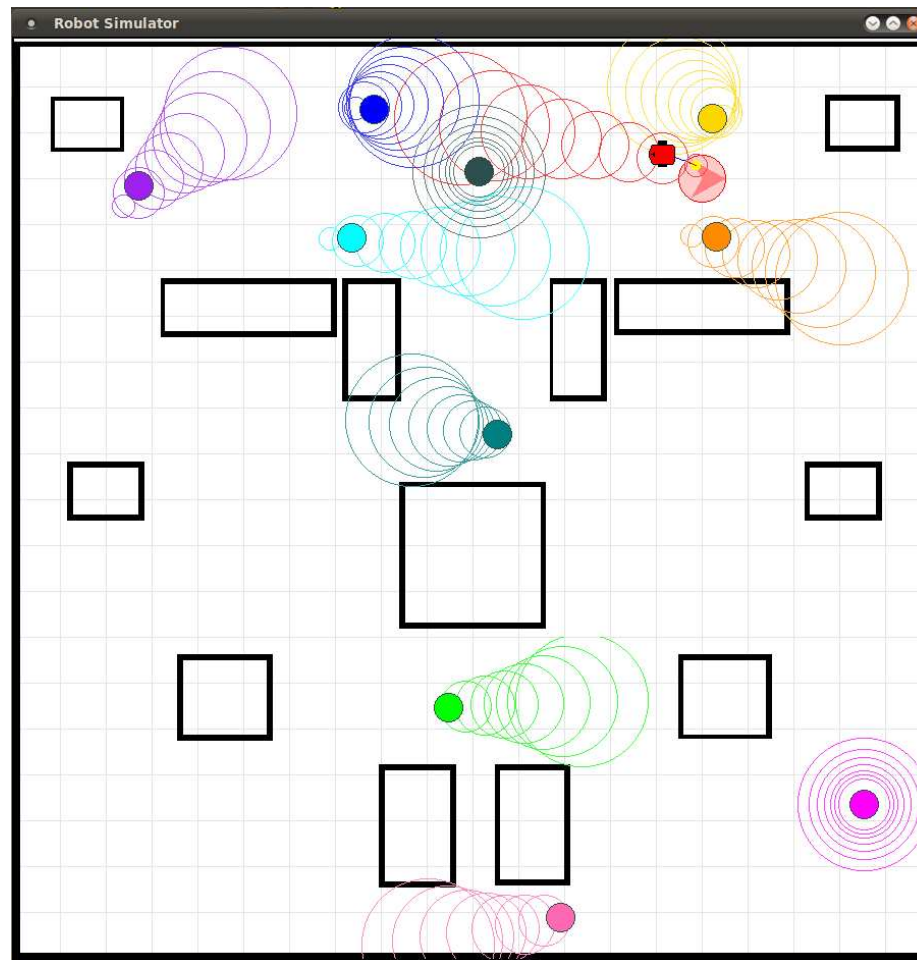
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■ **Random Bms.**

■ Cost Incurred

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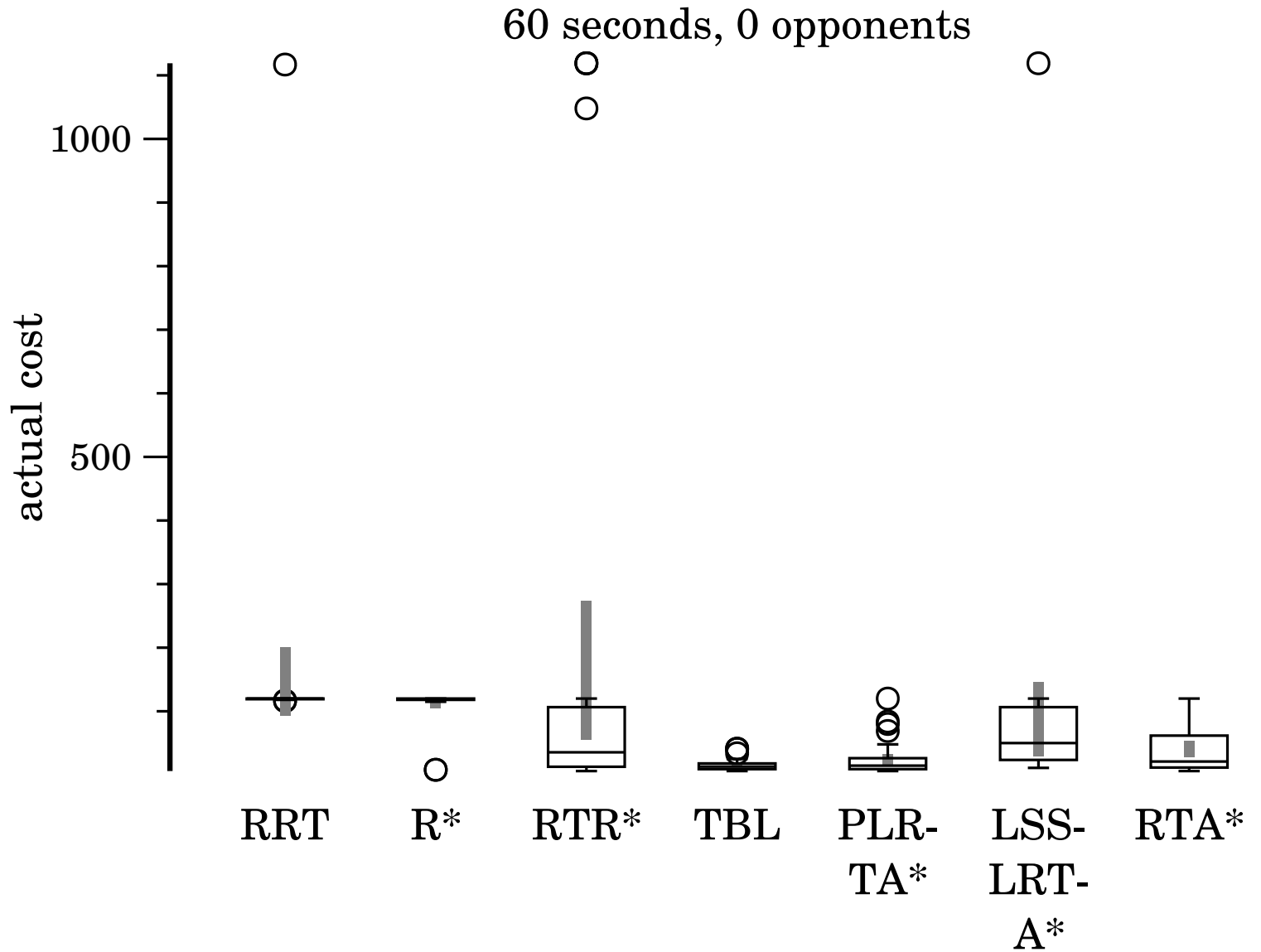
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36 random start/goal pairs, with prerecorded obstacles

