Shear-Warp Volume Rendering

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From:

Lacroute and Levoy, Fast Volume Rendering Using a Shear-Warp- Factorization of the Viewing Transformation, Siggraph '94

Shear-Warp 9/22/14

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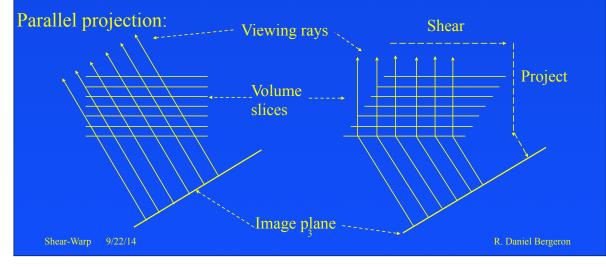
Volume Rendering Overview

- Spatial data structures
 - can lower costs without sacrificing quality
 - e.g., octrees, k-d trees, distance trees
- Image-order algorithms casting rays through pixels
 - traverse spatial d.s. for every ray; multiple traversals
- Object-order algorithms splatting
 - process data once, but hard to terminate processing early
- Shear-warp algorithms
 - efficient data traversal with possibility of early exit

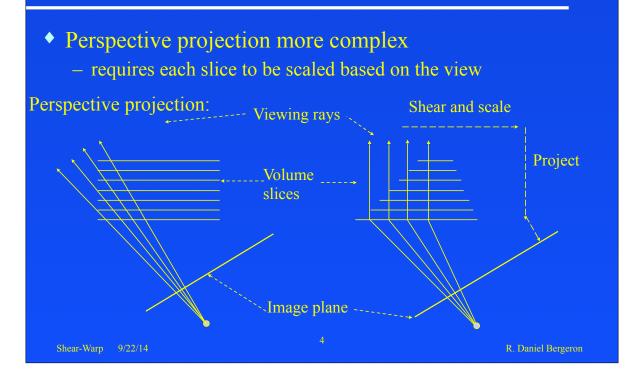
Shear-Warp: Parallel Projection

Sheared object space

- simple transformation of volume allowing efficient projection
- in this space all viewing rays are parallel to a coordinate axis



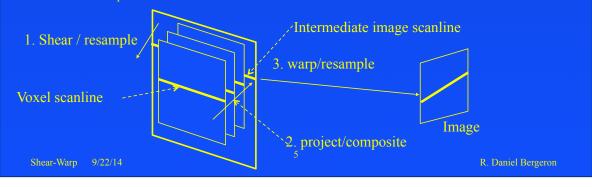
Shear-Warp: Perspective Projection



Basic Algorithm

Determine which of 3 possible slicing directions to use (P).

- 1. Transform volume data to sheared object space by *translating* and *resampling* each slice (S).
- 2. Composite resampled slices in front-to-back order. This produces a 2D intermediate image in sheared object space.
- 3. Transform intermediate image to image space by warping (M_{warp}). This is a 2d *resampling* step.



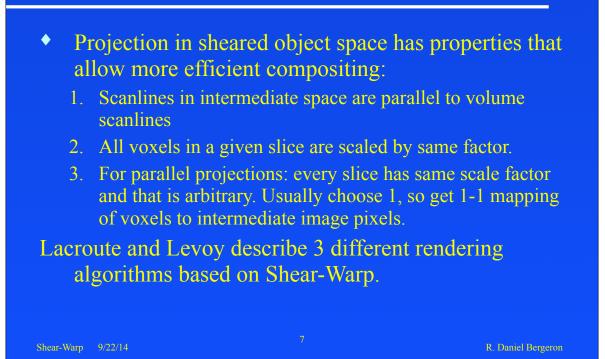
Shear-Warp Factorization

- Shear-Warp can be expressed as factorization of the view transform matrix: M_{view} = M_{warp2d} · M_{shear3d} = M_{warp2d} · S · P
 - P permutes axes that so shear is parallel to slices that are most perpendicular to viewing direction
 - S is shear whose terms can be extracted from M_{vie}

$S_{par} =$	[1	0	S_x	[0		[1	0	S_x	[0
	0	1	S_{y}	0	C	0	1	S_y	0
	0	0	1	0	\mathcal{S}_{pe}	$r^{r} = 0$	0	1	0
	0	0	0	1		$_{rr} = \begin{bmatrix} 1\\0\\0\\0\\0 \end{bmatrix}$	0	S _w	1

