

Anticipatory On-line Planning

Ethan Burns¹, J. Benton², Wheeler Ruml¹, Sungwook Yoon³, and Minh Do⁴



[Thanks to NSF, DARPA, ONR, and ARL for support]

An On-line Planning Problem

Introduction

■ Example: UAVs

■ Example Cont'd

■ Contributions

Formalization

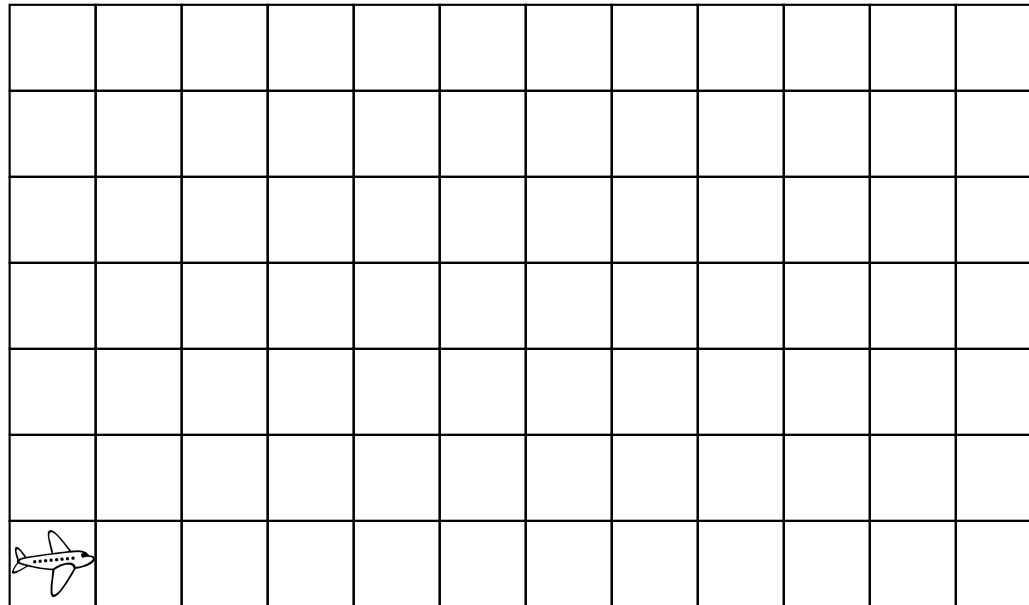
Hindsight Opt.

Experiments

Conclusion

Consider a UAV fulfilling observation requests:

- Observation requests (start–end locations) arrive over time
 - ◆ Requests draw from known distribution
- Minimize time to service observations
 - ◆ Re-planning may reduce cost.