Cost Incurred

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Cost Incurred

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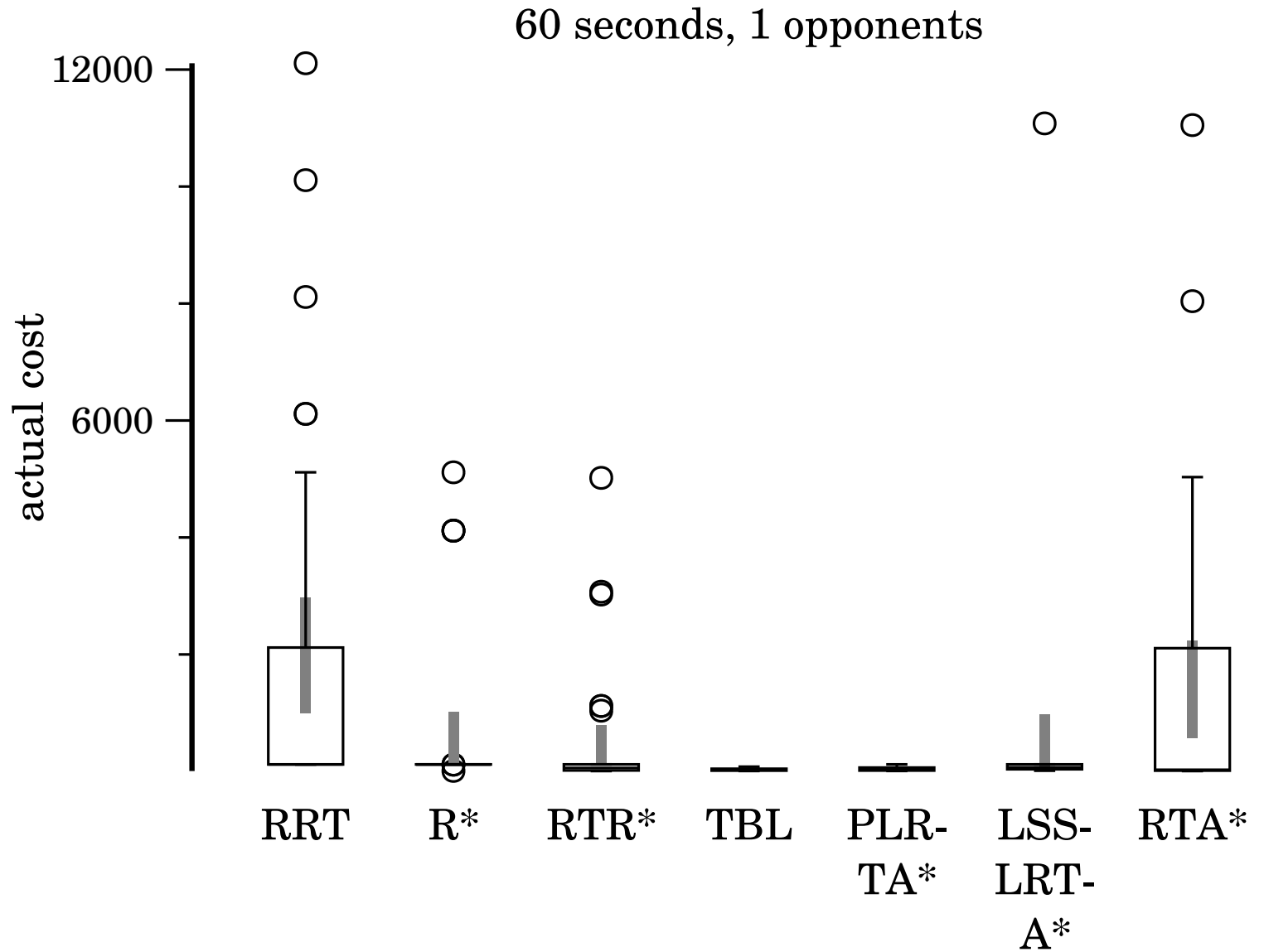
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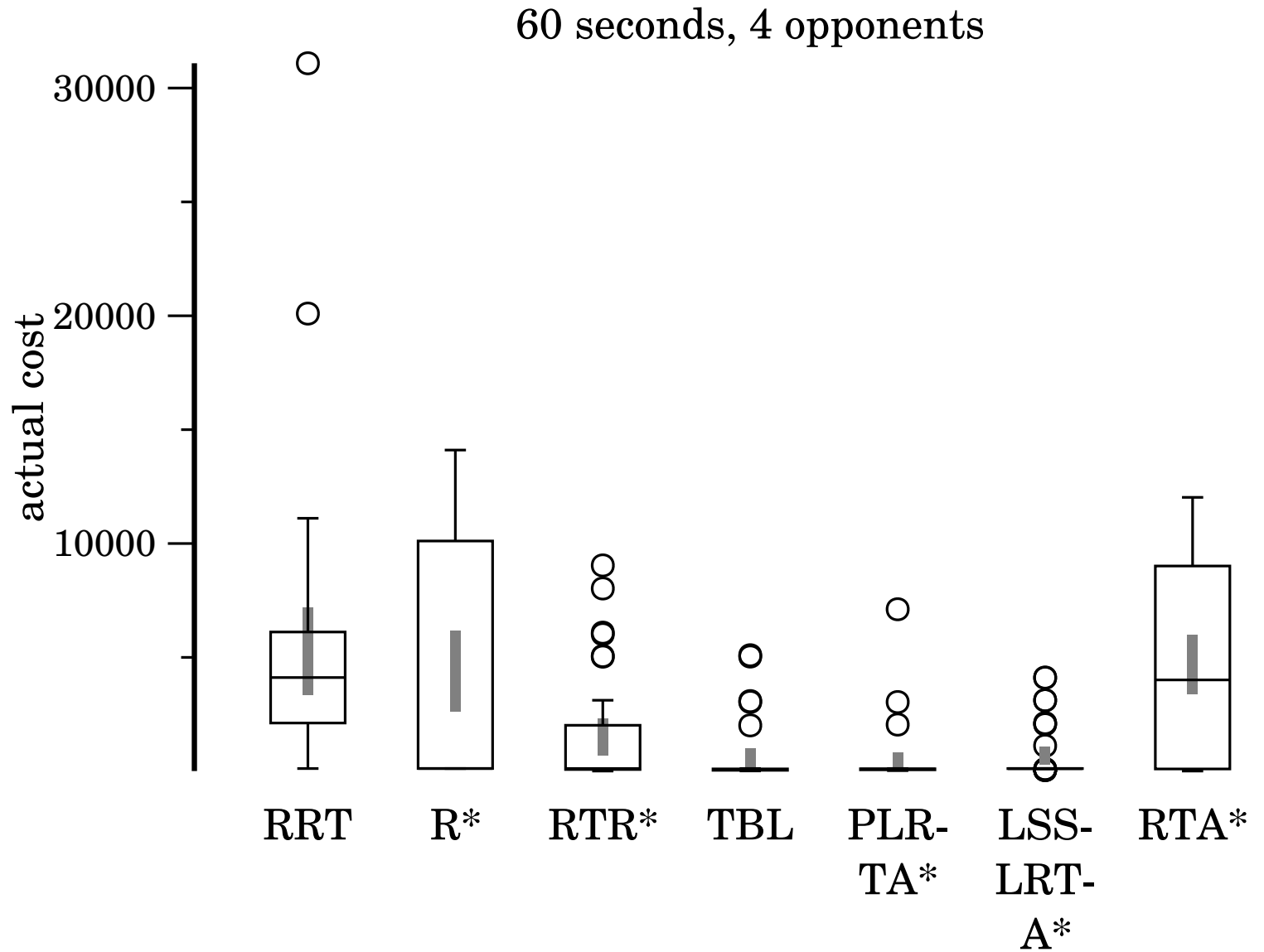
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