= M_{warp2d} transforms sheared object coords to image coords: $M_{warp2d} = M_{view} \cdot P^{-1} \cdot S^{-1}$

Shear-Warp Properties





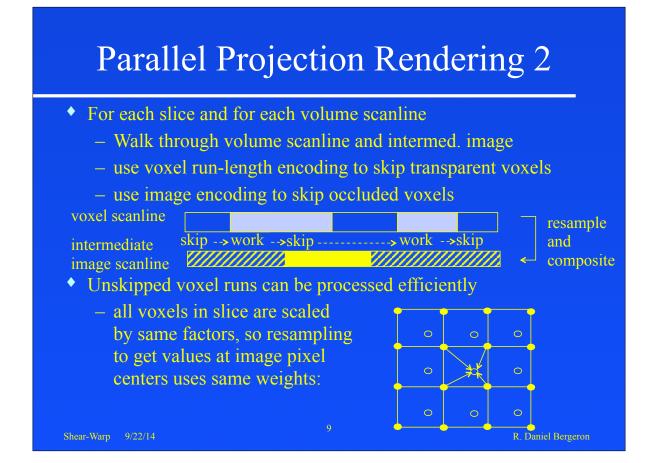
- Parallel view allows *run-length encoding* for data.
 - most data has lots of "empty" space
 - sheared, resampled volume stored as run-length encoded *voxel* scanlines, with 2 kinds of runs: transparent and non-transparent, defined by user-specified threshold
 - intermediate image scanline also stores run information: each opaque pixel (based on user threshold) has pointer to next nonopaque pixel in the scanline. Can skip quickly over runs of opaque pixels.

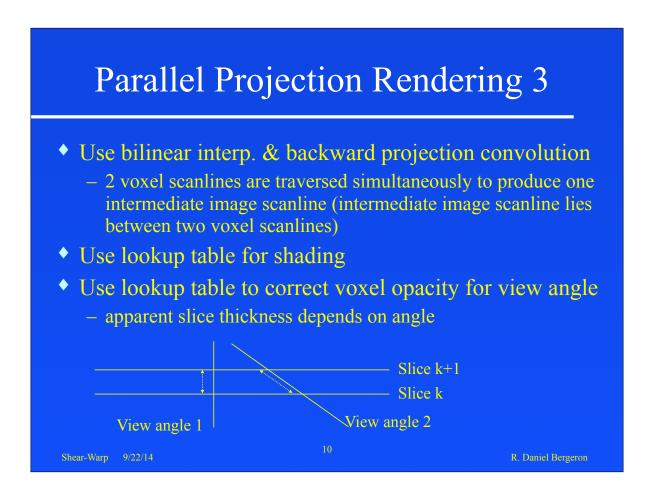


Non-opaque pixel



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Parallel Projection Rendering 4

- After compositing, need to warp 2D intermediate image to final image
 - use general purpose affine image warper with bilinear filter
 - image is small compared to volume, so this is minor part
- Run length encoded data structure
 - created on the fly, but it is (nearly) view-independent
 - create 3 encodings, one for each principal view direction
 - because transparent voxels are not stored, size is usually tractable
 - value of P matrix used to select which version to use

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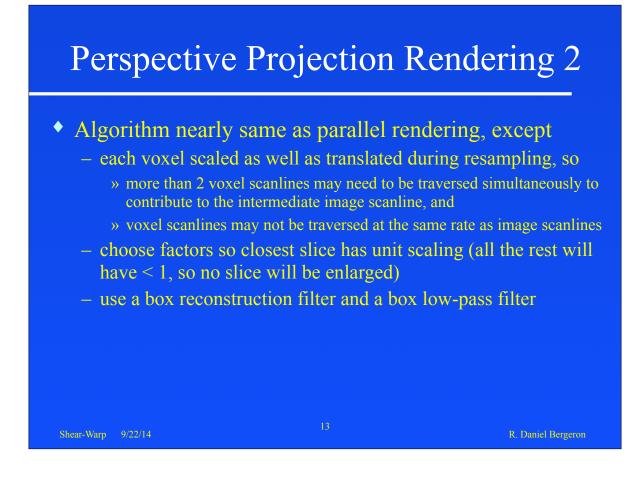
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Perspective Projection Rendering 1