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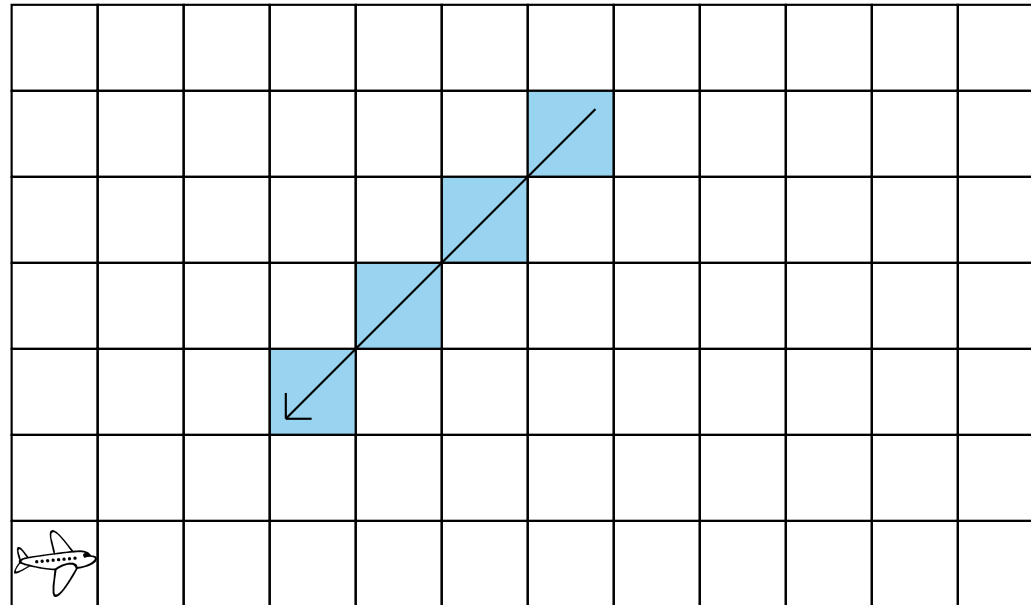
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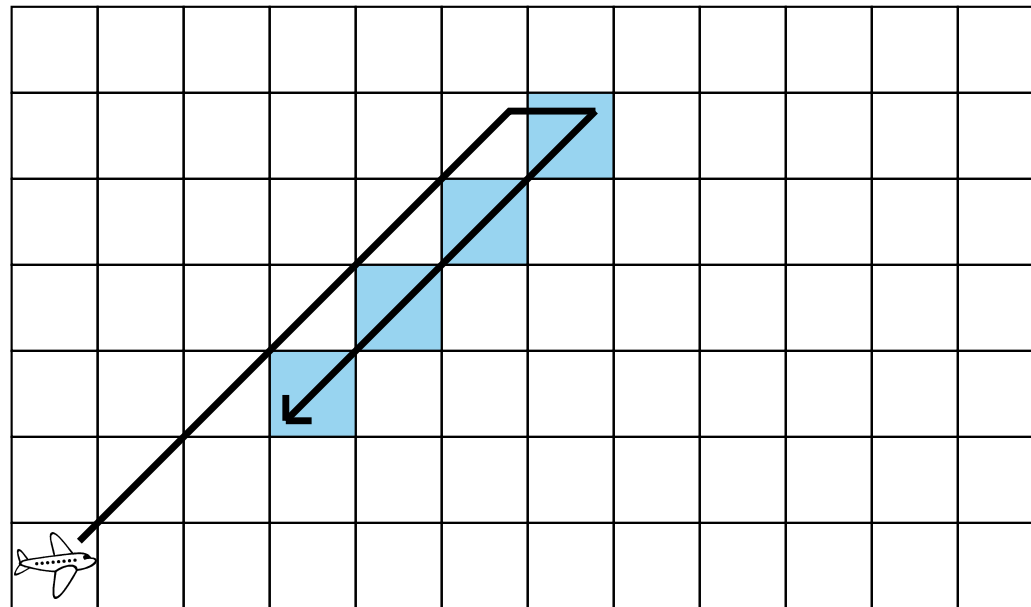
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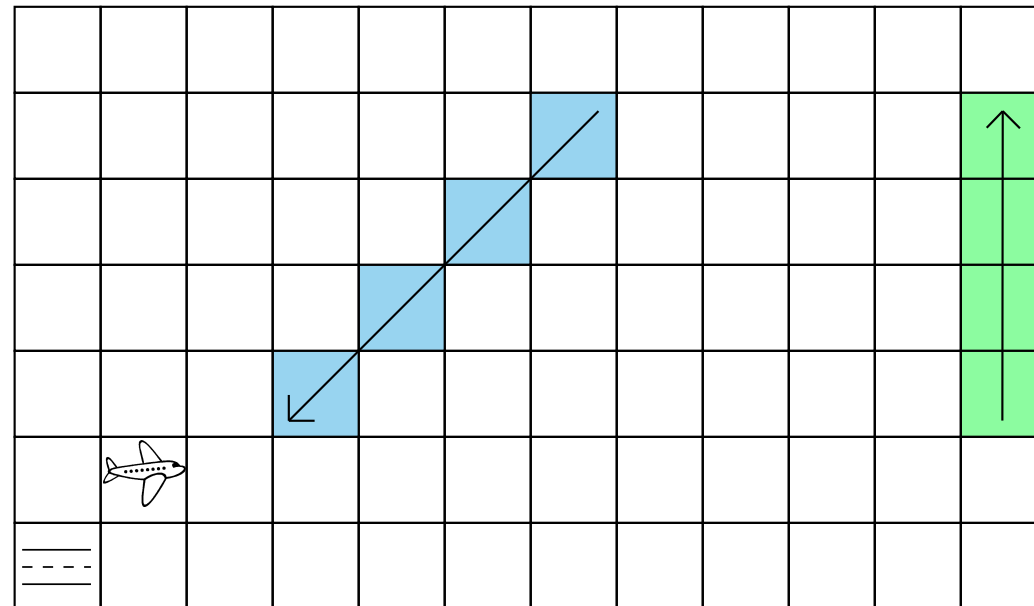
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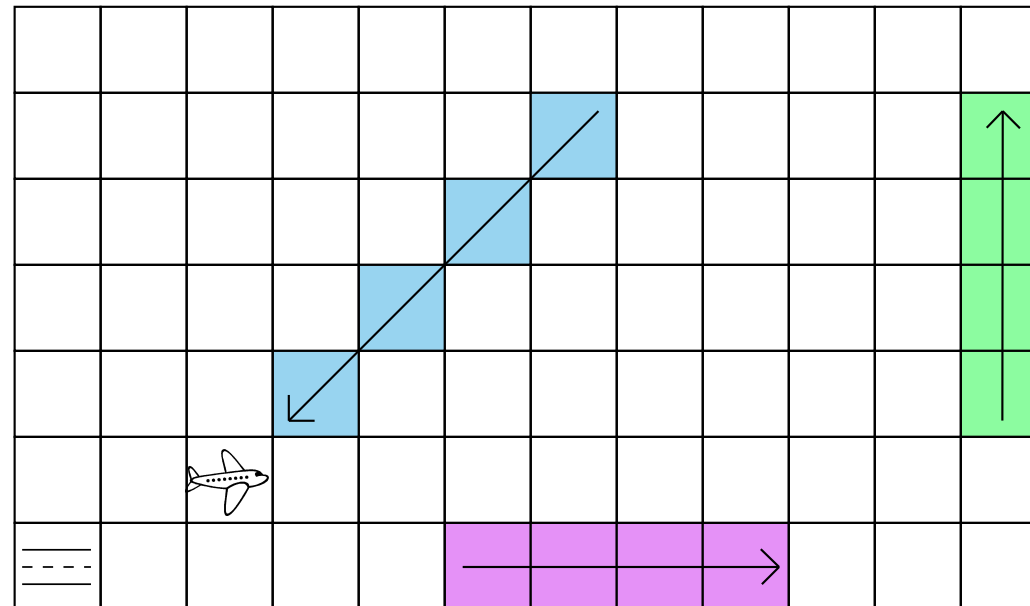
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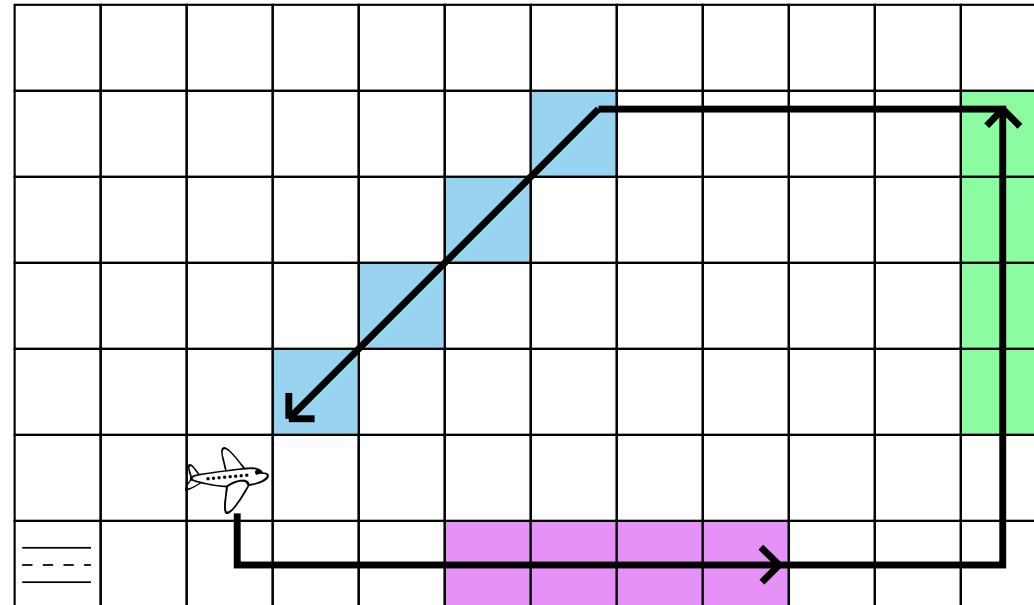
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Example Continued