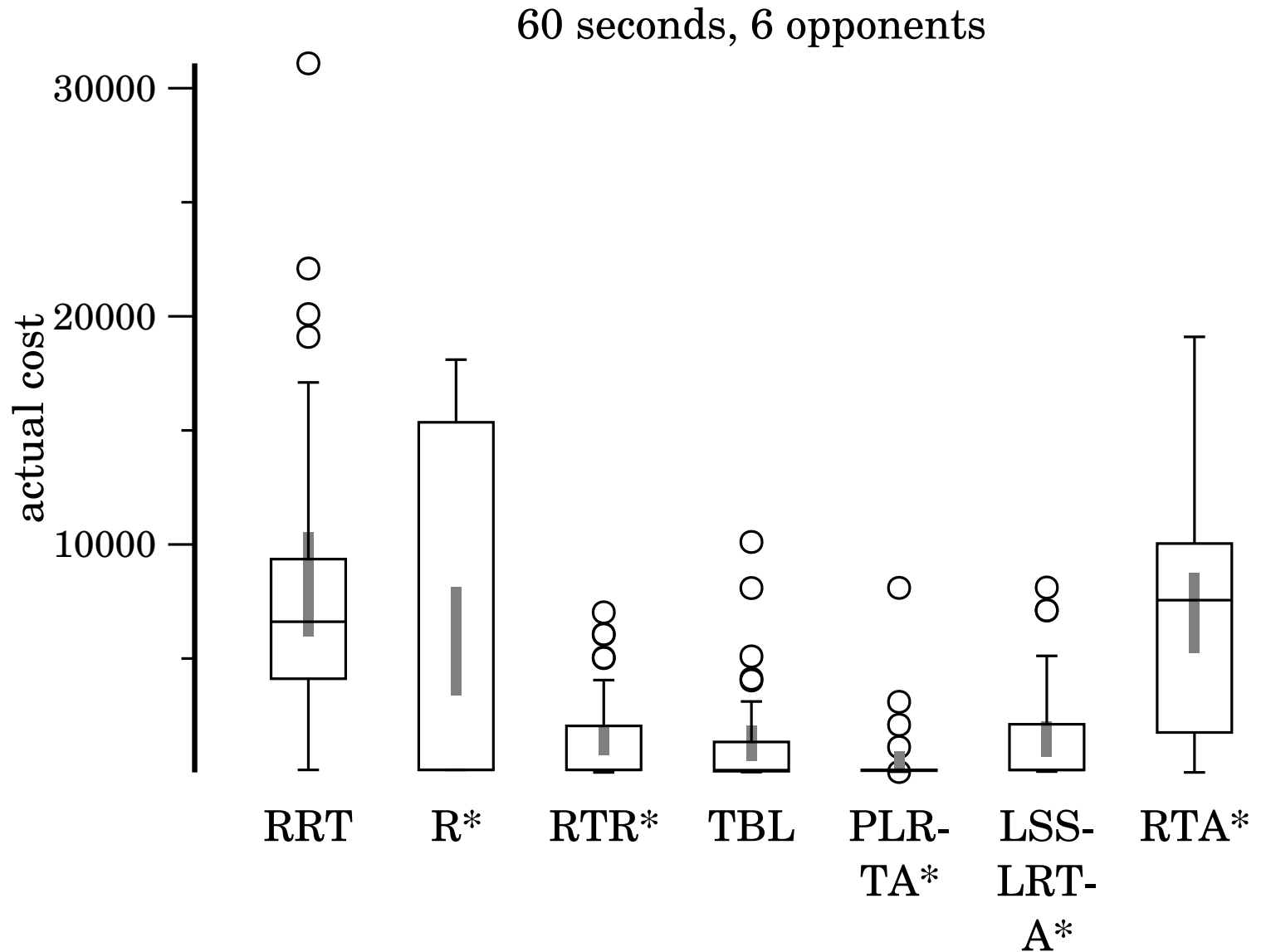
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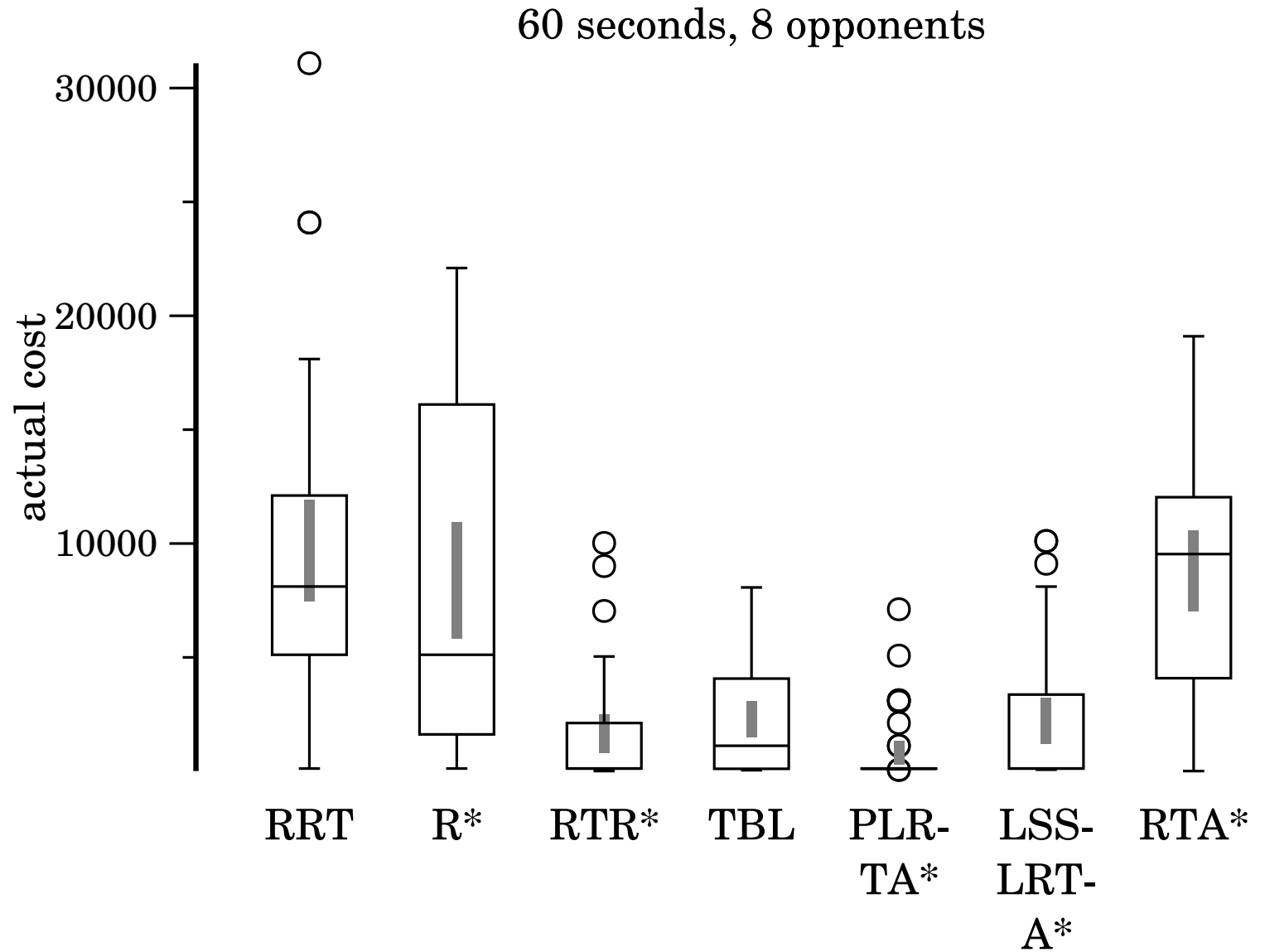
