

Beyond STRIPS

MDPs

Solving MDPs

1 handout: slides

## Beyond STRIPS

- Comparison
- Extensions
- Setting
- Class Outline

MDPs

Solving MDPs

# Beyond STRIPS

# Comparison

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Beyond STRIPS

■ Comparison

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MDPs

Solving MDPs

Forward: state space

- +: expressivity
- -: irrelevant states

Backward: sets of states

- +: relevant states
- -: larger space, reachable states, expressivity

Partial-order: plan space

- +: small space
- +/-: least commitment
- -: poor heuristics

# STRIPS Extensions

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Solving MDPs

**negated goals:** no problem with CWA

**disjunctive precondition:** for regression, just branch

**conditional effects:** for regression, if we need the effect, plan  
for the condition

**universal preconditions and effects:** just ground goals and  
preconditions

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## MDPs

## Solving MDPs

STRIPS assumes static, deterministic world, discrete time, single discrete actions.

1. time, resources
2. concurrent actions
3. abstraction: hierarchical planning
4. uncertainty: eg, disjunctive effects
5. execution monitoring, replanning
6. continuous state
7. multiple (self-interested) agents

# Class Outline

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## Beyond STRIPS

- Comparison
- Extensions
- Setting

## ■ Class Outline

## MDPs

## Solving MDPs

1. search: heuristics, CSPs, games
2. knowledge representation: FOL, resolution
3. planning: STRIPS, MDPs
4. learning: RL, supervised, unsupervised
5. KR with uncertainty: HMMs, Bayes nets

Beyond STRIPS

**MDPs**

- Examples
- Probability
- Definition
- What to do?
- Break

Solving MDPs

# Markov Decision Processes

# Examples

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Beyond STRIPS

MDPs

■ Examples

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Solving MDPs

1. robot navigation
2. driving
3. business
4. war
5. diagnosis
6. life



# Probability

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Beyond STRIPS

MDPs

■ Examples

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Solving MDPs

propositional

domain: discrete or continuous

0–1, sum to 1

distribution of continuous = density

$$E(X) = \int x P(X = x) dx$$

$P(X = x_1)$  written as  $P(x_1)$  or if  $X$  is true/false,  $P(x)$

conditional (=posterior):  $P(x|y) = P(x \wedge y) / P(y)$

# Markov Decision Process (MDP)

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Beyond STRIPS

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Solving MDPs

**initial state:**  $s_0$

**transition model:**  $T(s, a, s')$  = probability of going from  $s$  to  $s'$  after doing  $a$ .

**reward function:**  $R(s)$  for landing in state  $s$ .

**terminal states:** sinks = absorbing states (end the trial).

# Markov Decision Process (MDP)

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Solving MDPs

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objective:

**total reward:** reward over (finite) trajectory:

$$R(s_0) + R(s_1) + R(s_2)$$

**discounted reward:** penalize future by  $\gamma$ :

$$R(s_0) + \gamma R(s_1) + \gamma^2 R(s_2) \dots$$

# Markov Decision Process (MDP)

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Solving MDPs

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find:

**policy:**  $\pi(s) = a$

**optimal policy:**  $\pi^*$

**proper policy:** reaches terminal state

# What to do?

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- **What to do?**
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Solving MDPs

$$\pi^*(s) =$$

# What to do?

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Solving MDPs

$$\pi^*(s) = \operatorname{argmax}_a \sum_{s'} T(s, a, s') U^{\pi^*}(s')$$

$$U^\pi(s) =$$

# What to do?

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Solving MDPs

$$\pi^*(s) = \operatorname{argmax}_a \sum_{s'} T(s, a, s') U^{\pi^*}(s')$$

$$U^\pi(s) = E\left[\sum_{t=0}^{\infty} \gamma^t R(s_t) \mid \pi, s_0 = s\right]$$

# What to do?

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Solving MDPs

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$$U^\pi(s) = E\left[\sum_{t=0}^{\infty} \gamma^t R(s_t) \mid \pi, s_0 = s\right]$$

The key:

$$U(s) = R(s) + \gamma \max_a \sum_{s'} T(s, a, s') U(s')$$

(Richard Bellman, 1957)



# Break

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Beyond STRIPS

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- Examples
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- Definition
- What to do?

■ Break

Solving MDPs

- asst 3
- textbook
- final project proposals due next Monday in class
  - ◆ project handout
  - ◆ convince me it's interesting and doable
- project presentations: Wed May 9, 9am-noon

Beyond STRIPS

MDPs

Solving MDPs

■ Value Iteration

■ EOLQs

# Solving MDPs

# Value Iteration

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Beyond STRIPS

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■ Value Iteration

■ EOLQs

Repeated Bellman updates:

Repeat until happy

for each state  $s$

$$U'(s) \leftarrow R(s) + \gamma \max_a \sum_{s'} T(s, a, s') U(s')$$
$$U \leftarrow U'$$

# Value Iteration

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Beyond STRIPS

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Solving MDPs

■ Value Iteration

■ EOLQs

Repeated Bellman updates:

Repeat until happy

for each state  $s$

$$U'(s) \leftarrow R(s) + \gamma \max_a \sum_{s'} T(s, a, s') U(s')$$
$$U \leftarrow U'$$

For infinite updates, guaranteed to reach equilibrium.  
Equilibrium is unique solution to Bellman equations!

Beyond STRIPS

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■ Value Iteration

■ EOLQs

- What question didn't you get to ask today?
- What's still confusing?
- What would you like to hear more about?

Please write down your most pressing question about AI and put it in the box on your way out.

*Thanks!*