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Observations:

- Life is more than one goal—others will come
- “Planner” can run, even before goal arrives

Other examples:

- Life (e.g., insurance)
- Satellite planning
- Taxi/ambulance dispatching
- Manufacturing
- PARC printer

Opportunity:

- Estimate of future goals

Contributions

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- Simple and clean formalization of on-line planning
 - ◆ *Exposes key issues, yet very approachable*
- Show that hindsight optimization applies easily
 - ◆ *Not just for probabilistic planning any more!*
- Show that simple HOP is better than “reactive” planning
 - ◆ *Many avenues for future work*

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■ OCPP

■ Reactive

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On-line Continual Planning Problems

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Like classical planning:

- Action effects are deterministic

but, on-line:

- Goals arrive stochastically, distribution is known

Like MDP:

- Minimize total cost, approximate over a fixed horizon, H
- When evaluating actions:

$$V_H^*(s_1) = \min_{a_1, \dots, a_H} E_{s_2, \dots, s_H} \left[\sum_{i=1}^H C(s_i, a_i) \right]$$

- State incorporates unachieved goals

Simple and clean formulation of on-line planning

A Simple Approach: Reactive Planning

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1. Plan for the current goals
2. Execute the plan until the goals change
3. Repeat

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■ OCPP

■ **Reactive**

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1. Plan for the current goals
2. Execute the plan until the goals change
3. Repeat

Doesn't take advantage of knowledge about future goals

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- Anticipatory
- MDP
- HOP
- HOP Cont'd
- Other Apps.