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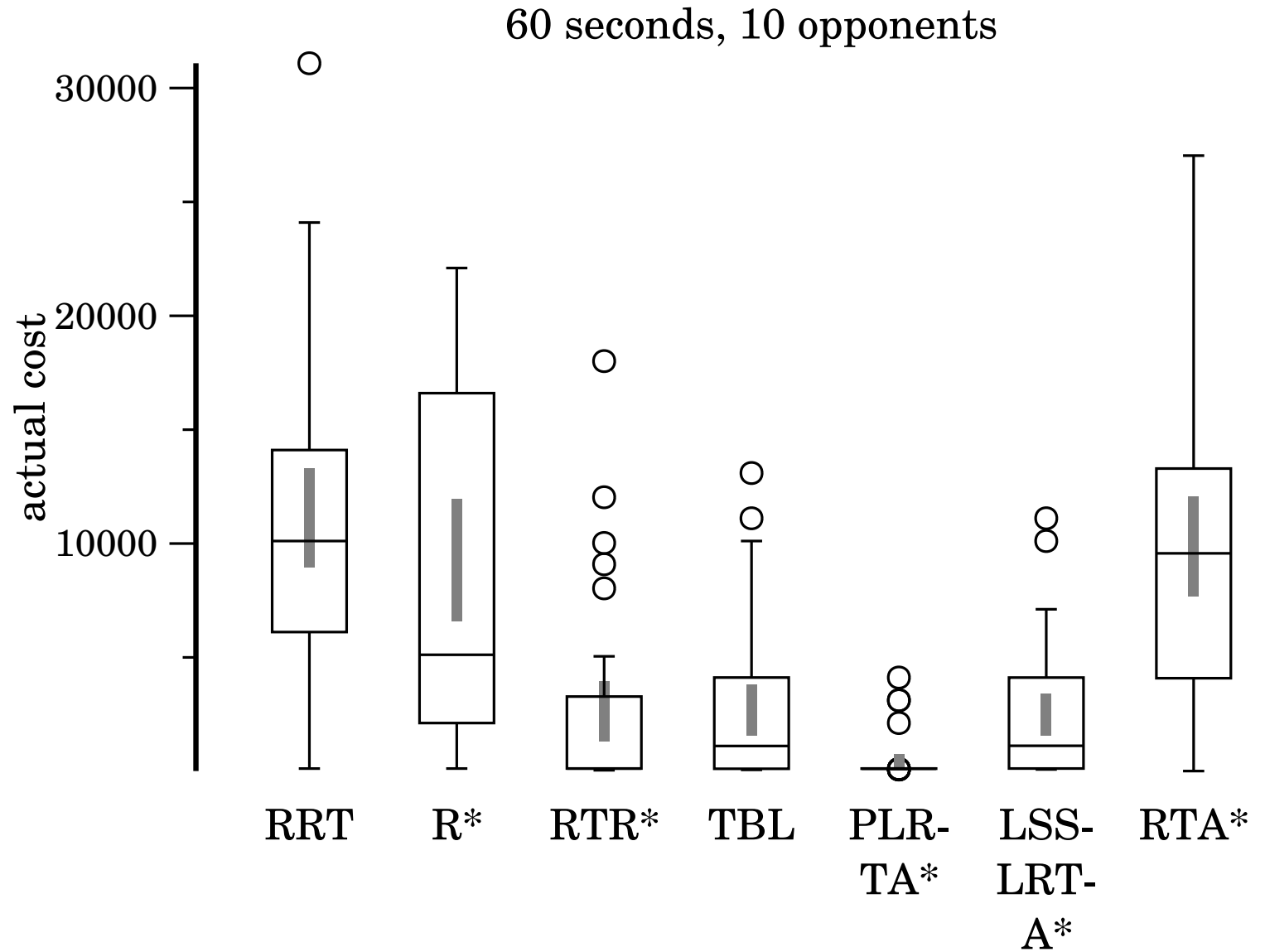
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Scaling

