Written Problems

Don’t forget to prove that your solutions meet the relevant time and/or space bounds!

1. Exercise 22.2–7 in CLRS.

2. Exercise 22.2–9 in CLRS. My understanding is that this is one of the oldest algorithms known (> 2,000 years old).

3. Given a sequence of $n$ values $x_1, x_2, \ldots, x_n$, you will need to answer queries of the form: given $i, j$ (with $i \leq j$), what is the smallest value in the subsequence $x_i, \ldots, x_j$? Show how to answer queries in $O(\lg n)$ time per query using $O(n \lg n)$ space.

4. Give an $O(|V| + |E|)$ time algorithm that, given a graph, determines whether or not it is a forest.

5. Let $S = \{1, 2, \ldots, n\}$ and $f : S \to S$. For $R \subseteq S$, define $g(R) = \{f(x) | x \in R\}$. Design an $O(n)$ time algorithm for determining the largest $R \subseteq S$ such that $g(R) = R$.

6. (Those in 858 only) You observe the price of a stock for the last $n$ days and wonder wistfully how much money you could have made by trading in it. Give an algorithm that finds the best day $i$ to buy and day $j > i$ to sell to maximize your profit. For 2/3 credit, your algorithm can run in $O(n \lg n)$ time; for full credit, it must be $O(n)$ (so that you can afford to run it for all the stocks in NASDAQ).

7. What suggestions do you have for improving this assignment in the future?

Submission

Hand your written work to the TA in class.