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Hindsight Optimization

A Better Approach: Anticipatory On-line Planning

- Consider possible future goals when planning actions

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MDP

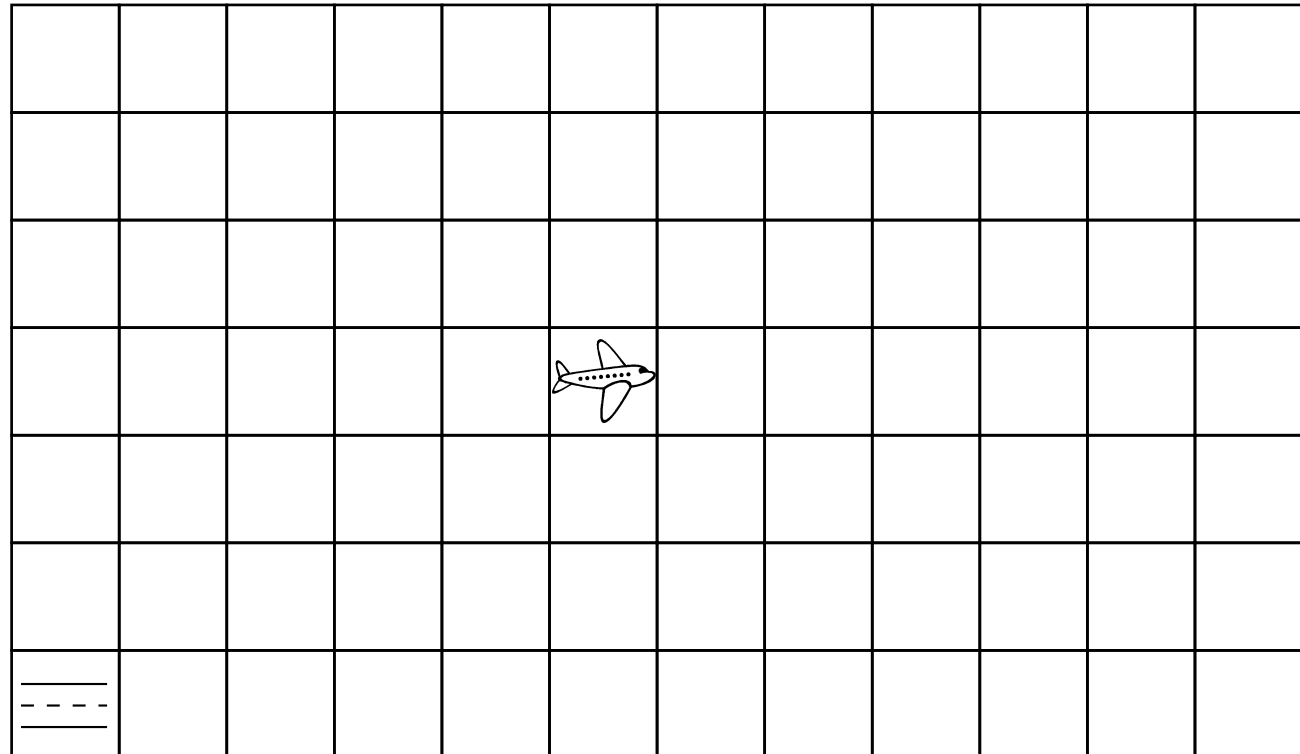
HOP

HOP Cont'd

Other Apps.

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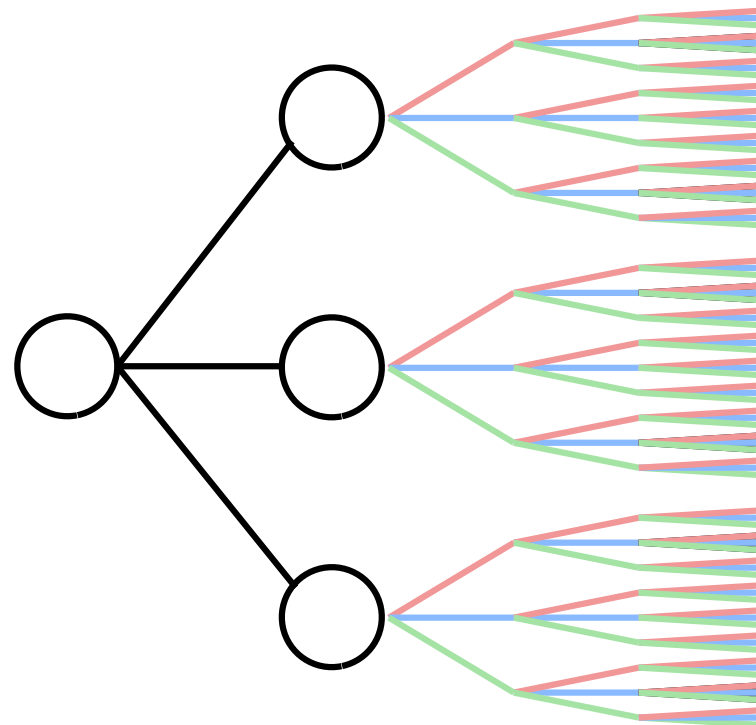
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Markov Decision Process

Solve for all possible future goals

$$V_H^*(s_1) = \min_{a_1, \dots, a_H} E_{s_2, \dots, s_H} \left[\sum_{i=1}^H C(s_i, a_i) \right]$$



A 3x3 UAV with ≤ 3 requests has tens of millions of states.

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■ Other Apps.