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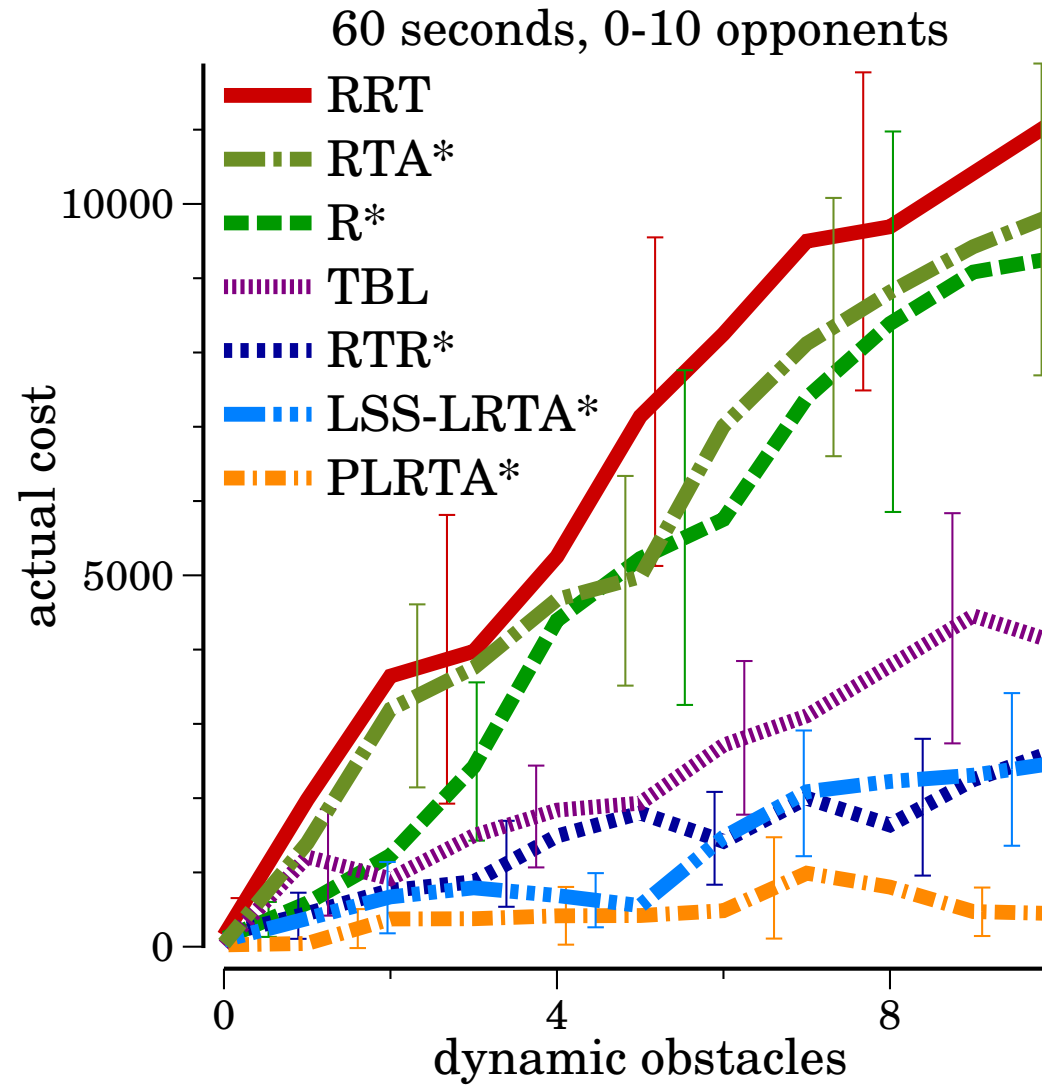
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RTR* better than R*