Perspective rays diverge, so uniform sampling is hard

– ray tracing solutions:

- » as distance along ray increases, split ray into multiple rays, or
- » use each sample point to sample larger portion of volume using a mip-map
- splatting: resampling filter footprint must be recomputed for each voxel
- shear-warp: adaptive area sampling is part of the algorithm
 - » each slice is scaled differently, so farther slices are smaller and each ray is, in effect, sampling a larger portion of volume as it gets farther away



Fast Classification Algorithm

- 2 algorithms presented don't allow experimentation with transfer function (it's done in run-length encoding)
- 3rd variation keeps the full volume and evaluates opacity transfer while rendering; need to avoid unnecessary computations
- Key data structures
 - min-max octree: each node stores min/max of all children; built at data loading time; it is not dependent on transfer fcn
 - summed area table: built after transfer fcn defined
 - 3D voxel array

Summed Area Table



Transfer Function Evaluation

Opacity transfer function can be of form:

- $\alpha = f(p, q, ...)$ where p might be data value, q the length of the gradient, or whatever.
- given a threshold, f partitions the multidim space (defined by p,q, ...) into transparent/non-transparent regions
- for region of volume that just contains current scanline
 - 1. find extrema of parameters: min and max of p,q,...
 - 2. determine if opacity is transparent throughout the region
 - if so, discard scanline since it is transparent everywhere
 - else if scanline is small enough, render it
 - else subdivide scanline (and region) and recurse



Fast Classification Rendering Algorithm

- Build min-max octree as preprocessing step; octree is independent of both view and transfer function
- Just before rendering, build summed area table based on current opacity transfer function
- Use either parallel or perspective algorithm accessing 3d array of voxels in scanline order
 - for each scanline, use octree and SA table to skip transparent regions
 - for non-transparent regions, classify each voxel via a lookup table and proceed as before.
 - opaque regions of the image still cause voxel processing to be skipped.
 - note that voxel classification never done in transparent volume regions or opaque image regions; that saves computation

Fast Classification Limitations

Octree traversal and SA table computations add overhead can be reduced by avoiding re-computation: e.g., transparency test for an octree node is computed once on demand, then saved in the tree Opacity transfer function has restrictions

- parameters must be available and function pre-computable for each voxel in order to build octree
- domain of parameter space must be manageable
- context-sensitive segmentation does not satisfy these restrictions
- If major view axis changes, access to scanlines in the 3d array won't follow storage order. For large volumes get thrashing.
 - can reorder the array, but that causes delay
 - best to use this algorithm only for small range of views; once desired opacity function is defined, switch to one of other algorithms.

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Performance Results
 Lacroute/Levoy tested on a modest machine: SGI Indigo R4000 with 64Mbytes and no graphics accelerator
 256x256x225 head MRI data set using gray scale

 Parallel Perspective Fast classification/Parallel
 Avg time (sec)
 1.2
 3.3
 2.8
 Memory (Mb)
 13
 13
 61

 Color rendering takes about twice as long
 Ray casting versions were 5 times longer for 128³ data sets and

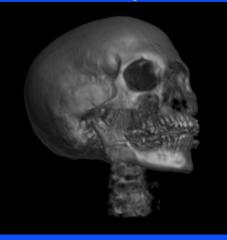
10 times longer for 256³ data sets

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Image Quality

 Many images are virtually identical to ray casting. The 2 resampling steps might lead to blurring, but they don't see it.

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Ray Casting

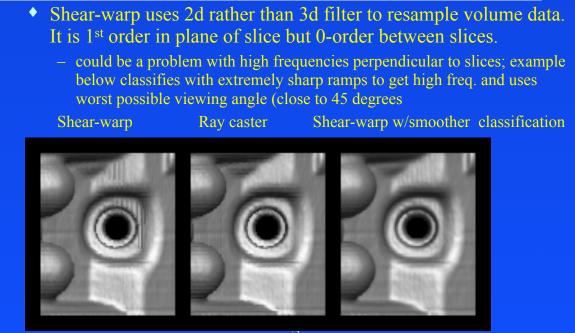


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Image Quality Problems



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