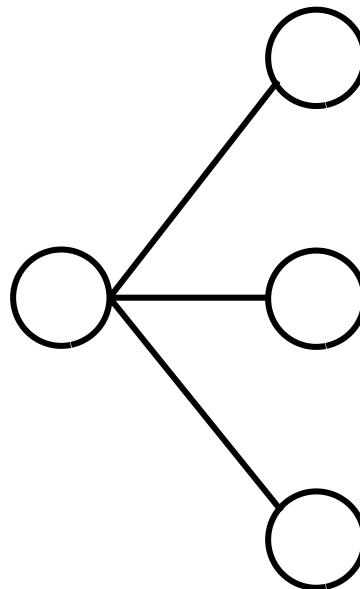
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Hindsight Optimization for Anticipatory Planning

Hindsight optimization – solve a sample of future goals

$$\hat{V}_H(s_1) = E_{s_2, \dots, s_H} \left[\min_{a_1, \dots, a_H} \sum_{i=1}^H C(s_i, a_i) \right]$$



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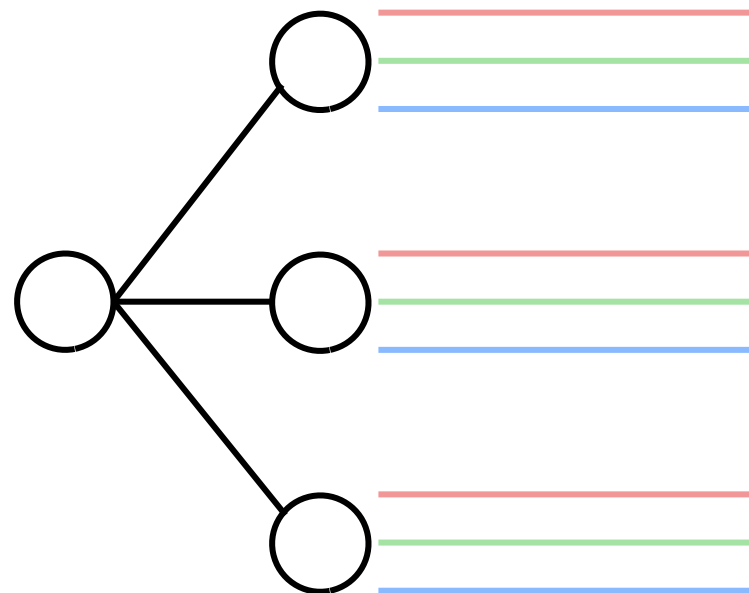
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Hindsight Optimization for Anticipatory Planning

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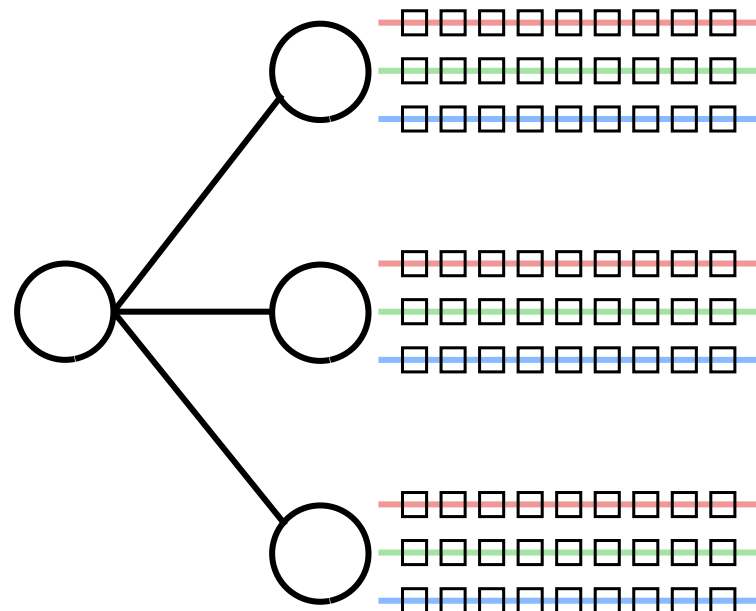
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Hindsight Optimization for Anticipatory Planning

Hindsight optimization – solve a sample of future goals

$$\hat{V}_H(s_1) = E_{s_2, \dots, s_H} \left[\underbrace{\min_{a_1, \dots, a_H} \sum_{i=1}^H C(s_i, a_i)}_{\text{Deterministic Planning}} \right]$$



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1. Sample future goal arrivals
2. For each action
 Evaluate mean plan cost over sampled futures
3. Take the best action
4. Repeat

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1. Sample future goal arrivals
2. For each action
 Evaluate mean plan cost over sampled futures
3. Take the best action
4. Repeat

Simple, and uses knowledge about goal arrivals

Other Applications

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■ MDP

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■ HOP Cont'd

■ **Other Apps.**

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HOP has been applied to:

- On-line scheduling (Chong, Givan, Chang 2000)
- Stochastic integer programs (Mercier and van Hentenrych 2007)
- Probabilistic planning (Yoon et al. 2008)

Now:

- **On-line Planning**

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■ Manufacturing

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How do we compare different techniques?

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Goal: **gain the most reward**

How do we know our technique is doing well?

How do we compare different techniques?

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Goal: **gain the most reward**

How do we know our technique is doing well?