Scaling

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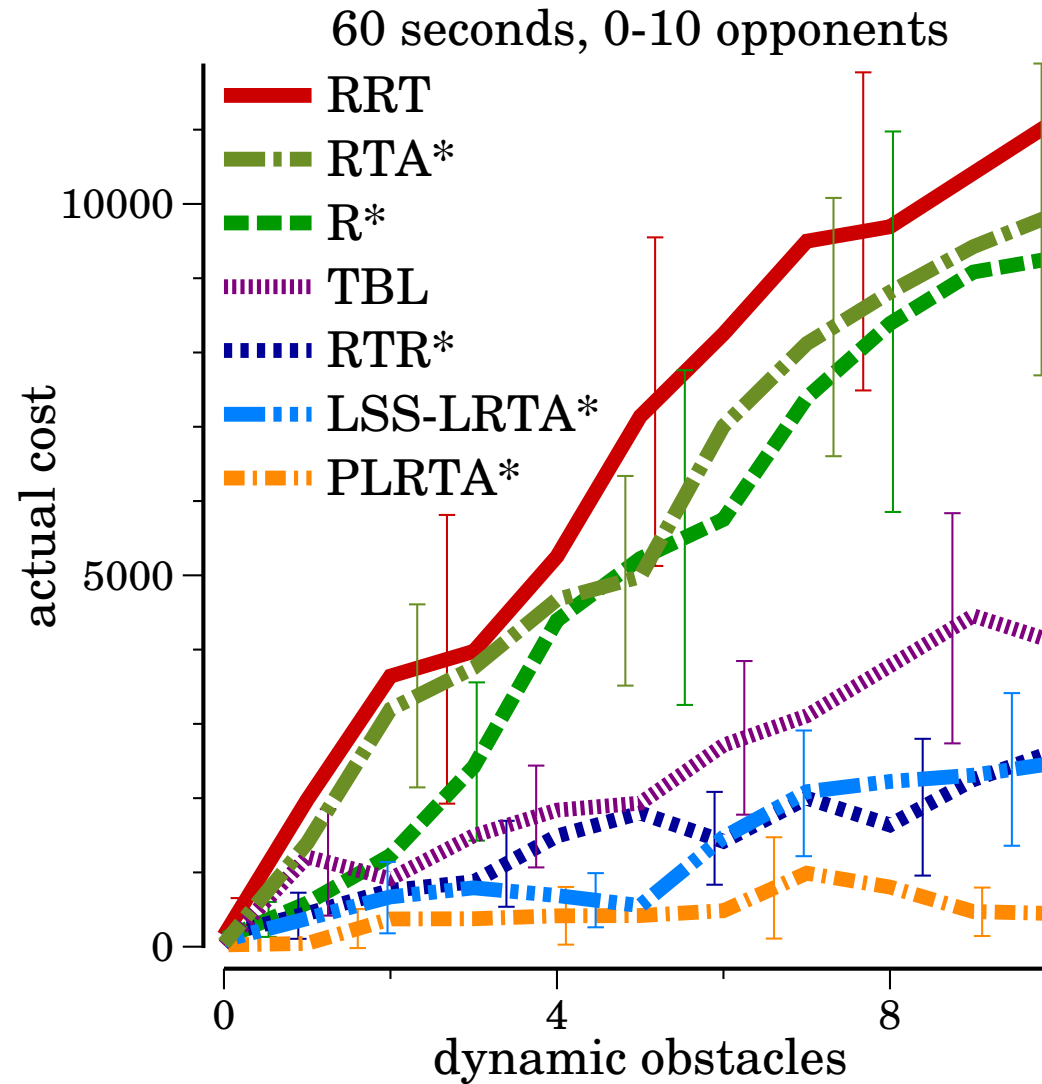
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PLRTA* best

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- Dynamic motion planning is a challenging domain!
- Real-time search with dynamic edge weights is important
- non-trivial to use standard algorithms
- PLRTA* is a simple hack — more work needed!

The University of New Hampshire

tell your students to apply to grad school in CS at UNH!