- How does it compare to optimal?
 - ◆ Imagine we have an oracle that knows the future
- How does it compare to a simple planner?
 - ◆ Greedy: evaluate cost-to-go heuristic on each successor
 - ◆ Go to the state with the lowest heuristic value

How do we compare different techniques?

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Normalized reward:

reward normalized between optimal (1) and greedy (0)

UAV Domain

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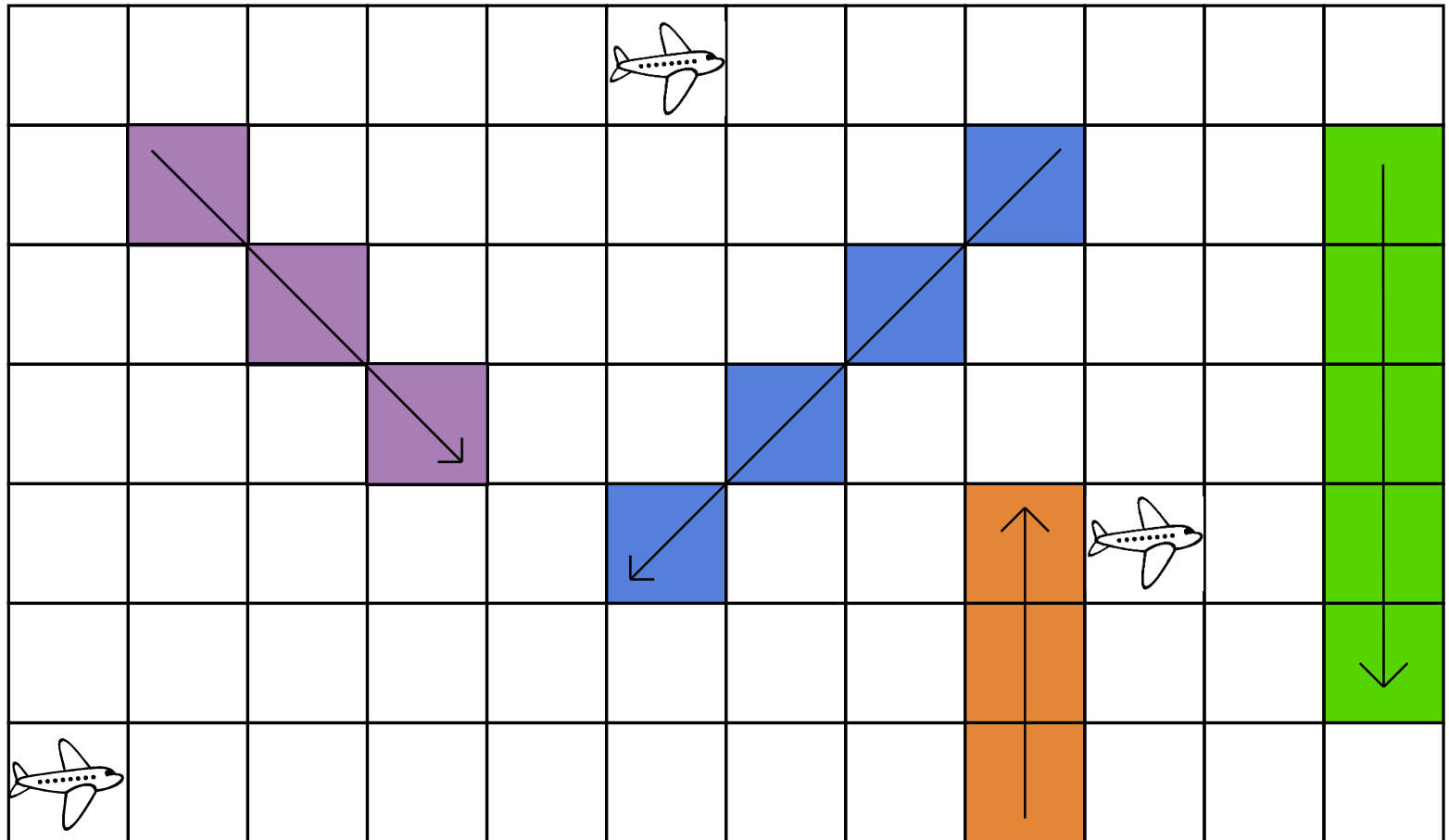
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UAV Results

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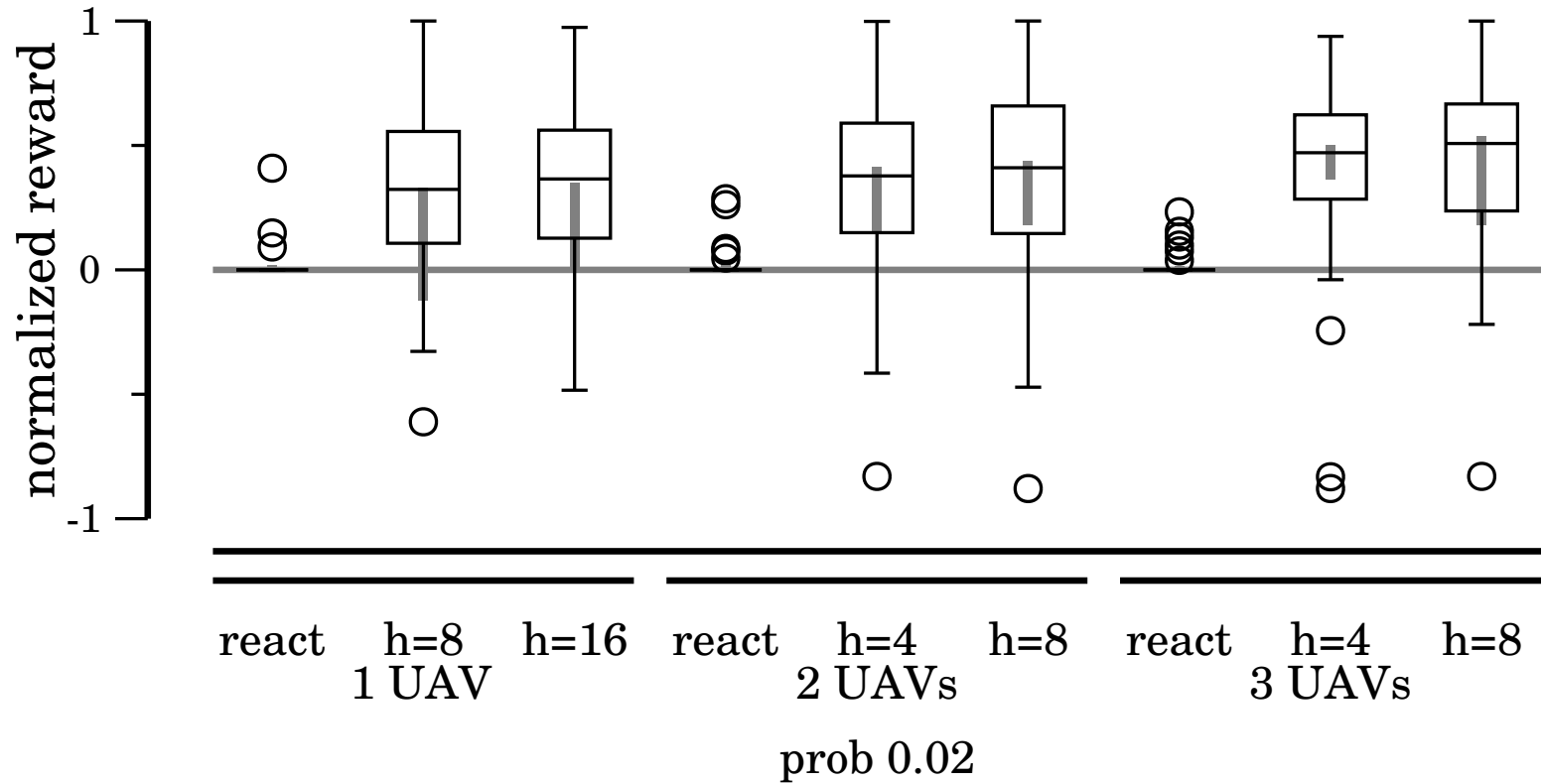
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Reactive ~ greedy, HOP gives the most reward

Manufacturing Domain

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■ How?

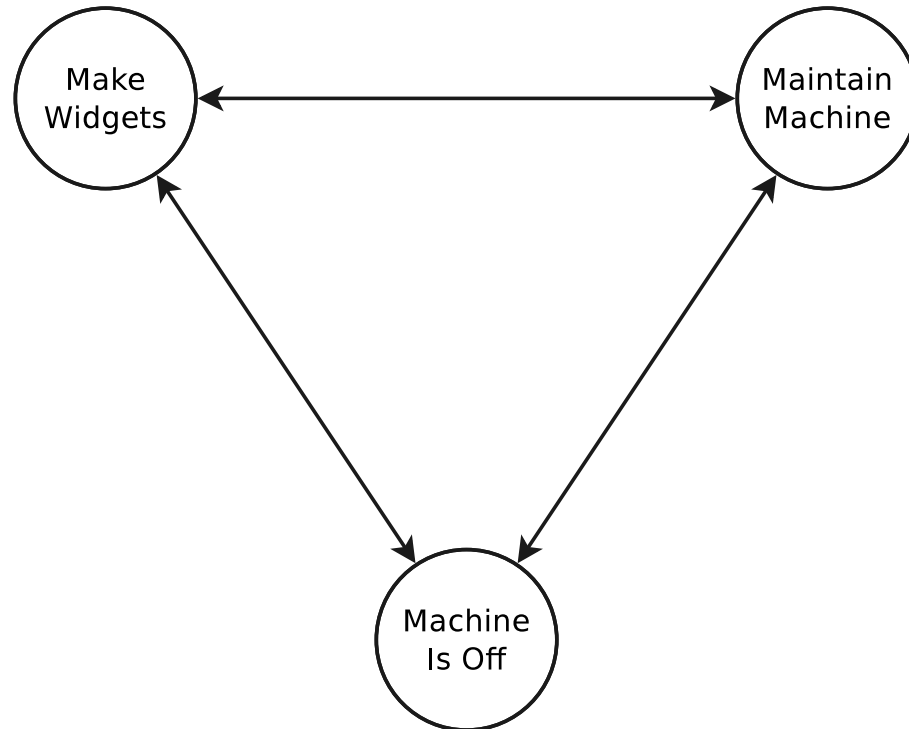
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Manufacturing Results