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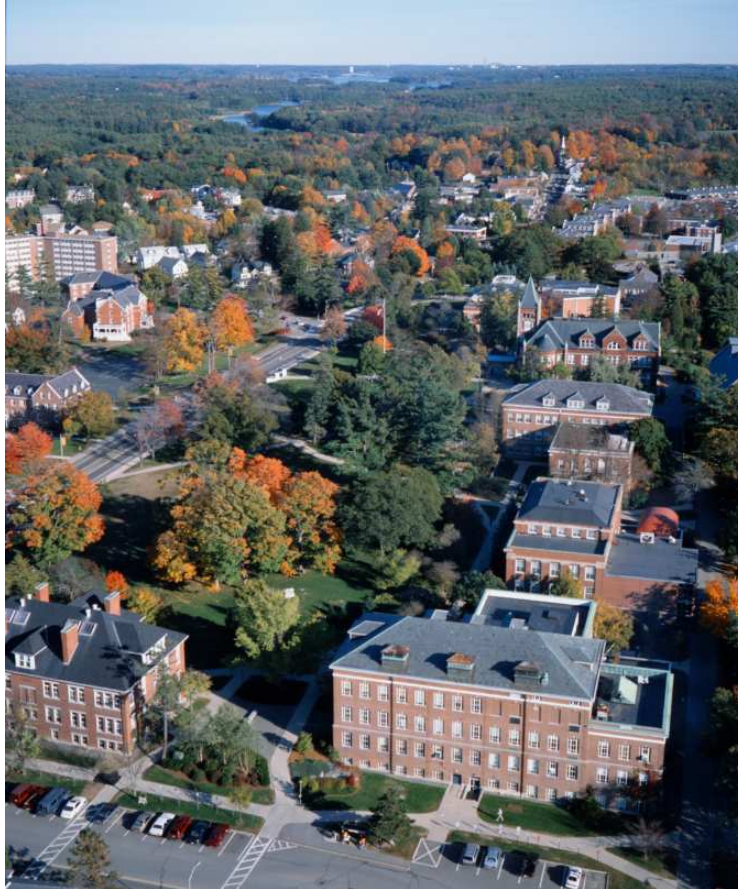
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- friendly faculty
- funding
- individual attention
- beautiful campus
- low cost of living
- easy access to Boston, White Mountains
- strong in AI, infoviz, networking, bioinformatics

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Back-up Slides

Handcrafted Scenarios

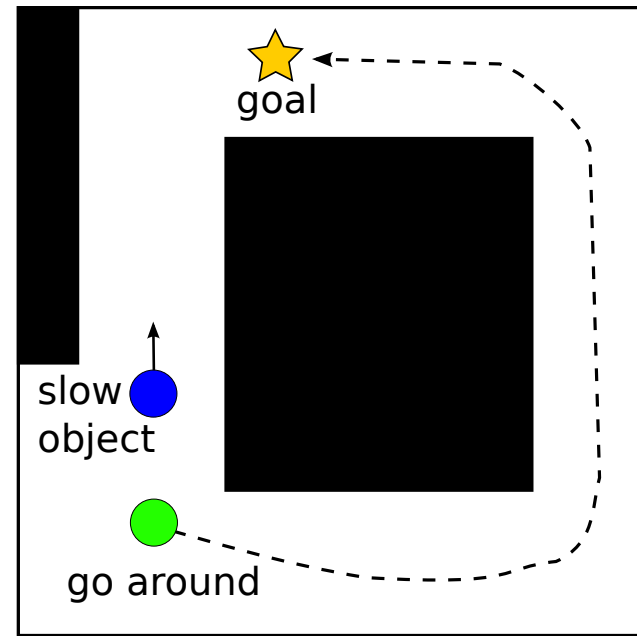
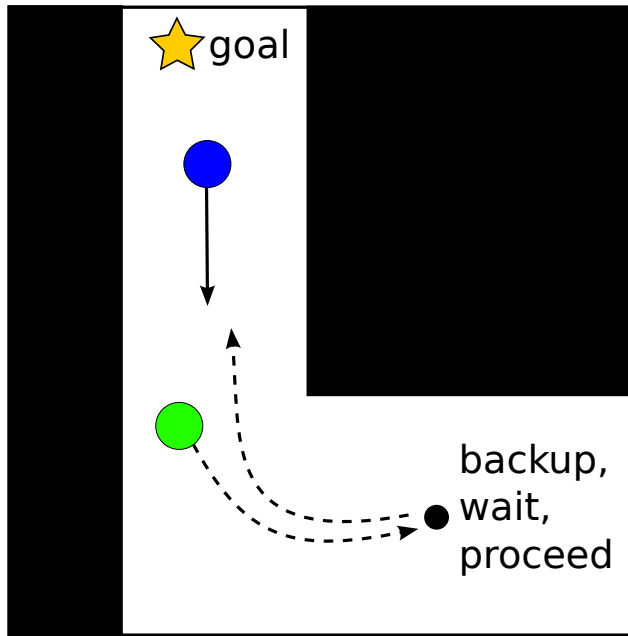
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6 handcrafted benchmarks, qualitative evaluation

PLRTA*: 2 bad

TBL: 3 bad (missed deadline > 10 times per instance)

others: much worse