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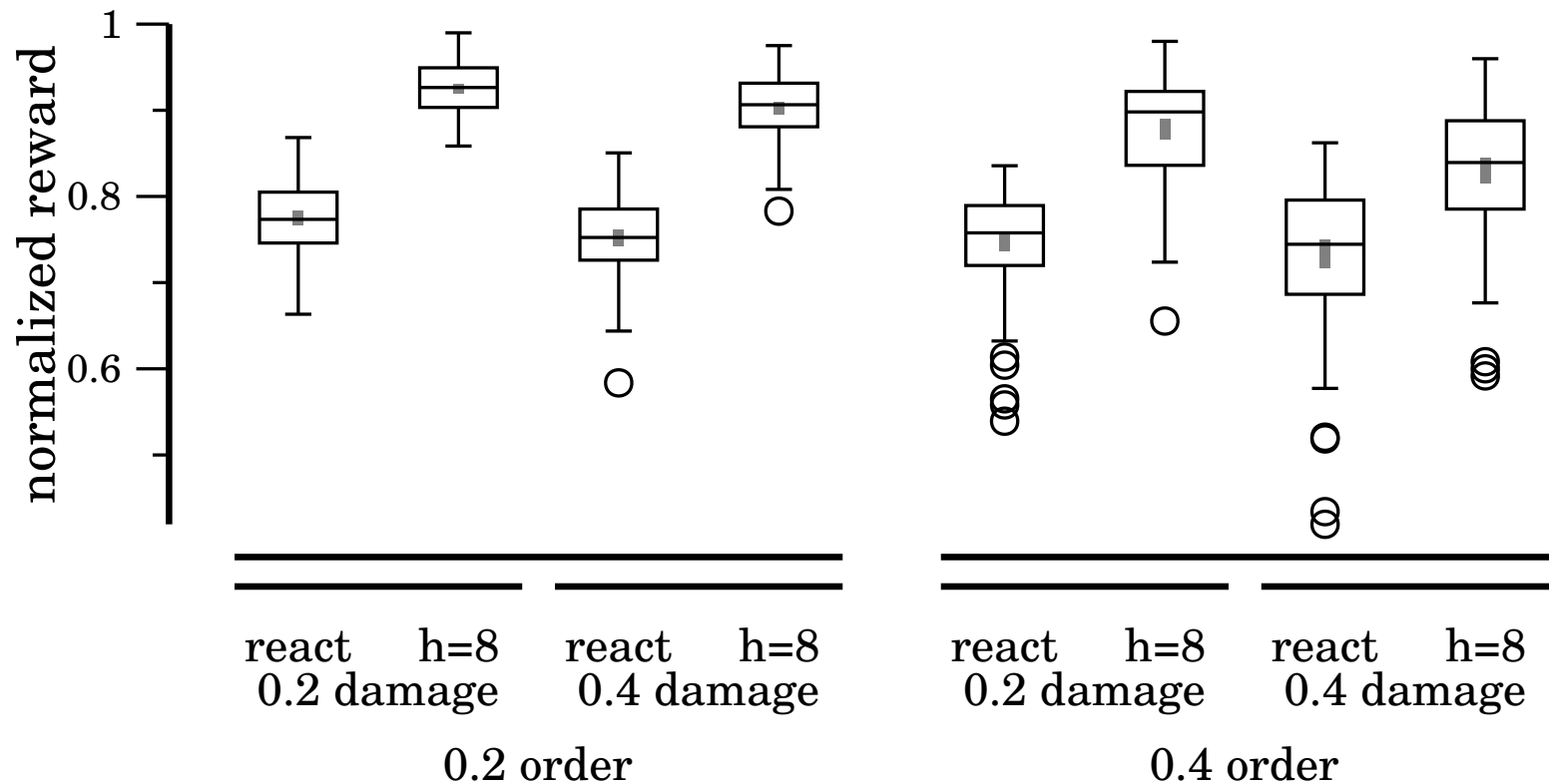
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HOP is close to optimal and gives the most reward

Pros and Cons

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■ Pros and Cons

■ Conclusion

Pros:

- HOP simple to implement (just need deterministic planner)
- Better than the simple reactive approach
- Better than MDP solvers for these problems
 - ◆ 3x3 UAV: LRTDP 100x slower and worse than greedy

Cons:

- HOP slower than reactive
 - ◆ Finds many plans instead of just one
 - ◆ Reactive: ~ 0 seconds, HOP: 0.002–10 seconds
 - ◆ But, see (Yoon et al. ICAPS 2010)

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■ Pros and Cons

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- Many problems are on-line continual planning problems
- We can take advantage of the known goal distribution
- Hindsight optimization is simple and works well

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